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First Direct Observation of Muon Antineutrino Disappearance

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This Letter reports the first direct observation of muon antineutrino disappearance. The MINOS experiment has taken data with an accelerator beam optimized for $\bar{\nu}_\mu$ production, accumulating an exposure of 1.71×10^{20} protons on target. In the Far Detector, 97 charged current $\bar{\nu}_\mu$ events are observed. The no-oscillation hypothesis predicts 156 events and is excluded at 6.3σ . The best fit to oscillation yields $|\Delta\bar{m}^2| = [3.36_{-0.40}^{+0.46}(\text{stat}) \pm 0.06(\text{syst})] \times 10^{-3} \text{ eV}^2$,

$\sin^2(2\bar{\theta}) = 0.86_{-0.12}^{+0.11}(\text{stat}) \pm 0.01(\text{syst})$. The MINOS ν_μ and $\bar{\nu}_\mu$ measurements are consistent at the 2.0% confidence level, assuming identical underlying oscillation parameters.

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Observations by many experiments provide compelling evidence for neutrino oscillation [1–9]. This oscillation, a consequence of the quantum mechanical mixing of the neutrino mass and weak flavor eigenstates, is governed by the elements of the Pontecorvo-Maki-Nakagawa-Sakata matrix [10], parameterized by three mixing angles and a CP phase, and by two independent neutrino mass-squared differences. As the measurement precision on oscillation parameters improves, so does the potential for observing new phenomena. In particular, measured differences between the neutrino and antineutrino oscillation parameters would indicate new physics. CPT symmetry, one of the most fundamental assumptions underlying the standard model, constrains the allowed differences in the properties of a particle and its antiparticle [11] and requires that their masses be identical. This symmetry has been extensively tested in other sectors, most notably the kaon sector [12]. Additionally, neutrinos passing through matter could experience nonstandard interactions [13] that alter the ν_μ and $\bar{\nu}_\mu$ disappearance probabilities and, thus, the inferred oscillation parameters [14].

The MINOS experiment has used a ν_μ beam to measure the larger (atmospheric) mass-squared difference $|\Delta m^2| = (2.32_{-0.08}^{+0.12}) \times 10^{-3} \text{ eV}^2$ and the mixing angle $\sin^2(2\theta) > 0.90$ (90% confidence limit [C.L.]) through observation of ν_μ disappearance [3, 15]. The corresponding antineutrino oscillation parameters are much less precisely known.

This Letter describes the first direct observation of $\bar{\nu}_\mu$ disappearance consistent with oscillation, yielding the most precise measurement to date of the larger antineutrino mass-squared difference. The only previous measurements from $\bar{\nu}_\mu$ -tagged samples, providing weak constraints, come from the MINOS atmospheric neutrino sample [16] and an analysis of the $\bar{\nu}_\mu$ component of the MINOS ν_μ data sample [17, 18]. The strongest indirect constraints come from a global fit [19], dominated by Super-Kamiokande data which measure the sum of atmospheric ν_μ and $\bar{\nu}_\mu$ interaction rates.

For this measurement the NuMI beam line [20] was configured to produce a $\bar{\nu}_\mu$ -enhanced beam. The current in the magnetic horns was configured to focus negative pions and kaons produced by 120 GeV protons incident on a graphite target. Most mesons travel along a 675 m long decay pipe, filled with helium at 0.9 atm, and decay to produce a $\bar{\nu}_\mu$ -enhanced beam with a peak energy of 3 GeV (see Fig. 1). Interactions of ν_μ comprise a fraction of all charged current (CC) events in the MINOS detectors which rises from about 21% below 6 GeV up to about 81% at 20 GeV, in the case of no oscillation.

The data set in this paper corresponds to an exposure of 1.71×10^{20} protons on target (POT).

The MINOS experiment uses two similar detectors located 1.04 km [Near Detector (ND)] and 735 km [Far Detector (FD)] from the NuMI target. The $\bar{\nu}_\mu$ CC interaction rate as a function of reconstructed $\bar{\nu}_\mu$ energy is measured in each detector. The measured FD energy spectrum is compared to that predicted using the ND data. In this comparison, many sources of systematic uncertainty cancel. Antineutrino oscillation causes a deficit in the FD with an energy dependence, in the approximation of two-flavor mixing, of

$$P(\bar{\nu}_\mu \rightarrow \bar{\nu}_\mu) = 1 - \sin^2(2\bar{\theta}) \sin^2\left(\frac{1.267\Delta\bar{m}^2 L}{E}\right) \quad (1)$$

where L [km] is the distance from the point of antineutrino production, E [GeV] the $\bar{\nu}_\mu$ energy, $\Delta\bar{m}^2$ [eV^2] the antineutrino mass-squared difference and $\bar{\theta}$ the antineutrino mixing angle.

