Estimating the Health Effects of Environmental Exposures: Statistical Methods for the Analysis of Spatio-temporal Data

The Harvard community has made this article openly available. Please share how this access benefits you. Your story matters

<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Citable link</td>
<td><a href="http://nrs.harvard.edu/urn-3:HUL.InstRepos:11158266">http://nrs.harvard.edu/urn-3:HUL.InstRepos:11158266</a></td>
</tr>
<tr>
<td>Terms of Use</td>
<td>This article was downloaded from Harvard University’s DASH repository, and is made available under the terms and conditions applicable to Other Posted Material, as set forth at <a href="http://nrs.harvard.edu/urn-3:HUL.InstRepos:dash.current.terms-of-use#LAA">http://nrs.harvard.edu/urn-3:HUL.InstRepos:dash.current.terms-of-use#LAA</a></td>
</tr>
</tbody>
</table>
Estimating the Health Effects of Environmental Exposures: Statistical Methods for the Analysis of Spatio-temporal Data

A dissertation presented

by

Andrew William Correia

to

The Department of Biostatistics

in partial fulfillment of the requirements
for the degree of
Doctor of Philosophy
in the subject of
Biostatistics

Harvard University
Cambridge, Massachusetts

April 2013
Estimating the Health Effects of Environmental Exposures: Statistical Methods for the Analysis of Spatio-temporal Data

Abstract

In the field of environmental epidemiology, there is a great deal of care required in constructing models that accurately estimate the effects of environmental exposures on human health. This is because the nature of the data that is available to researchers to estimate these effects is almost always observational in nature, making it difficult to adequately control for all potential confounders - both measured and unmeasured. Here, we tackle three different problems in which the goal is to accurately estimate the effect of an environmental exposure on various health outcomes.

In Chapter 1, we extend and expand upon a previous study examining the relationship between fine particle air pollution and life expectancy in the United States (US) by analyzing data from the period 2000 to 2007 from 545 counties across the US. Using straightforward regression techniques, we estimate the association between changes in air pollution levels and changes in life expectancy over the period from 2000 to 2007 for the entire US as well as for a number of subpopulations within the US.

Chapter 2 builds upon the previous chapter by developing a modeling approach for estimating the effects of monthly variations in fine particle air pollution on monthly variations in mortality while controlling for potential sources of confounding. We first show via a simulation study where previous approaches to estimating this relationship break down. We then propose a new model to overcome those deficiencies, and we evaluate this approach using a large Medicare dataset linked with air pollution exposure estimates from across the US.
In Chapter 3, we evaluate the impact of noise exposure from airports on hospitalizations for cardiovascular disease (CVD) among Medicare enrollees living in zip codes surrounding major airports in the continental US. We begin with a fully Bayesian hierarchical Poisson model for the expected number of CVD hospitalizations in each zip code as a function of exposure to noise as well as several other individual and area-level covariates. We then conduct a thorough sensitivity analysis, examining potential sources of confounding, spatial dependence, and the possibility of a threshold effect.
Contents

Title page ........................................... i
Abstract ........................................... iii
Table of Contents .................................. v

Acknowledgments ..................................... vii

1 The Effect of Air Pollution Control on Life Expectancy in the United States: An Analysis of 545 US counties for the period 2000 to 2007 1
1.1 Introduction .................................... 2
1.2 Methods ........................................ 3
    1.2.1 Data ...................................... 3
    1.2.2 Statistical Analysis ......................... 7
1.3 Results ........................................ 8
1.4 Discussion ..................................... 21

2 A Closer Look at Exposure Decomposition in Long-term Air Pollution Studies: A Distributed Lag Approach 26
2.1 Background .................................... 27
2.2 Overview of Methodology and Modeling Assumptions ................. 28
2.3 Simulation Study ............................... 30
    2.3.1 Equality of $\eta_1$ and $\eta_2$ ................. 30
    2.3.2 Size of the Window for Averaging Monthly Air Pollution ......... 34
2.4 Extensions to Greven et al ........................ 39
2.5 Methods ................................................................. 42
  2.5.1 Statistical Approach .............................................. 42
2.6 Results ............................................................... 44
2.7 Discussion ............................................................ 50

