Strategy and Enhanced Temperature Determination in a Laser Heated Diamond Anvil Cell

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Strategy and Enhanced Temperature Determination in a Laser Heated Diamond Anvil Cell

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We show that a strategy for increased accuracy in temperature determination by optical pyrometry when the wavelength dependence of the emissivity is unknown is to measure the spectral irradiance at short wavelengths. We then introduce an improved method of determining the temperature in laser heated diamond anvil cells. In general a blackbody source is used to determine the optical transfer function required for determining the blackbody curve. By using the thermal radiation of a heated absorber at ambient pressure and known temperature, uncertainties in the temperature determination caused by the wavelength dependence of the emissivity of the heated absorber can be eliminated. Temperature determination reduces to a one-parameter fit to the blackbody curve rather than the usual two parameters (emissivity and temperature), leading to increased precision and accuracy.

I.   Introduction

Laser heating in diamond anvil cells (DACs) is an important technique that allows the

development of high temperature conditions at static high pressure and has been widely used in

many disciplines [1]. In a laser heated diamond anvil cell (LHDAC) pressures of the order of

100 GPa and temperatures of several thousand Kelvin can be achieved. In condensed matter

physics, chemistry, material science, and earth and planetary sciences, the LHDAC enables

mapping of P-V-T phase diagrams, discovery and study of high P-T phases, melting lines, and

studying the electronic, magnetic, and structural properties of materials at elevated temperatures

and pressures [2, 3]. In earth and planetary sciences studies under such conditions are crucial in

understanding the interior of planets [4].

Pressure and temperature are the two most important parameters to be determined in

LHDAC experiments. Advances in the LHDAC technology have continued, e.g., [5-9], since its

inception [10]; still the complexity of these measurements can lead to significant uncertainty in

determining pressure and temperature. The most commonly used method for determining the

temperature of a sample in an LHDAC is spectral optical pyrometry [11]. In this paper we

consider the strategy for optimally determining temperature and a present a technique that can

improve the accuracy and precision in temperature determination. The advantage of this

technique is demonstrated by experimental measurements using platinum to absorb the laser

power.

II.   Temperature Measurement in the LHDAC: Theory

Optical pyrometry in an LHDAC allows non-contact, remote temperature determination

of a material. The laser beam is focused on a sample or an absorber that heats to a local

thermodynamic equilibrium temperature described by the Planck radiation law and it is the temperature of the absorber that is determined. For temperature measurement by optical pyrometry the thermal irradiance from the absorber is collected as a function of wavelength; temperature is determined by fitting to the Planck thermal radiation function

$$I(\lambda,T)\Delta\lambda = \frac{2hc^2}{\lambda^5} \cdot \frac{\varepsilon(\lambda,T)}{\exp(hc/\lambda kT)-1}\Delta\lambda \equiv \varepsilon(\lambda,T)I_{\lambda,T}^{bb}\Delta\lambda \,. \tag{1}$$

Here, $I(\lambda,T)$ is the spectral irradiance, λ the wavelength, T the temperature, $\varepsilon(\lambda,T)$ the emissivity, h Planck's constant, c the speed of light, and k the Boltzmann constant. The emissivity of a blackbody is 1, while an absorber is at best a graybody with wavelength independent emissivity less than 1. In reality the emissivity usually is both wavelength and temperature dependent. In order to accurately determine the temperature, the BB lineshape, which is usually distorted by the measurement instruments, must be determined and the emissivity of the absorber must be known as a function of wavelength and temperature. It is sufficient to measure the irradiance in a limited spectral region and fit to the BB curve in that region. If the temperature is not uniform in space and time (for example in pulsed laser heating), then appropriate corrections must be made [12]. For purposes of discussion we introduce the notation $I_{\lambda,T}^{bb} \equiv BB(\lambda,T)$ for a blackbody emitter and $GB \equiv \varepsilon I_{\lambda,T}^{bb}$, with $\varepsilon =$ constant for a graybody emitter.

III.   Strategies for Determining the Temperature

Ideally to determine the temperature by pyrometric methods one would like to measure the irradiance over a broad spectral range, but this is impractical and unnecessary. In some instruments, spectral measurements are made at only one or two wavelengths and in principle, accurate temperatures can be determined, although measuring at several wavelengths should

increase the accuracy of the measurement. One of the most egregious problems is the lack of knowledge of the wavelength and temperature dependence of the emissivity (in this section we concentrate the discussion on the wavelength dependence). When knowledge of the wavelength dependence of the emissivity is lacking, temperatures in an LHDAC are usually determined by fitting the irradiance to a GB curve. This can lead to serious errors in the accuracy, as we shall demonstrate.