The MINOS detectors [21] are tracking calorimeters, formed of planes of steel interleaved with planes of scintillator. The scintillator is divided into strips with a width of 4.1 cm. In CC interactions, $\bar{\nu}_\mu(\nu_\mu) + N \rightarrow \mu^+(\mu^-) + X$, a hadronic shower (X) and a muon track may be observed. The hadronic energy is measured by summing the amount of light produced in the scintillator. Muon energy is measured by range for contained tracks or, for exiting tracks, by the curvature in a ~ 1.4 T toroidal magnetic field. The incoming neutrino energy is reconstructed as the sum of the hadronic and muon energies. For the data presented in this Letter, the fields in both detectors focus μ^+ and defocus μ^- , allowing the separation of $\bar{\nu}_\mu$ and ν_μ CC interactions on an event-by-event basis.

A sample of $\bar{\nu}_\mu$ CC interactions is isolated by identifying the presence of a positively charged track. Neutral current (NC) interactions produce only a hadronic shower at the vertex. Similarly, CC interactions of ν_e and $\bar{\nu}_e$ (which correspond to 2.0% of all CC interactions at the ND) produce only showerlike activity. The main background arises from tracks reconstructed out of shower activity. This background is reduced [2, 22] by a method which uses four variables to identify the presence of an isolated track with muonlike energy deposition. These four variables are the track length, the average pulse height per plane along the track, the transverse energy deposition profile of the track, and the fluctuation of the energy deposited in scintillator strips along the track, and are combined using a k -nearest-neighbor (k NN) algorithm [23] to produce a single output variable. The position of the selection cut on this variable

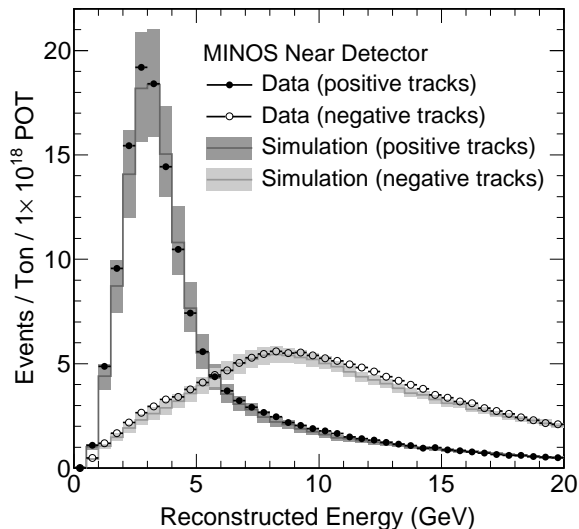


FIG. 1: The reconstructed energy spectra of events in the Near Detector classified as charged current interactions, separated according to the reconstructed charge of the track. The events with a negatively charged track are not used in the oscillation analysis. The shaded bands represent the systematic uncertainty on the simulation.

is tuned to optimize the statistical sensitivity to $|\Delta\bar{m}^2|$, yielding the same selection criterion as for the MINOS ν_μ analysis [2].

The charge of reconstructed muon tracks is determined by analyzing the curvature of the track in the magnetic field [24]. Figure 1 shows the reconstructed energy of selected CC events in the ND, separated according to the measured track charge sign. The events reconstructed with a negatively charged track consist primarily of ν_μ CC interactions, and are removed from further analysis. Events with a positively charged track form the selected $\bar{\nu}_\mu$ CC sample, and are used to predict the expected energy spectrum at the FD. Below 6 GeV, where the majority of the oscillation signal is expected, the selected $\bar{\nu}_\mu$ CC sample at the ND has a purity, obtained from the simulation, of 98% (the background consisting of 1% NC events, 1% ν_μ CC events). Above 6 GeV the purity is 88%, and the contamination is primarily ν_μ CC events; higher momentum muons follow a less curved path, giving a greater probability of charge misidentification. The total $\bar{\nu}_\mu$ CC reconstruction and selection efficiency is 93%.

