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Fracture of electrodes in lithium-ion batteries caused by fast charging

Kejie Zhao, Matt Pharr, Joost J. Vlassak, and Zhigang Suo^{a)}

School of Engineering and Applied Sciences and Kavli Institute, Harvard University, Cambridge, Massachusetts 02138, USA

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During charging or discharging of a lithium-ion battery, lithium is extracted from one electrode and inserted into the other. This extraction-insertion reaction causes the electrodes to deform. An electrode is often composed of small active particles in a matrix. If the battery is charged at a rate faster than lithium can homogenize in an active particle by diffusion, the inhomogeneous distribution of lithium results in stresses that may cause the particle to fracture. The distributions of lithium and stress in a LiCoO_2 particle are calculated. The energy release rates are then calculated for the particle containing preexisting cracks. These calculations predict the critical rate of charging and size of the particle, below which fracture is averted. © 2010 American Institute of Physics. [doi:10.1063/1.3492617]

I. INTRODUCTION

Batteries are a key to the commercialization of clean and secure energy.^{1,2} Essential roles of batteries include leveling loads on power grids and storing energy from renewable sources. Furthermore, batteries are ubiquitous in all forms of electronics and transportation. For applications sensitive to weight and size, such as portable electronics and electric cars, the technology of choice is lithium-ion batteries.³

A lithium-ion battery contains an electrolyte and two electrodes. Each electrode is an atomic framework that hosts mobile lithium. During charging or discharging of the battery, lithium ions are extracted from one electrode, migrate through the electrolyte, and are then inserted into the other electrode. Meanwhile electrons flow from one electrode to the other through an external metallic wire. Extraction or insertion of lithium induces stresses in the electrodes that may cause fracture⁴ or morphological change.⁵ The loss of structural integrity may reduce electric conductance, causing the capacity of the battery to fade.⁶

Lithiation-induced damage is a bottleneck in developing batteries of high energy density. For example, the ability of silicon to absorb a large amount of lithium has motivated intense research^{7,8} but such absorption causes volumetric swelling of $\sim 400\%$, leading to fracture. The mechanical failure has so far prevented silicon from serving as a viable electrode. Fracture has also been observed in commercial electrodes that undergo small deformation, such as LiCoO_2 , LiMn_2O_4 , and LiFePO_4 .^{4,9–13}

Lithiation-induced deformation and stress have been studied in recent years. For example, Christensen and Newman^{14,15} calculated swelling and stress, Sastry and co-workers^{16,17} simulated the stress generation during lithiation under galvanostatic control, Cheng and Verbrugge^{18,19} calculated the strain energy under both potentiostatic and galvanostatic operations in spherical particles. Lithiation-

induced stress in silicon has been calculated.^{20,21} Several recent papers have studied lithiation-induced fracture by applying fracture mechanics.^{22–25}

While a conceptual framework to analyze lithiation-induced deformation, stress, and fracture is emerging, limited work has been published that predicts fracture of practical systems by using actual material data. This paper attempts to predict fracture in a widely used material for cathode, LiCoO_2 . A commercial electrode often takes the form of active particles embedded in a binding matrix (Fig. 1). The distribution of lithium in the particle is inhomogeneous. The gradient of this inhomogeneity is large if the battery is charged at a rate faster than lithium can homogenize in the particle by diffusion. We calculate the distributions of lithium and stress in a LiCoO_2 particle, and then calculate the energy release rates for the particle containing preexisting cracks. These calculations predict the critical rate of charging and size of the particle, below which fracture is averted.

II. THEORY AND SCALING

In a battery, the electrolyte conducts lithium ions but not electrons. When the battery discharges, the difference in the chemical potential of lithium in the two electrodes drives lithium ions to diffuse out of the anode, through the electrolyte, and into the cathode. To keep the electrodes electrically neutral, electrons flow from the anode to the cathode through

FIG. 1. (Color online) A schematic of the microstructure of the cathode. The cathode is composed of active particles, a matrix, and pores containing the electrolyte.

^{a)}Electronic mail: suo@seas.harvard.edu.

FIG. 2. (Color online) (a) When the rate of discharging is high, the distribution of lithium in the active particle is inhomogeneous, which causes a field of stress in the particle. (b) When the rate of discharging is low, the distribution of lithium in the particle is negligible. The arrows indicate the direction of lithium insertion.

the external metallic wire. Both the ionic and the electronic processes are reversed when the battery is charged by an external power source. As illustrated in Fig. 1, an electrode in commercial lithium-ion batteries is usually a composite, consisting of active particles, a compliant matrix composed of polymer binders and additives, and pores filled with the electrolyte.^{13,26} Migration of lithium in the electrolyte is fast, so that diffusion of lithium in the active particles limits the rate of charging and discharging. Because of the porosity of the composite and the compliance of the binder, stress in an active particle is often due primarily to the mismatch created by an inhomogeneous distribution of lithium within the particle.