In Fig. 1 we multiply the blackbody curve for T=1000 K by the experimental emissivity of platinum to show how wavelength dependent emissivity can affect the BB curve. One sees that the peak of the platinum curve is shifted to shorter wavelength. Both curves look like BB curves and if Wien's Law ($\lambda_{max}T$ = constant) is used to determine the temperature for the platinum curve, T=1160 K is found, rather than the true temperature of 1000 K (Note that Wien's constant is independent of the absolute value of the emissivity if the emitter is a graybody). Alternately, if the wavelength dependence of the emissivity is unknown and the irradiance is fit to a GB curve, shown in Fig. 1, one finds a serious error in the temperature, with $T = 1184 \pm 0.5 \,\mathrm{K}$ and $\varepsilon = 0.07 \pm 0.000$, resulting in an inaccuracy of 184 K or 18%. For this fit we used 6000 points in the wavelength range 0.5-6.5 micron with no noise added to the irradiance values.

One strategy for improving the accuracy is to select the wavelength region for the fit. In an LHDAC one is interested in the fitted value of T, whereas the emissivity (or emittance) is less significant, and does not represent a reliable measurement value. Because of the nature of the BB curve, exponential in T for short wavelengths and linear in T for long wavelengths, we expect the impact of the wavelength dependence of the emissivity on the accuracy of the temperature determination to be much less if irradiance is measured and fitting is done in the

exponential part of the curve. In Table I we show the results for fitting in several different

wavelength regions using a graybody approximation when the emissivity is actually wavelength

dependent, confirming our conjecture.

To quantify this we have defined a parameter Λ that represents the normalized difference

between a graybody curve (fitting curve) and a non graybody emitter curve, with

$\varepsilon_{NGB}(\lambda) = 0.33235 - 0.047064\lambda$ [13] and T=1000, in a given wavelength interval (λ, $\lambda+\Delta\lambda$):

$$\Lambda(\varepsilon,T) = \sum_{\lambda}^{\lambda+\Delta\lambda} \frac{[\varepsilon_{NGB}(\lambda)BB_{T=1000K} - GB(\varepsilon,T)]^2}{[\varepsilon_{NGB}(\lambda)BB_{T=1000K} + GB(\varepsilon,T)]^2} . \tag{2}$$

The best fit value(s) of ε, T for the GB curve minimizes Λ. In Fig. 2 we show the results for Λ as

a function of T and ε. Fitting in the short wavelength region a global minimum is found (not

visible in the figure) and there is a relatively narrow range of values for T. Fitting only to the

longer wavelength region, the global minimum is very shallow demonstrating the possibility of a

large inaccuracy in determining T, in particular if noise is added to the data points used in the fit.

The situation is even more extreme if the fit is done in the long wavelength region, beyond the

peak.

IV. An Improved Method and Optical Transfer Functions in the LHDAC

For practical reasons, the optimum wavelength region where the irradiance of a non

blackbody emitter is collected for temperature determination cannot always be chosen in the

exponential part of the thermal radiation curve. More specifically at lower temperatures in an

LHDAC ($T \sim 700K$ or lower) there are very few thermally radiated photons at shorter

wavelengths and for improved signal-to-noise and precision, measurements should be made

closer to the BB peak where uncertainties in wavelength dependence of emissivity can give rise

to large errors in temperature. In principle use of an absorber with well-known emissivity would

eliminate this problem, however this would create an experimental limitation in the choice of an

absorber. In this section of the paper we introduce a technique in optical pyrometry that removes the uncertainties in temperature determination due to the lack of knowledge of the wavelength dependence of the emissivity without direct measurement of the wavelength dependence of emissivity. This technique can be used for any material that is chosen as the absorber and thermal emitter in an LHDAC.

In general, for a BB source, the optical response of a system, including detector, spectrometer, filters, etc, is wavelength dependent so that the measured irradiance is distorted from the BB curve and must be corrected. The correction can be made by determining the response using a calibrated source of radiation such as a BB source at a known temperature. This response is usually characterized by the optical transfer function, TF_λ^{bb}. In principle, the transfer function is independent of the temperature of the BB source and is defined as

$$TF_\lambda^{bb} = \frac{I_{\lambda,T}^{bb}}{S_{\lambda,T}^{bb}},$$ (3)

where $I_{\lambda,T}^{bb}$ is the theoretical (calculated) Planck BB irradiance at temperature T and wavelength λ, and $S_{\lambda,T}^{bb}$ is the signal of the BB source collected by the optical system at temperature T and wavelength λ. There is always a finite spectral width or resolution, $\delta\lambda$, over which the signal is measured. The transfer function is independent of the temperature only if $\delta\lambda$ is small enough so that the optical response of the system is not a rapidly varying function over the resolution width and the average signal over $\delta\lambda$ is a good approximation to the signal at λ.