The measured ND energy spectrum is used to predict the FD spectrum, as previously [1, 2, 17]. This procedure is particularly effective in mitigating sources of systematic uncertainty which affect both detectors similarly. For example, uncertainties on the neutrino flux and cross sections dominate the systematic error band on the ND

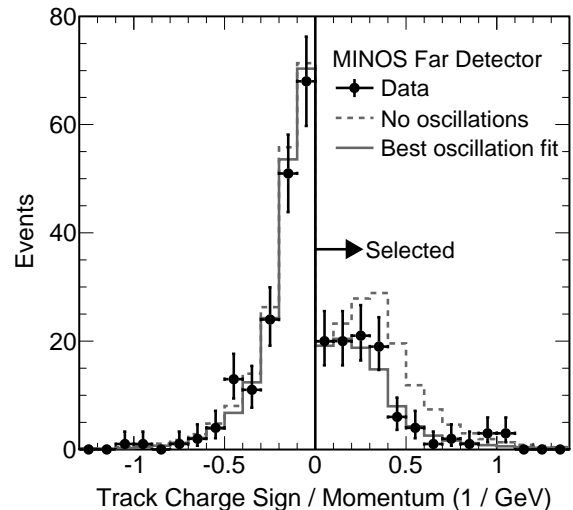


FIG. 2: The distribution of the sign of the reconstructed charge divided by the momentum of selected muon tracks in the Far Detector. The simulated distribution is shown in the case of no oscillation and oscillation assuming the best fit ν_μ parameters from Ref. [3] and $\bar{\nu}_\mu$ parameters from this analysis.

energy spectrum, shown in Fig. 1, but have a negligible impact on the oscillation measurement.

The production of hadrons in the NuMI target is constrained by fits to the ND data [1, 2]. These fits use data from the ν_μ beam to determine the π and K yields as a function of their transverse and longitudinal momenta at production. Recent measurements [25] of the ratio of π^+/π^- yields are included as constraints in these fits. This tuning procedure improves agreement between the simulated ND energy spectrum and the data, but does not significantly affect the predicted FD energy spectrum. Uncertainties on the modeling of the beam have a negligible effect on the predicted FD energy spectrum, and are accounted for in the oscillation measurement.

The same event selection criteria are used in both detectors. The FD data selection was determined using simulation and ND data, before the FD data was examined. All FD events passing the k NN selection are shown in Fig. 2, distributed according to the sign of the reconstructed track charge, divided by the momentum. The figure shows good modeling of track charge identification. Events with a negatively charged track are minimally affected by oscillation due to their higher mean energy, and are removed from further analysis.

The systematic uncertainty on the oscillation parameters is much smaller than the statistical uncertainty. The sources of systematic uncertainty are very similar to those discussed for the MINOS ν_μ analysis [3]. An additional uncertainty is estimated on the level of ν_μ

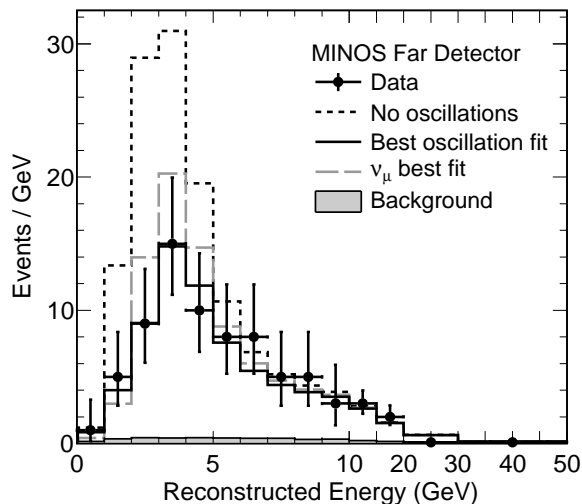


FIG. 3: Comparison of the measured Far Detector $\bar{\nu}_\mu$ CC energy spectrum to the expectation in three cases: in the absence of oscillation, using the oscillation parameters which best fit this $\bar{\nu}_\mu$ data (for this case, the total expected background is also indicated), and using the best-fit ν_μ oscillation parameters measured by MINOS [3].