The degree of the inhomogeneity depends on the competition between the rate of discharging and the rate of diffusion. Denote τ as the time to discharge the battery, D a representative value of diffusivity of lithium in the particle, and L the characteristic size of the particle. These quantities form a dimensionless group:

$$\chi = \frac{L}{\sqrt{D\tau}}. \quad (1)$$

The parameter χ characterizes the relative rate of discharging and diffusion. If χ is large, the battery is discharged at a rate faster than lithium can homogenize in the particle by diffusion. Consequently, lithium is crowded in the outer shell of the particle, causing a large stress in the particle [Fig. 2(a)]. By contrast, if χ is small, the battery is discharged at a rate slow enough for lithium in the particle to maintain nearly a homogeneous distribution. Consequently, lithiation causes the particle to swell or contract but the particle is nearly unstressed [Fig. 2(b)].

Cracklike flaws are assumed to preexist in the active particles.¹³ We ask if the lithiation-induced stress will cause any of the flaws to grow. The elastic energy in the particle reduces when a crack advances. The reduction in the elastic energy in the particle associated with the crack advancing a unit area defines the energy release rate G . Dimensional considerations dictate that the energy release rate should take the form

$$G = ZE\epsilon_m^2 L, \quad (2)$$

where E is Young's modulus of the particle, L a characteristic size of the particle, and ϵ_m a characteristic mismatch strain, defined as

$$\epsilon_m = \frac{l_1 - l_0}{l_0}. \quad (3)$$

Here l_0 and l_1 are the lattice parameters in the initial state and in the fully lithiated state, respectively. At a given time, the distribution of the stress in the particle is determined by solving the diffusion equation, and the dimensionless coefficient Z is determined by solving the elastic boundary-value problem. Once the geometry of the particle and the location of the crack are given, Z can only vary with the length of the crack, the dimensionless parameter χ , and time. We note this functional dependence in a normalized form:

$$Z = f\left(\frac{a}{L}, \chi, \frac{t}{\tau}\right), \quad (4)$$

where a denotes the length of the crack. At a fixed value of χ and a fixed time, if the crack is very short, the elastic energy in the particle does not change appreciably when the crack grows, and the energy release rate is small. Likewise, when the crack is very long, the elastic energy is nearly fully relaxed because the crack introduces larger constraint-free area, and the energy release rate is also small. In between these two limits, the energy release rate reaches the maximum value $G_{\max}$ for a crack of a certain length. Let Γ be the fracture energy of the particle. No preexisting flaws will advance if the maximum energy release rate is below the fracture energy of the particle

$$G_{\max} < \Gamma. \quad (5)$$

To ensure no preexisting flaws will advance, $G_{\max}$ indicates the energy release rate maximized for all configurations of the flaws and for all time. This approach has been used to analyze many systems, such as polycrystals,²⁷ composites,²⁸ and thin films.²⁹

The comparison between the energy release rate and the fracture energy defines another dimensionless parameter

$$\Lambda = \frac{E\epsilon_m^2 L}{\Gamma}. \quad (6)$$

When Λ is small, the elastic energy is insufficient to cause fracture. Therefore, a particle with small stiffness, small size, and large fracture energy is more resistant to fracture. This statement is consistent with recent experimental observation that the electrochemical cycling behavior is significantly improved if the size of active particles are small.^{30,31}

The dimensionless groups χ and Λ characterize the fracture behavior of the active particles. In the case of a highly inhomogeneous distribution of Li ions, to prevent fracture it is necessary to decrease the particle size, decrease the rate of discharging, and/or enhance the fracture energy. This concept is sketched schematically in Fig. 3 in terms of χ and Λ . The red line delineates an upper boundary to the safe regime in which no fracture occurs.

FIG. 3. (Color online) Criteria to avoid fracture of an electrode particle in terms of the nondimensional quantities Λ and χ .

The concentration of lithium in a particle is a time-dependent field governed by the diffusion equation

$$\frac{\partial c}{\partial t} = [D_{ij}c_{,j}]_{,i}, \quad (7)$$

where c denotes the normalized lithium concentration in the host—the actual lithium concentration divided by the concentration of lithium in the fully lithiated state. The diffusivities in the crystal are in general anisotropic and are functions of the concentration, $D_{ij}(c)$. The concentration gradient is the primary driving force for diffusion. The effect of stress on diffusion has been explored in Ref. 16, and is found to be small. In this paper, we will neglect this small effect. Equa-

tion (7), along with suitable initial and boundary conditions, determines the time-dependent concentration field in the particle.