The spectral irradiance of the absorber at any other unknown temperature T_x can be determined from the following relation,

$$I_{\lambda,T_x}^{absorber} = TF_\lambda^{bb} \times S_{\lambda,T_x}^{absorber}$$ (4)

which corrects the measured signal for temperature T_x to an undistorted irradiance of the absorber at T_x.

Here, $I_{\lambda,T_x}^{absorber}$ and $S_{\lambda,T_x}^{absorber}$ are the irradiance and the signal of the absorber at λ and T_x, respectively, and

$$I_{\lambda,T_x}^{absorber} = \varepsilon(\lambda,T_x)^{absorber} \times I_{\lambda,T_x}^{bb}. \tag{5}$$

The unknown temperature, T_x, is determined by fitting the result of Eq. (4) to a Planckian spectrum. Since most absorbers are not blackbodies the emissivity of the absorber, $\varepsilon(\lambda,T)$, which includes its temperature and wavelength dependence should be determined to achieve high accuracy. However, the wavelength dependence of the emissivity for most materials is not known, and as mentioned earlier, in most cases emissivity is assumed to be independent of wavelength and its value is determined using a two-parameter (ε,T_x) fit to the Planck function. This uncertainty in the wavelength dependence of the emissivity can lead to serious errors in the accuracy of the temperature, substantially larger than 10%, while a two parameter fit leads to lower precision than fitting to a single parameter.

Here we introduce a method in which the emissivity of the sample is absorbed into the optical transfer function. We show that the unknown wavelength dependence of the emissivity will be removed by such a method and a more precise determination of the temperature is made using a one-parameter (T) fit to the Planck blackbody radiation function.

Define the optical transfer function which includes the emissivity of the absorbing material, $TF_{\lambda}^{absorber}$, as follows:

$$TF_{\lambda}^{absorber} = \frac{I_{\lambda,T}^{bb}}{S_{\lambda,T}^{absorber}}; \tag{6}$$

then

$$TF_\lambda^{bb} = \varepsilon(\lambda)^{absorber} \times TF_\lambda^{absorber} \ . \tag{7}$$

From Eqs. 3-7, if we heat the absorber to an unknown temperature, T_x, the following relation

will be true because the emissivity term that appears in $TF_\lambda^{absorber}$ will be cancelled by the

emissivity term in the numerator of $S_{\lambda,T_x}^{absorber}$,

$$I_{\lambda,T_x}^{absorber} = TF_\lambda^{absorber} \times S_{\lambda,T_x}^{absorber} = BB(\lambda,T) \ . \tag{8}$$

Thus, the wavelength dependence of the emissivity is eliminated without knowledge of the

absolute value of the emissivity of the absorber, without using a blackbody source. T_x can be

determined by fitting to the Planck blackbody radiation function, $BB(\lambda,T)$, with a single fit

parameter.

Experimentally $TF_\lambda^{absorber}$ can be measured by using a sample that is identical to the

absorber used in the LHDAC and heating it at ambient pressure to a known temperature T.

However, here the temperature or pressure dependence of the emissivity is not taken into

account. As long as the temperature or pressure dependence of the emissivity is weakly varying,

$TF_\lambda^{absorber}$ gives a good first order approximation to the true value and provides a much more

accurate temperature determination than found using a graybody fit. If the temperature

dependence of the transfer function is known in the temperature interval of interest, the simplest

approach to determine the temperature would be to normalize the Planck blackbody function by

dividing it by $TF^{absorber}(\lambda,T)$, and determine the temperature of the absorber at any other

unknown temperature by simply fitting the $S_{\lambda,T_x}^{absorber}$ to the normalized Planck function. We

mention here that since the radiation from the absorber passes through the pressurization medium

and one diamond in a DAC, a correction must be made for these effects.

V. Temperature Measurement in the LHDAC: Experiment

Here we demonstrate how absorbing the emissivity into the transfer function can improve the accuracy of the temperature measurement. Figure 3 shows the schematic layout of our optical system. We measure in the near IR at several discrete wavelengths [14] in the wavelength range between 1.8-3.1μm, using a series of 5 narrow band filters to determine the wavelength dependence of the irradiance of the sample (optical spectrometers and CCDs can be used for measuring in the visible). Thermal radiation from a platinum foil, embedded inside a homemade oven, is collected by a CaF_2 lens with 1:1 magnification, focused into a 25 micron diameter pinhole which spatially filters the light. This light is then collected by two CaF_2 lenses, and focused onto a liquid nitrogen cooled InSb detector. The temperature of the platinum is measured with an R type thermocouple that is attached to the surface of the platinum, and for this demonstration the temperature is increased in increments of ~100K between 625-1150K. The transfer function, $TF_{\lambda,T}^{absorber}$ (shown in Fig. 4a, inset) was determined using Eq. 6, where $I_{\lambda,T}^{bb}$ was evaluated at temperature T, measured by the thermocouple. The signal from the platinum, $S_{\lambda,T}^{Pt}$, was measured with the system in Fig. 3. We also measured $TF_{\lambda,T}^{bb}$ by replacing the Pt source with a homemade BB source with $\varepsilon \geq 0.99$. The temperature of the BB source was measured with an R type thermocouple with its tip imbedded inside the BB cavity. $TF_{\lambda,T}^{bb}$ was determined by calculating $I_{\lambda,T}^{bb}$ at a temperature determined by the thermocouple, and $S_{\lambda,T}^{bb}$ was the signal detected by the InSb detector.