CC background in the selected $\bar{\nu}_\mu$ CC event sample; below 6 GeV, the purity of the selected $\bar{\nu}_\mu$ CC sample is known to within 1%. To evaluate this uncertainty, the simulated background is scaled until the total number of simulated and data events match in the background-enhanced set of events which fail the k NN selection criterion. This scale factor is taken as the uncertainty on the level of background in the selected $\bar{\nu}_\mu$ CC sample. The total systematic uncertainty on the measurement of $|\Delta\bar{m}^2|$ is $+0.063 - 0.060 \times 10^{-3} \text{ eV}^2$; on the measurement of $\sin^2(2\bar{\theta})$ the total systematic uncertainty is ± 0.012 .

Using the prediction obtained from the ND data, 156 selected $\bar{\nu}_\mu$ CC events with energy below 50 GeV are expected in the FD in the absence of oscillation while 97 events are observed. The energy spectra of these FD events are shown in Fig. 3. A clear energy dependent deficit is observed, showing the first conclusive evidence for $\bar{\nu}_\mu$ disappearance consistent with oscillation in a $\bar{\nu}_\mu$ -tagged sample. The no-oscillation hypothesis is disfavored at 6.3 standard deviations.

Oscillation is incorporated into the predicted energy spectrum according to Eq. 1. Comparing the prediction to the data using a binned log likelihood, oscillation parameters are found which maximize the likelihood. These are $|\Delta\bar{m}^2| = [3.36^{+0.46}_{-0.40}(\text{stat}) \pm 0.06(\text{syst})] \times 10^{-3} \text{ eV}^2$ and $\sin^2(2\bar{\theta}) = 0.86^{+0.11}_{-0.12}(\text{stat}) \pm 0.01(\text{syst})$, and are consistent with all other previous direct limits [16–18]. The prediction for oscillation with these best fit values is shown in Fig. 3, and includes 2 NC events, 5 ν_μ CC events and 0.3

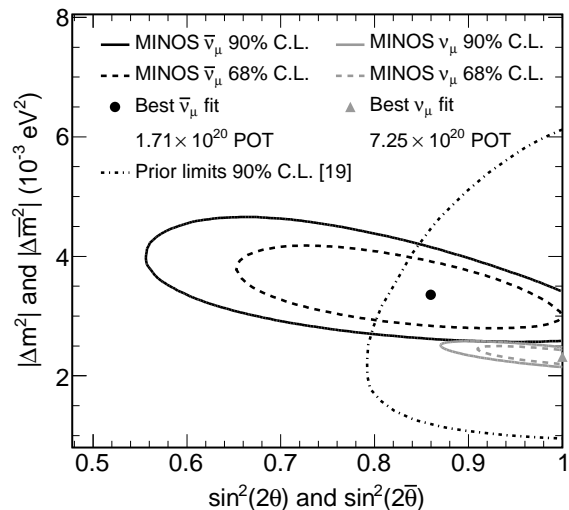


FIG. 4: Allowed regions for the $\bar{\nu}_\mu$ oscillation parameters from a fit to the data in Fig. 3, including all sources of systematic uncertainty. Indirect limits prior to this work [19] and the MINOS allowed region for ν_μ oscillation [3] are also shown.

$\bar{\nu}_\tau$ CC events.

The confidence limits on the oscillation parameters, shown in Fig. 4, are calculated using the Feldman-Cousins technique [26], in which the effect of all sources of systematic uncertainty is included [27, 28]. Figure 4 compares these limits to the previous best limit [19].

MINOS has measured the ν_μ oscillation parameters to obtain a best fit of $|\Delta m^2| = 2.32 \times 10^{-3} \text{ eV}^2$, $\sin^2(2\theta) = 1.0$ [3]. Assuming that muon antineutrinos oscillate with these parameters, 110 selected events are expected in the FD below 50 GeV. This expected energy spectrum is shown in Fig. 3, denoted as “ ν_μ best fit”.

Figure 4 compares the MINOS measurements of the ν_μ and $\bar{\nu}_\mu$ oscillation parameters. In both measurements the purity of the event samples in the oscillation region is high. Below 6 GeV, there is no more than 3% ν_μ CC contamination in the $\bar{\nu}_\mu$ CC sample and vice-versa. Therefore the measurements of the ν_μ and $\bar{\nu}_\mu$ oscillation parameters are nearly independent. Since the $\bar{\nu}_\mu$ measurement is heavily statistically limited, the impact of correlated systematic uncertainties is negligible.