3 Exposure to Aircraft Noise and Hospital Admissions for Cardiovascular Diseases: A Large National Multi-Airport Population Cohort Study 54
  3.1 Introduction .......................................................... 55
  3.2 Methods .............................................................. 56
    3.2.1 Noise Exposure Estimates ...................................... 56
    3.2.2 Statistical Methods ............................................. 58
  3.3 Results .............................................................. 61
  3.4 Sensitivity Analyses ................................................ 76
    3.4.1 Residual Spatial Confounding ................................... 76
    3.4.2 Modeling Spatial Dependency ................................... 80
    3.4.3 Threshold Effects and Non-linearity in the Exposure Response Curve 84
  3.5 Discussion .......................................................... 85

Appendix ................................................................. 91

References ............................................................... 99
Acknowledgments

I would like to thank my advisor, Francesca Dominici, for being an excellent mentor, and for her support, positive energy, and commitment to not only me, but to everyone in our group.

I would also like to thank my committee members Jonathan Levy and Brent Coull for their guidance and feedback, as well as Arden Pope, Majid Ezzati, and Doug Dockery who all played a significant role in my development as a graduate student. I feel quite fortunate to have had a chance to work with each these very talented and dedicated people.

I am extremely grateful to my parents, Gil and Gabriela Correia, whose love and support helped me to become the person I am today. Thank you for always encouraging me, for always pushing me to do better, and for never letting me quit anything I started.

Lastly, I would like to thank my beautiful bride to be, Andrea Saunders. Thank you for always being there, no matter what.
Dedicated to my Dad.
The Effect of Air Pollution Control on Life Expectancy in the United States: An Analysis of 545 US counties for the period 2000 to 2007

Andrew W. Correia\textsuperscript{1}, C. Arden Pope III\textsuperscript{2}, Douglas W. Dockery\textsuperscript{3}, Yun Wang\textsuperscript{1}, Majid Ezzati\textsuperscript{4}, and Francesca Dominici\textsuperscript{1}

\textsuperscript{1} Department of Biostatistics, Harvard University

\textsuperscript{2} Department of Economics, Brigham Young University

\textsuperscript{3} Departments of Environmental Health and Epidemiology, Harvard School of Public Health

\textsuperscript{4} MRC-HPA Centre for Environment and Health and Department of Epidemiology and Biostatistics, Imperial College London
1.1 Introduction

Since the 1970s, enactment of increasingly stringent air quality controls has led to improvements in ambient air quality in the United States at costs that the U.S. Environmental Protection Agency (EPA) has estimated as high as $25 billion per year (United States Environmental Protection Agency (1997)). However, even with the well-established link between long-term exposure to air pollution and adverse effects on health (Pope (2007)), the extent to which more recent regulatory actions have benefited public health remains in question.

Air pollutant concentrations have been generally decreasing in the U.S., with substantial differences in reductions across metropolitan areas. Levels of fine particulate matter air pollution (particulate matter < $2.5\mu g/m^3$ in aerodynamic diameter, PM$_{2.5}$) remain relatively high in some areas. In a 2010 study, the EPA estimated that 62 U.S. counties, accounting for 26% of their total study population, had PM$_{2.5}$ concentrations not in compliance with the National Ambient Air Quality Standards (NAAQS) (Schmidt et al. (2010)).