The stress field is calculated by solving the elastic boundary-value problem. Since elastic deformation is much faster than atomic diffusion, mechanical equilibrium is established during lithium insertion. Therefore, the governing equations are the same as those in the theory of elasticity. Specifically, the strains ε_{ij} relate to the displacements u_i by

$$\varepsilon_{ij} = \frac{1}{2}(u_{i,j} + u_{j,i}). \quad (8)$$

The stresses σ_{ij} relate to the strains as

$$\sigma_{ij} = C_{ijkl}(\varepsilon_{kl} - \varepsilon_{kl}^L), \quad (9)$$

where ε_{kl}^L are the insertion-induced strains and C_{ijkl} represents the stiffness coefficients of the crystal. The stresses obey mechanical equilibrium, namely,

$$\sigma_{ij,j} = 0. \quad (10)$$

As mentioned before, the particle is embedded in a porous and compliant matrix, so that we will neglect any traction on the surface of the particle, namely,

$$\sigma_{ij}n_j = 0, \quad (11)$$

where n_j represents a unit vector normal to the particle surface.

FIG. 4. (Color online) (a) The layered structure of LiCoO_2 . (b) Variation in lattice parameter along the z axis with normalized lithium concentration (reproduced from Ref. 32). The lattice parameter along the x axis is nearly a constant. (c) The cross section of the model. Lithium diffusion is along the x axis, toward the center of the particle. (d) The lithium diffusivity as a function of the normalized lithium concentration (reproduced from Ref. 33).

FIG. 5. (Color online) Lithium distribution with time for a LiCoO₂ particle at (a) discharge rate of 0.5C, (b) discharge rate of 2C. Here $x/L=0$ represents the center of the particle, and $x/L=1$ represents the outside surface.

III. NUMERICAL RESULTS FOR LiCoO₂

Following the above theory, we perform calculations for a LiCoO₂ particle. As illustrated in Fig. 4(a), LiCoO₂ has a layered crystalline structure, where oxygen ions form close-packed planes in an *ABCABC* sequence, and cobalt and lithium ions occupy alternating layers of octahedral sites between the oxygen layers. The oxygen ions cause repulsion between the neighboring layers. These oxygen layers are attracted to the lithium ions inserted between them. Thus, during discharge the insertion of lithium decreases the repulsion between the CoO₂ sheets and leads to a contraction.³² The lattice parameter along the direction normal to the CoO₂ sheets is shown as a function of lithium concentration in Fig. 4(b), which is reproduced from Ref. 32. The insertion of lithium also causes strains in the other directions of the crystal but these strains are much smaller,³² and will be neglected in our numerical simulation.

Diffusion of lithium is much faster in the planes between CoO₂ sheets than in the direction normal to the CoO₂ sheets.³³ In the numerical simulation, we consider the diffusion in the planes between CoO₂ sheets but neglect the diffusion normal to the sheets [Fig. 4(c)]. Experiments show that the diffusivity D decreases one order of magnitude when the normalized lithium concentration increases from 0.5 to 1.³³ The experimentally measured diffusivity as a function of the lithium concentration is reproduced in Fig. 4(d).

In practical applications, the size of an individual LiCoO₂ particle in an electrode is on the order of microns or smaller. At such a small scale, the particle is often a single

crystal or at most consists of a few grains.⁴ We assume that the particle is a single grain. In a commercial battery, LiCoO₂ particles typically take an equiaxed shape. For simplicity, we assume that the particle deforms under the plane-strain conditions, and has a square cross section of side $2L$ [Fig. 4(c)]. The plane-strain assumption should not alter the scaling with respect to length and time.

As illustrated in Fig. 4(c), within the cross section, lithium only diffuses along the x axis, between the CoO₂ sheets. The diffusion of lithium in the particle is governed by Eq. (7). In practice, the working regime for lithium cobalt oxide is in the range of $0.5 \leq c \leq 1$. In the simulation we have allowed the diffusivity to vary with concentration, a dependence that is usually neglected in other works. The initial and boundary conditions are given by

$$t = 0; \quad c = 0.5,$$

$$x = 0; \quad t > 0 \quad \frac{\partial c}{\partial x} = 0,$$

$$x = L; \quad t > 0 \quad -D(c) \nabla c = \text{constant}. \quad (12)$$

The constant in Eq. (12) is given by the discharge current density under galvanostatic (constant current) operation. Thus, in the simulation the discharge rate is controlled by changing the flux constant. Discharge is completed once the normalized concentration of lithium at the outside surface reaches a value of unity. The concentration profile of lithium inside the particle is obtained by solving the diffusion equation in COMSOL MULTIPHYSICS.

Figures 5(a) and 5(b) show the distributions of lithium at several times, at discharge rates of 0.5C and 2C, respectively. Here the discharge rates are reported in the C-rate convention given by C/τ , where the value of τ is calculated as the theoretical capacity (~ 140 mAh/g) divided by the discharge current. It is evident from the figures that, in both cases, the lithium concentration gradient increases with discharge time. This behavior is a direct consequence of the decrease in effective diffusivity with increasing Li content [see Fig. 4(d)]. As the discharge rate increases from 0.5C to of 2C, the lithium distribution inside the host particle becomes more inhomogeneous, in agreement with the schematics in Fig. 2.