To demonstrate the advantage of eliminating the emissivity, we determined the temperature of a Pt foil by two methods and compared the results to the temperature of the

sample, measured independently with a thermocouple. We calculated both $TF_{\lambda,T}^{absorber}$ for a Pt

absorber and $TF_{\lambda,T}^{bb}$. The temperature of the Pt absorber was then determined for five

temperatures by using

a) Emissivity eliminated method with a one parameter fit (T).

b) Emissivity eliminated method with two fitting parameters (T and $\varepsilon = const$; this assumes

that the absolute value of the emissivity is not known).

c) Conventional correction of the signal by $TF_{\lambda,T}^{bb}$ and assuming graybody behavior.

The results are summarized in Table II and some of the fits are shown in Fig. 4 a, b. T_{TC}

is the temperature of the absorber measured directly by thermocouple. T_{Pt-1P} is the temperature

of the sample determined by using the one-parameter fit to Planck blackbody function and the

signal of the sample was corrected for spectral distortion by $TF_{\lambda}^{absorber}$. T_{Pt-2P} and ε_{Pt-2P} are the

temperature and scaling factors of the Pt determined by the two-parameter fit to the Planck

graybody function. Here the signal of the sample was also corrected by $TF_{\lambda}^{absorber}$. T_{bb-2P} and

ε_{bb-2P} are the temperature and emissivity of the platinum foil determined by using a two-

parameter fit to the Planck graybody function in which the signal of the platinum was corrected

by multiplying by TF_{λ}^{bb}. Note that in Fig. 4 a and b the precision of the points fit to the curves

for both cases is excellent, but there is a serious error in the accuracy in Fig. 4b. Fig. 5

summarizes important results by plotting the fitted temperatures against the temperature

measured with a thermocouple.

We used the fitting routine of "Igor Pro 5.0" for data analysis. In curve fitting, Igor uses

raw data and a function with unknown coefficients and chooses the coefficients such that the

function matches the raw data to minimize the value of Chi-square ($\Sigma(y - y_i)^2 / \sigma_i^2$) where y is a

fitted value for a given point, y_i is the measured data value for the point and σ_i is the standard deviation for y_i. The errors in $I_{\lambda,T_x}^{absorber}$ for any given temperature and wavelength were the combination of the statistical errors in $S_{\lambda,T_x}^{absorber}$ and the errors in the determination of the transfer function. The errors in the transfer functions were estimated by the variation of the transfer function for different temperatures and were the dominant source of error for all temperatures. Igor automatically calculates the estimated error (standard deviation) for each of the coefficients in a curve fit. The T_{Pt-1P} agree with T_{TC} to within the uncertainties. The graybody assumption (T_{bb-2P}) leads to a significant overestimation of the temperature of the sample. An interesting point is that even when the temperature dependence of the emissivity is taken into account by using $TF_{\lambda}^{absorber}$, the two-parameter fit (T_{Pt-2P}, A_{Pt-2P}) has significantly lower accuracy in the temperature.

In Fig. 6, we simulate the one and two-parameter fits by adding random noise to calculated blackbody irradiances at 939 K and 797 K (two of the thermocouple temperatures). Here the one-parameter fit ($\varepsilon = 1$) results in temperature values that are in reasonable agreement with the temperature for the curve without noise, whereas in the two-parameter fit, the fitting function can adjust both the amplitude and temperature to generate a fit that is closer to all data points. Note that in this example the lower temperature data points have a higher two-parameter fit temperature than the higher temperature data points.

VI   Summary and Conclusion

If the emissivity of a radiant emitter is unknown in optical pyrometry, greater accuracy can be achieved by fitting to a graybody curve in the short wavelength exponential region of the Planck irradiance curve. Not accounting for the wavelength and temperature dependence of the

emissivity can lead to serious errors in the temperature determination. Lacking knowledge of the emissivity of a material used for temperature measurement, it can be absorbed into the optical transfer function of the system by a modified spectral calibration method. This method can be useful for applications such as remote temperature determination in an LHDAC where the wavelength dependence of the absorbing material may not be known.

Acknowledgement

References

[1]   N. Shekar, P. Sahu, and K. Rajan, J. of Mat. Sci. and Tech. **19**, 518 (2003).

[2]   N. Subramanian, N. Shaker, N. Kumar, and P. Sahu, Current Sci. **91** (2006).