In a joint fit to the data used in the MINOS ν_μ and $\bar{\nu}_\mu$ measurements, assuming identical ν_μ and $\bar{\nu}_\mu$ oscillation parameters, the best fit parameters are $|\Delta\bar{m}^2| \equiv |\Delta m^2| = 2.41 \times 10^{-3} \text{ eV}^2$, $\sin^2(2\bar{\theta}) \equiv \sin^2(2\theta) = 0.97$. The significance of the difference in likelihood between this best fit and the fits to the individual ν_μ and $\bar{\nu}_\mu$ data sets is evaluated using a Feldman-Cousins approach [27]. Ten thousand simulated experiments are generated assuming the joint best fit oscillation parameters above, and include all sources of systematic uncertainty. The

difference in likelihood between the joint and individual ν_μ and $\bar{\nu}_\mu$ fits is recorded for each experiment, and the fraction of simulated experiments with a difference in likelihood larger than that observed in the data is a measure of the significance of the observed difference. Assuming identical ν_μ and $\bar{\nu}_\mu$ oscillation parameters, the probability that the MINOS measurements of the ν_μ and $\bar{\nu}_\mu$ parameters would be more discrepant than those observed is 2.0%.

A thorough search for sources of mismodeling that could provide a difference between the ν_μ and $\bar{\nu}_\mu$ measurements was performed. The only change between ν_μ and $\bar{\nu}_\mu$ running modes was the reversal of the directions of the current in the focusing horns of the beam and of the magnetic fields in the detectors. Very similar data analysis procedures are used in both modes, with the same reconstruction code and similar selection criteria used to obtain the event samples, and the same technique used to obtain the FD predictions. These similarities make the comparison of ν_μ and $\bar{\nu}_\mu$ measurements robust and limit the possible sources which could generate a spurious difference.

The ν_μ and $\bar{\nu}_\mu$ analyses differ in that the $\bar{\nu}_\mu$ -enhanced beam contains a significant ν_μ component (which is effectively removed by the selection cuts). Figure 1 shows that this component is at high energy, away from the oscillation signal region, and therefore any residual contamination has little effect on the oscillation measurement. Figures 1 and 2 show the ν_μ CC component to be well modeled in both detectors in both shape and normalization. All FD events were scanned by eye to ensure the selection does not anomalously mis-classify events by the sign of the charge. Performing the analysis without any selection on track charge in the FD produces consistent results. A scan by eye of events in the ND showed the track reconstruction efficiency to be well modeled.

Differences in the underlying inelasticity distributions for ν_μ and $\bar{\nu}_\mu$ events lead to differences in the muon and hadron energy distributions for the two samples. Studies to validate the reconstruction of muon tracks and hadronic showers included the tightening of reconstruction quality criteria, investigation of the comparative performance of various detector regions, and the use of an alternative hadronic energy estimator. These studies show the detectors to be well modeled, and that any mismodeling in reconstruction and selection efficiencies is accounted for in the systematic uncertainty. In conclusion, no evidence is found for any systematic error that could cause a significant difference between the measured ν_μ and $\bar{\nu}_\mu$ oscillation parameters.

In summary, MINOS has used a beam optimized for the production of $\bar{\nu}_\mu$ to make the first direct observation of $\bar{\nu}_\mu$ disappearance and, assuming the disappearance is caused by oscillation, has made the most precise measurement of the corresponding antineutrino mass-squared difference to date. From fits to these data,

MINOS has measured the oscillation parameters to be $|\Delta\bar{m}^2| = [3.36_{-0.40}^{+0.46}(\text{stat}) \pm 0.06(\text{syst})] \times 10^{-3} \text{ eV}^2$ and $\sin^2(2\bar{\theta}) = 0.86_{-0.12}^{+0.11}(\text{stat}) \pm 0.01(\text{syst})$. The MINOS ν_μ and $\bar{\nu}_\mu$ measurements are consistent at the 2.0% confidence level, assuming identical underlying oscillation parameters. Additional data are currently being taken with the $\bar{\nu}_\mu$ -enhanced NuMI beam, with the aim of doubling the statistics presented in this Letter.

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