This inhomogeneous distribution of Li results in a large deformation mismatch. The strain along the z direction [see Fig. 4(a)] in the host particle is given by

$$\varepsilon = \frac{l(c) - l_0}{l_0}, \quad (13)$$

where $l(c)$ is the lattice parameter in the direction normal to the CoO₂ sheets at a given lithium concentration, l_0 is the lattice parameter at the initial normalized lithium concentration $c=0.5$. Here we use the experimental values for the LiCoO₂ lattice parameter as a function of concentration to calculate the strain.³² The inhomogeneous distribution of lithium leads to a nonuniform strain field inside the particle and thus a stress field in the particle.

The elastic boundary-value problem is solved by using

FIG. 6. (Color online) (a) Mismatch strain profile. (b) Normalized stress distribution at various discharge rates when the normalized lithium concentration at the outer surface reaches unity. The center of the particle is under compression, and the outside surface is under tension.

the finite element software ABAQUS. An orthotropic material model is employed with stiffness coefficients taken from atomistic simulations.³⁴ The input strain field is simulated by imposing a thermal strain, equal to the concentration induced mismatch strain; the stress field is obtained as the output. In this configuration, the stress component σ_{zz} is the tensile stress responsible for the crack propagation. Figures 6(a) and 6(b) plot the internal mismatch strains and the normalized stress distributions as a function of the dimensionless distance at discharge rates of $0.5C$ and $2C$, respectively. We represent E as $C_{22}=375$ GPa used for the normalization. It can be seen that the outer shell (near $x/L=1$) of the particle is under tension, while the core (near $x/L=0$) is under compression during lithium insertion. The tensile stress in the outer shell may drive a preexisting crack to grow. The driving force is much larger for the faster discharge of rate $2C$ because of the highly inhomogeneous distribution of lithium.

To calculate the energy release rate, a crack of length a is assumed to preexist inside the particle. In the simulation, we fix the particle size and the location of the preexisting crack, and we vary the preexisting crack length and discharge rate. In each case, we use the stress distribution at the end of discharge. The J -integral is used to calculate the energy release rate. Figure 7 gives the normalized energy release rate dependence on the crack length to the particle size ratio, for discharge rates of $2C$, $4C$, and $6C$. The energy release rates are maximized at normalized lengths of 0.11, 0.09, and 0.07, respectively.

As pointed out in Sec. II, no preexisting crack can ad-

FIG. 7. (Color online) Energy release rate as a function of crack size at various discharge rates.

vance if the maximum energy release rate is smaller than the fracture energy. This condition defines a critical particle size

$$L_c = \frac{\Gamma}{Z_{\max} E \epsilon_m^2}, \quad (14)$$

where Z is found from Fig. 7. When the particle is smaller than the critical value, no preexisting crack in the particle can advance. The critical particle size as a function of discharge rate is illustrated in Fig. 8. Here we have used approximate fracture energy of 1 J/m² for LiCoO₂.³⁵ From the figure, decreasing the electrode particle size can effectively prevent fracture during fast charging.

Experimental observations of cracked LiCoO₂ particles in the literature are limited. Crack damage is reported for an average particle size of 300–500 nm after 50 cycles.⁴ The model presented here shows that fracture can be prevented by decreasing the electrode particle size and/or discharge rate. To further test the accuracy of the model, more data for fracture of particles of different sizes and for a range of discharge rates are needed. Finally, it should be noted we used stiffness coefficients derived from atomistic simulations and estimated fracture energy to calculate the critical particle size. These values may vary with lithium concentration,³⁶ and should be ascertained by further experiments.

FIG. 8. (Color online) Critical LiCoO₂ particle size to avoid crack propagation as a function of discharge rate.

IV. CONCLUDING REMARKS

Using a combination of diffusion kinetics and fracture mechanics, we have outlined a theory to study how material properties, particle size, and discharge rate affect fracture of electrodes in lithium-ion batteries. We characterize the discharge rate relative to diffusion rate by a dimensionless parameter χ . We characterize the magnitude of the elastic energy relative to the fracture energy by a dimensionless parameter Λ . A “fracture map,” demonstrating criteria for fracture, can be constructed in terms of the nondimensional parameters Λ and χ . To illustrate the theory, a numerical example of a LiCoO_2 particle is presented. We calculate the distribution of lithium and stress at different discharge rates. We also calculate the energy release rates for preexisting flaws of different sizes. When the maximum energy release rate is smaller than the fracture energy, no pre-existing cracks can advance. This approach enables us to calculate the critical particle size and discharge rate necessary to avoid fracture.

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