[3]   S. Meenakshi, V. Vijayakumar, and B. Godwal, Ind. Journ. of Pure and Appl. Phys. **44**, 440 (2006).

[4]   R. Boehler, Rev. Geophys. **38**, 221 (2000).

[5]   K. K. T. Walter M. J., Physics of the Earth and Planetary Interiors **143-144**, 541 (2004).

[6]   Y. Meng, G. Shen, and H. Mao, J. Phys. Cond. Matter. **18**, 1097 (2006).

[7]   S. Deemyad, E. Sterer, C. Barthel, S. Rekhi, J. Tempere, and I. F. Silvera, Rev. Sci. Instruments **76**, 125104 (2005).

[8]   J. Lin, W. Sturhahn, J. Zhao, G. Shen, H.-K. Mao, and R. J. Hemley, Geophys. Res. Lett. **31**, L14611 (2004).

[9]   G. Shen, H. K. Mao, and R. J. Hemley, Geophysical Res. Letters **25**, 373 (1998).

[10]   L. Ming, and W. A. Bassett, Rev. Sci. Inst. **45**, 1115 (1974).

[11]   A. P. Jephcoat, and S. P. Besedin, Phil. Trans. R. Soc. Lond. A **354**, 1333 (1996).

[12]   S. Rekhi, J. Tempere, and I. F. Silvera, Rev. Sci. Inst. **74**, 3820 (2003).

[13]   We approximate the emissivity with a linear function. In the long wavelength limit (Hagen-Rubens limit) the emissivity decreases as the square root of the frequency of light.

[14]   P. Shuker, A. Melchior, Y. Assor, D. Belker, and E. Sterer, Rev. Sci. Inst. **79**, 073908 (2008).

[15]   L. S. Dubrovinsky, and S. K. Saxena, High-temperature High-Pressure **31**, 393 (1999).

[16]   S. Deemyad, and I. F. Silvera, Rev. Sci. Inst. **79**, 086105 (2008).

Table I. The best graybody (ε=*const.*) fit values to a non-blackbody irradiance at T=1000 K calculated at several 0.5 µm intervals between 0.5-5 µm. The irradiance was calculated with ε = 0.33- 0.05λ and these curves were fit with the graybody approximation.

Wavelength range	T_{GB-2P} (K)	% error in T	ε_{GB-2P}
0.5-1µm	1010	1	0.25
1-1.5µm	1022	2.2	0.21
1.5-2µm	1043	4.3	0.18
2.5-3µm	1079	7.9	0.14
3-3.5µm	1142	11.4	0.11
3.5-4µm	1252	12.5	0.07
4-4.5µm	Non convergent		--------
4.5-5µm	Non convergent		--------

Table II

Measured and calculated temperatures of the Pt source. T_{TC} is the temperature of the Pt source measured by a thermocouple. T_{Pt_1P} is the temperature of the Pt calculated by the emissivity eliminated method with a one parameter fit (T). T_{Pt_2P} and A_{Pt-2P} are the temperature and scaling coefficients calculated by the emissivity eliminated method with two fitting parameters, and T_{bb_2P} and ε_{bb-2P} are the temperature and the emissivity of the Pt calculated by the conventional correction of the signal by $TF_{\lambda,T}^{bb}$, assuming graybody behavior. All temperatures are in degrees Kelvin.

T_{TC}	T_{Pt_1P}	T_{Pt_2P}	A_{Pt-2P}	T_{bb_2P}	ε_{bb-2P}
625±10	623±2.8	643±22	0.78±0.2	736±29	0.04±0.01
739±10	734±2.4	749±13	0.84±0.1	878±18	0.043±0.01
797±10	807±2.7	814±15	0.93±0.1	967±21	0.048±0.01
939±10	939±3.6	942±19	0.98±0.1	1154±29	0.05±0.01
1131±10	1130±5.1	1101±26	1.15±0.2	1408±44	0.06±0.01

Figure Captions

Figure 1. Irradiance of Pt (solid curve) and a blackbody source (dashed dot curve) at 1000 K

calculated using the emissivity of platinum (dotted curve) [15, 16]. The blackbody

irradiance is scaled down by 0.16 in the graph. The dashed line is a two-parameter fit,

assuming graybody behavior for the Pt.

Figure 2. Determination of the temperature for fitting to a GB in two different spectral regions

using the emissivity function given in Table I.

Figure 3. Schematic drawing of the optical configuration for measuring temperature of an

absorber and a blackbody in the infrared.

Figure 4. Corrected Pt thermal spectra: a) correction of the emissivity using Pt for the transfer

function (inset graph is $TF_{\lambda,T}^{absorber}$ and $TF_{\lambda,T}^{bb}$ of the optical system as a function of

wavelength); b) Same, without emissivity correction, using a BB source for the transfer

function. Thermocouple temperatures for different curves are shown for both a and b.