Reductions in particulate matter air pollution are associated with reductions in both cardiopulmonary and overall mortality (Pope (2007)). In the mid-1990s, the Harvard Six Cities Study and the American Cancer Society (ACS) study reported associations of cardiopulmonary mortality risk with chronic exposure to fine particulate air pollution while controlling for smoking and other individual risk factors (Dockery et al. (1993); Pope et al. (1995)). Reanalysis and extended analyses of these studies have confirmed that fine particulate air pollution is an important independent environmental risk factor for cardiopulmonary disease and mortality (Krewski et al. (2000); Pope et al. (2002, 2004); Jerrett et al. (2005); Laden et al. (2006); Krewski et al. (2005b,a)). Additional cohort studies, population-based studies, and short-term time-series studies have also shown associations between reductions in air pollution and reductions in human mortality (Burnett et al. (2001); Samet et al. (2000); Schwartz et al. (2008); Evans et al. (1984); Özkaynak and Thurston (1987); Pope and Dockery (2006); Schwartz (1991, 1992); Dominici et al. (2003)).
More recently, studies have suggested an association between PM$_{2.5}$ and life expectancy (Tainio et al. (2007); Pope et al. (2009)), a well-documented and important measure of overall public health (Brunekreef (1997); McMichael et al. (1998); Rabl (2003)).

As our primary analysis, we estimate the association between changes in PM$_{2.5}$ and in life expectancy in 545 U.S. counties during the period 2000 to 2007. This period is of particular interest, as the EPA restarted wide collection of PM$_{2.5}$ data in 1999 - 2000, after stopping the nationwide PM$_{2.5}$ monitoring program during the mid-1980s and most of the 1990s. In secondary analyses, we extended the data and statistical analysis originally reported by Pope et al. (2009) for the period 1980 - 2000 to 2007, and investigated whether the relationship reported by Pope et al. (2009) persists in the more recent years.

1.2 Methods

1.2.1 Data

We constructed and analyzed three data sets to estimate the association between changes in life expectancy and changes in PM$_{2.5}$ during the period 2000 to 2007 in 545 counties (Dataset 1), and to investigate whether the association previously reported by Pope et al. (2009) persists when the data on the same 211 counties are extended to the year 2007 (Datasets 2 and 3).

Dataset 1 included information on 545 U.S. counties for the years 2000 and 2007. These counties include all counties with available matching PM$_{2.5}$ data for 2000 and 2007. Additionally, unlike previous work in which counties were located only in metropolitan areas Pope et al. (2009), Dataset 1 is comprised of counties in both metropolitan and non-metropolitan areas. Figure 1.1 shows the counties in this dataset shaded according to life expectancy in 2000 and 2007. Variables in this dataset were available at the county level, for both 2000 and 2007, and included: life expectancy, PM$_{2.5}$, per capita income, population, proportions who were high school graduates, and propor-
tions who were white, black, or Hispanic. Because data on smoking prevalence were not available for all 545 counties, we used age-standardized death rates for lung cancer and chronic obstructive pulmonary disease (COPD) as proxy variables for smoking prevalence [Peto et al. (1992); Eftim et al. (2008)]. Death rates were calculated in 5-year age groups and age-standardized for the 2000 U.S. population of adults 45 years of age or older. Daily PM$_{2.5}$ data were obtained from the EPA’s Air Quality System (AQS - http://www.epa.gov/ttn/airs/airsaqs/detaildata/downloadaqsdata.htm). Daily PM$_{2.5}$ levels for each county were averaged across monitors within that county using a trimmed mean approach; those daily county-level means were further averaged across days to obtain a county-specific yearly PM$_{2.5}$ average [Peng and Dominici (2008)].

County-level life expectancies were calculated by applying a mixed-effects spatial Poisson model to mortality data from the National Center for Health Statistics (NCHS) and population data from the U.S. Census to obtain robust estimates of the number of deaths in each county [Kulkarni et al. (2011)]. These estimated counts were then used to calculate county life expectancies using standard life table techniques, which we discuss in more detail in the eAppendix (Section A).