Fit temperatures are tabulated in Table 1.

Fig. 5   Temperature of Pt determined by different methods listed in Table I as a function of

temperature of Pt measured directly by a thermocouple. The dash-dot line represents

the temperature equal to the thermocouple temperature. The 1-parameter fit has a slope

close to 1.

Fig. 6.   Data generated by adding random noise to blackbody irradiance at T=939 K and T=797

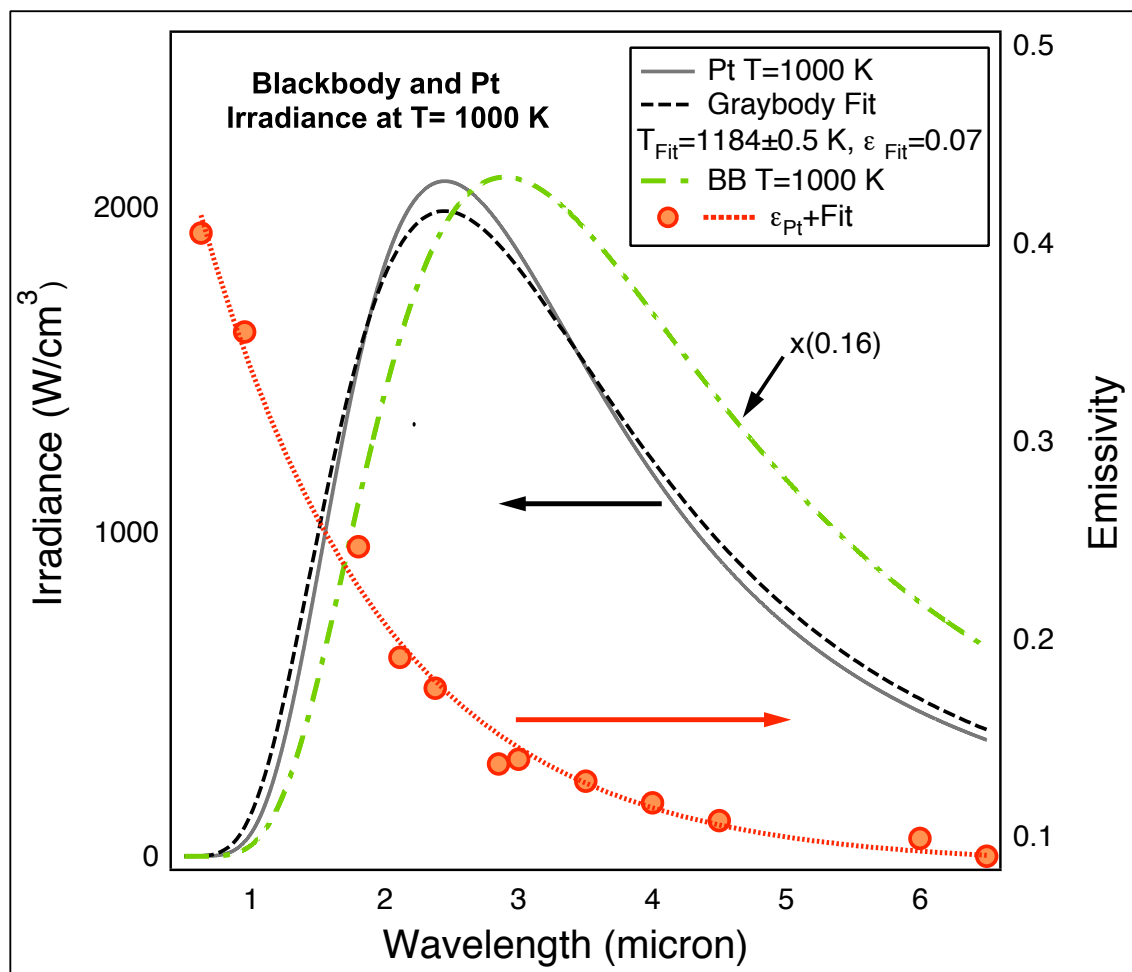K. Solid curves are one parameter fits to data points and dashed curves are two-
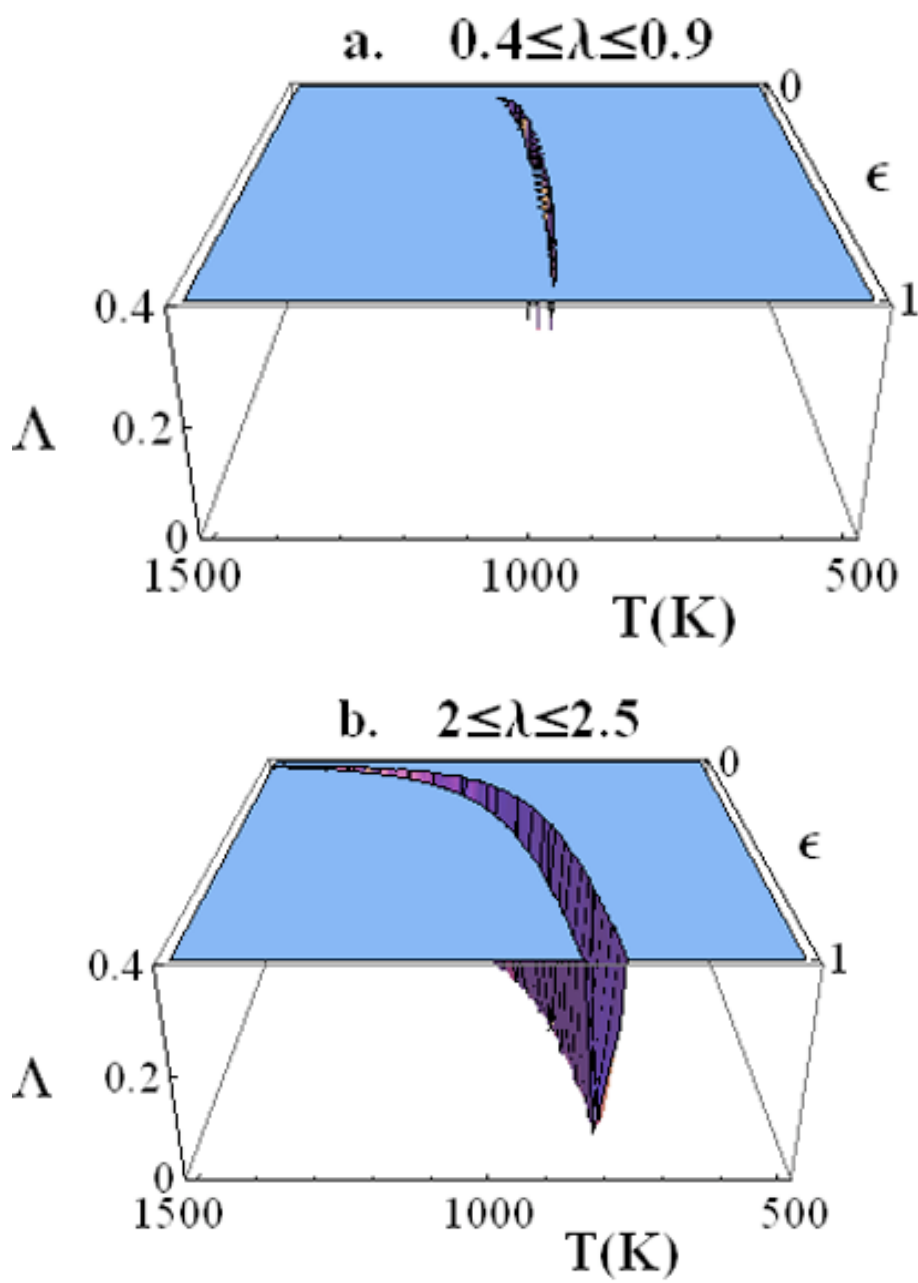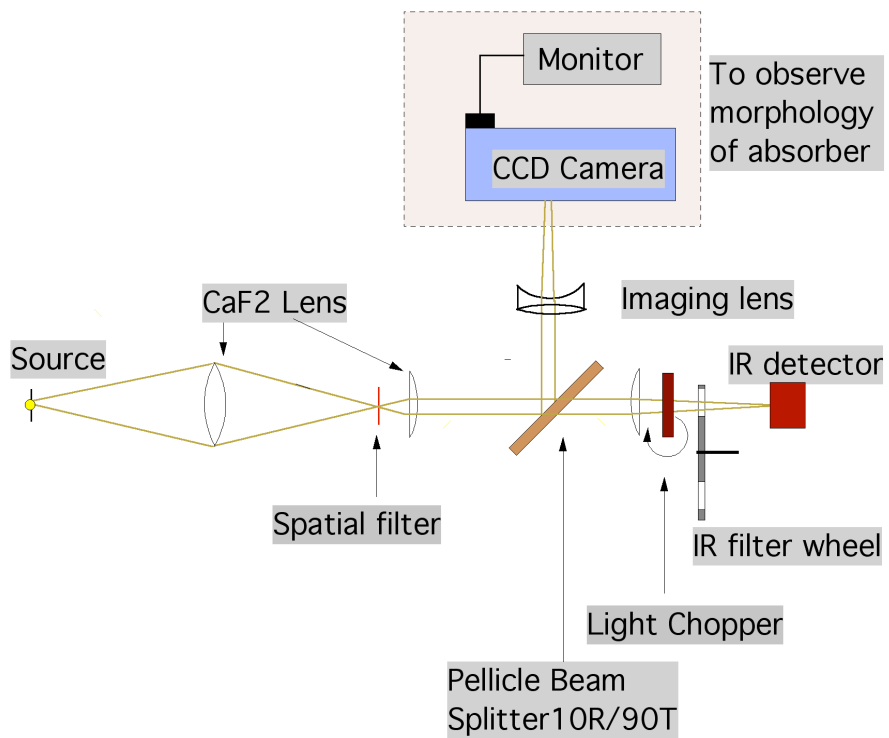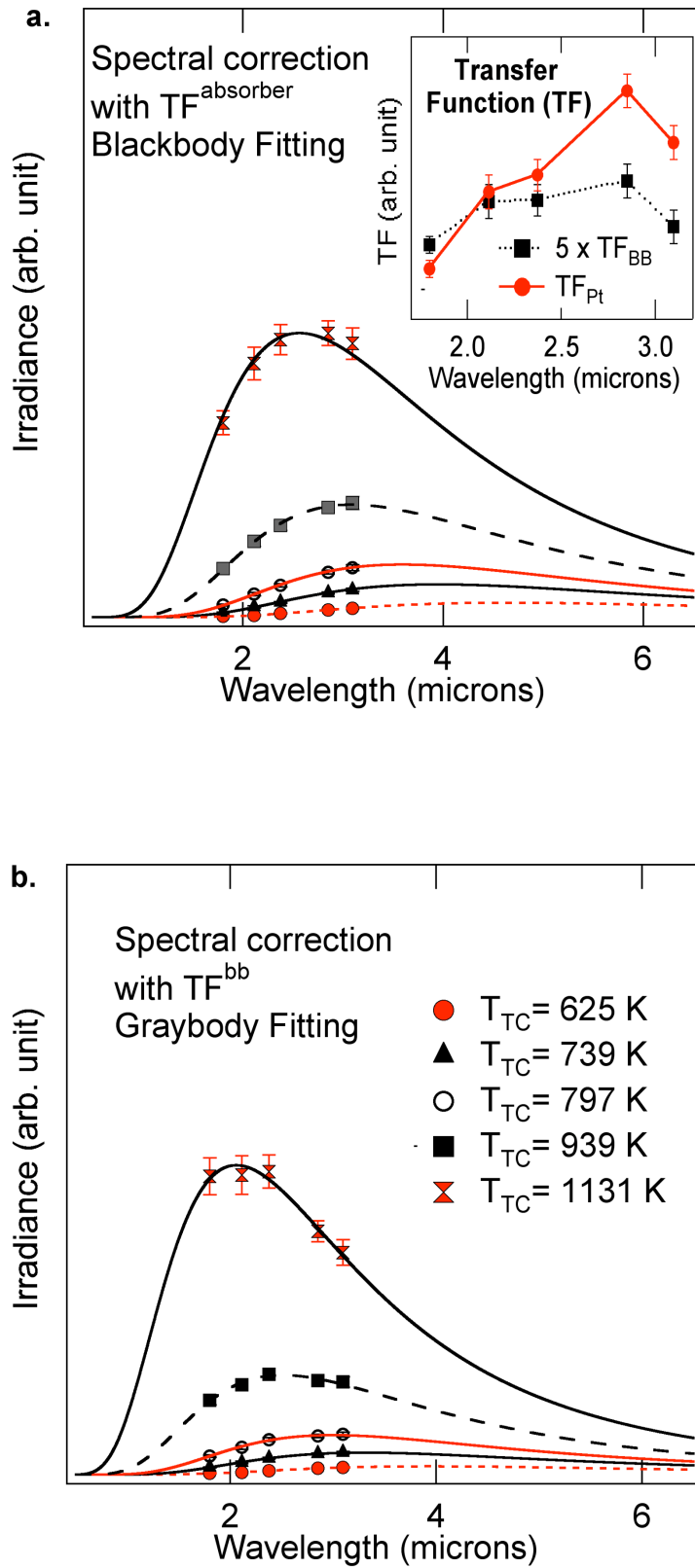
parameter fits.

Figure 1.

Figure. 2.

Monitor

To observe
morphology
of absorber

CCD Camera

CaF2 Lens

Imaging lens

Source

IR detector

Spatial filter

IR filter wheel

Light Chopper

Pellicle Beam
Splitter10R/90T

Figure 3.

a. Spectral correction with TF^{absorber} Blackbody Fitting

Inset: **Transfer Function (TF)**
- 5 x TF$_{BB}$
- TF$_{Pt}$

b. Spectral correction with TF^{bb} Graybody Fitting

- T_{TC} = 625 K
- T_{TC} = 739 K
- T_{TC} = 797 K
- T_{TC} = 939 K
- T_{TC} = 1131 K

Figure 4.

Figure 5.

Figure 6