Socioeconomic and demographic variables were obtained from the U.S. Census and the American Community Survey except per capita income, which was obtained from the Bureau of Economic Analysis. All yearly income variables were adjusted for inflation with 2000 as the base year. Age-standardized death rates for lung cancer and COPD were calculated using mortality data from NCHS using death rates for 2005 to serve as a proxy for 2007 (NCHS data for 2007 was not readily available). Lastly, data on smoking prevalence (proportion of the population who are current smokers) were available from the Behavioral Risk Factor Surveillance System in both 2000 and 2007 for 383 of the 545 counties.

Dataset 2 included data for the year 1980 and the year 2000 for the same 211 U.S. counties included in the 51 metropolitan statistical areas (MSAs) previously analyzed by Pope et al. (2009). This dataset is identical to that in the paper by Pope et al. (2009) where
Figure 1.1: United States County Maps Shaded by Life Expectancy: Maps of the US with the 545 counties from Dataset 1 shaded according to life expectancy for the years 2000 (a) and 2007 (b).
Figure 1.1 (Continued)

(a) yr. 2000 county life expectancies

(b) yr. 2007 county life expectancies
it is described in more detail.

Dataset 3 extended Dataset 2 to 2007. All data were available at the county level except for $PM_{2.5}$, which for the year 1980 was available only at the MSA level and for the year 2007 was available at the county level for only 113 of the 211 counties originally included in Pope et al. (2009). Thus, for the year 2007, we assigned the same $PM_{2.5}$ values to all the counties that shared an MSA, consistent with the previous analysis by Pope et al. (2009). Details and results pertaining to Datasets 2 and 3 are summarized in the eAppendix (Section B1).

1.2.2 Statistical Analysis

Cross-sectional and first-difference linear regression models were fitted to all three datasets. Specifically, we regressed life expectancy versus $PM_{2.5}$ levels across counties separately for the years 1980 (Dataset 2), 2000 (Datasets 1 and 2), and 2007 (Datasets 1 and 3). We then regressed changes in life expectancy over the years 2000 to 2007 (Datasets 1 and 3), 1980 to 2000 (Dataset 2), and 1980 to 2007 (Dataset 3) versus changes in $PM_{2.5}$ over those same periods adjusted for changes in the socioeconomic, demographic, and proxy smoking variables outlined above. Additionally for our largest dataset (Dataset 1: 545 counties, 2000 to 2007), we also performed several stratified and weighted analyses. More specifically, we estimated the effect of changes in $PM_{2.5}$ on life expectancy in models stratified by: 1) percentage of the population with an urban residence in 2000; 2) population density in 2000; 3) land area in 2000; 4) $PM_{2.5}$ levels in 2000; 5) 5-year in-migration in 2000; and 6) change in average yearly temperature over the entire period. These stratified analyses allowed us to examine whether $PM_{2.5}$ effects on life expectancy were different in counties with particular demographic or weather characteristics. The sensitivity of our results to model specification was further assessed by fitting models weighted by: 1) total population; 2) year 2000 population density; and 3) inverse land area. We included direct measures of the change in prevalence of smoking for the subgroup of counties with matching data on smoking prevalence (383 out of 545), and
fit separate models for men and women to determine if effects differed by sex. To account for the correlation due to clustering of counties in the same MSA, robust clustered standard errors were calculated for all models [Pope et al. (2009); Diggle et al. (1994)]. Specifically, the variance of the vector of estimated regression coefficients, \( \hat{\beta} \), is given by:

\[
\text{Var}(\hat{\beta}) = (X^T X)^{-1} \left( X^T \hat{V} X \right) (X^T X)^{-1},
\]

where \( \hat{V} \) is a block-diagonal matrix with non-zero blocks \( V_{0,j} = (y_j - \hat{\mu}_j) (y_j - \hat{\mu}_j)^T \), where \( j \) indexes the MSAs, \( y_j \) is the vector of observed outcomes in MSA \( j \), and \( \hat{\mu}_j \) is the vector of fitted values from a standard ordinary least squares (OLS) regression for MSA \( j \). \( \hat{\beta} \) is equal to the OLS estimator. Models were estimated using either REGRESS in Stata version 11.0, `lm()` in R version 2.11.1, or PROC SURVEYREG in SAS version 9.2.

### 1.3 Results

We report the results of our primary analysis, which estimated the cross-sectional relationship between life expectancy and PM2.5, and between changes in life expectancy and changes in PM2.5, for the period 2000 to 2007 in 545 US counties (Dataset 1). Results of the secondary analyses of the counties studied by Pope et al. (2009) using Datasets 2 and 3 are summarized in Appendix D (Tables 4.1 - 4.4). Table 1.1 lists the summary statistics for the variables in Dataset 1. In 2000, 189 of the 545 counties had a PM2.5 level greater than the current 3-year NAAQS level of 15\( \mu \text{g/m}^3 \); by 2007 only 48 of those 189 were not in compliance with the NAAQS. On average, PM2.5 levels decreased at a rate of 0.22\( \mu \text{g/m}^3 \) per year, a rate 33% lower than observed in the 211 counties analyzed for the period 1980 to 2000 (0.33\( \mu \text{g/m}^3 \) per year) [Pope et al. (2009)].

Figures 1.2A and 1.2B show life expectancies plotted against PM2.5 levels for the years 2000 and 2007. Consistent with Pope et al. (2009) cross-sectional regression models showed a negative association between life expectancy and PM2.5 in both years. Details are summarized in the Appendix C. Figures 1.2C and 1.2D show changes in life expectancy plotted against changes in PM2.5 levels for 2000 to 2007. We also plotted the estimated regression lines under Models 1 and 3 of Table 1.2, defined below.
Table 1.1: **Summary Characteristics of the 545 Counties Analyzed for the Years 2000 to 2007:** (*), 2005 death rates are used as a proxy for 2007 death rates. COPD denotes chronic obstructive pulmonary disease.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Mean(SD)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Life Expectancy (yr.)</td>
<td></td>
</tr>
<tr>
<td>2000</td>
<td>76.7 (1.7)</td>
</tr>
<tr>
<td>2007</td>
<td>77.5 (2.0)</td>
</tr>
<tr>
<td>Change</td>
<td>0.8 (0.6)</td>
</tr>
<tr>
<td>PM$_{2.5}$ ($\mu$g/m$^3$)</td>
<td></td>
</tr>
<tr>
<td>2000</td>
<td>13.2 (3.4)</td>
</tr>
<tr>
<td>2007</td>
<td>11.6 (2.8)</td>
</tr>
<tr>
<td>Reduction</td>
<td>1.6 (1.5)</td>
</tr>
<tr>
<td>Per Capita Income (in thousands of $)</td>
<td></td>
</tr>
<tr>
<td>2000</td>
<td>27.9 (7.4)</td>
</tr>
<tr>
<td>2007</td>
<td>30.4 (7.9)</td>
</tr>
<tr>
<td>Change</td>
<td>2.5 (2.3)</td>
</tr>
<tr>
<td>Population (in hundreds of thousands)</td>
<td></td>
</tr>
<tr>
<td>2000</td>
<td>3.5 (6.3)</td>
</tr>
<tr>
<td>2007</td>
<td>3.8 (6.6)</td>
</tr>
<tr>
<td>Change</td>
<td>0.3 (0.6)</td>
</tr>
<tr>
<td>HS Graduates (% of pop.)</td>
<td></td>
</tr>
<tr>
<td>2000</td>
<td>0.81 (0.07)</td>
</tr>
<tr>
<td>2007</td>
<td>0.85 (0.06)</td>
</tr>
<tr>
<td>Change</td>
<td>0.04 (0.02)</td>
</tr>
<tr>
<td>Black Population (% of pop.)</td>
<td></td>
</tr>
<tr>
<td>2000</td>
<td>0.115 (0.138)</td>
</tr>
<tr>
<td>2007</td>
<td>0.117 (0.139)</td>
</tr>
<tr>
<td>Change</td>
<td>0.002 (0.017)</td>
</tr>
<tr>
<td>Hispanic Population (% of pop.)</td>
<td></td>
</tr>
<tr>
<td>2000</td>
<td>0.119 (0.189)</td>
</tr>
<tr>
<td>2007</td>
<td>0.098 (0.135)</td>
</tr>
<tr>
<td>Change</td>
<td>-0.021 (0.057)</td>
</tr>
<tr>
<td>Deaths from Lung Cancer (no./ 10,000 pop.)*</td>
<td></td>
</tr>
<tr>
<td>2000</td>
<td>16.4 (3.5)</td>
</tr>
<tr>
<td>2007</td>
<td>15.5 (3.8)</td>
</tr>
<tr>
<td>Change</td>
<td>-0.9 (2.2)</td>
</tr>
<tr>
<td>Deaths from COPD (no./ 10,000 pop.)*</td>
<td></td>
</tr>
<tr>
<td>2000</td>
<td>12.8 (3.1)</td>
</tr>
<tr>
<td>2007</td>
<td>12.5 (3.5)</td>
</tr>
<tr>
<td>Change</td>
<td>-0.3 (2.1)</td>
</tr>
</tbody>
</table>
Figure 1.2: **Cross Sectional and First Difference Plots of PM$_{2.5}$ vs. Life Expectancy:** Cross-sectional life expectancies plotted vs PM$_{2.5}$ levels for (A) 2000 and (B) 2007 in Dataset 1. The slopes of the regression lines correspond to estimates from the simple model: $LE = \text{intercept} + \text{slope} \times \text{PM}_{2.5}$ in both the 2000 and 2007 plots. In the second row on the left (C) the data are plotted as change in life expectancy vs change in PM$_{2.5}$ over the period 2000 - 2007. The regression line corresponds to the simple model $\Delta LE = \text{intercept} + \text{slope} \times \Delta \text{PM}_{2.5}$ (Model 1 in Table 1.2). (D) On the right is the added variable plot for PM2.5 corresponding to Model 3 in Table 1.2.
Figure 1.2 (Continued)
Table 1.2 summarizes estimated regression coefficients for the association between changes in PM$_{2.5}$ and changes in life expectancy for 545 counties for 2000 to 2007 for selected regression models. When controlling for changes in all available socioeconomic and demographic variables as well as smoking prevalence proxy variables (Model 3), a 10µg/m$^3$ decrease in PM$_{2.5}$ was associated with an estimated mean increase in life expectancy of 0.35 years (SE= 0.16 years, $p = 0.033$). The estimated effect of PM$_{2.5}$ on life expectancy was consistent across models adjusting for various patterns of potentially confounding variables (e.g. Models 2 & 3). Models 4 - 8 of Table 1.2 show the results for select stratified and weighted regressions. In counties with a population density greater than 200 people per square mile, a 10µg/m$^3$ decrease in PM$_{2.5}$ was associated with an increased life expectancy of 0.72 (0.22 years, $p < 0.01$) (Model 5), compared with -0.31 years (0.22 years, $p = 0.165$) in counties with less than 200 people per square mile (P difference $< 0.01$). In counties whose proportion of urban residences was greater than 90 percent, a 10µg/m$^3$ decrease in PM$_{2.5}$ was associated with an increased life expectancy of 0.95 (0.31, $p < 0.01$) (Model 6), compared with -0.16 (0.16 years, $p = 0.299$) in counties with less than 90% urban residences (P difference $< 0.01$).
Table 1.2: **Results of Selected Regression Models for County-Level Analysis, 2000 - 2007:**

- (a), Included only counties with the largest year 2000 population in their respective MSA;
- (b), Included only counties with a year 2000 population density > 200 people per square mile;
- (c), Included only counties with a year 2000 urban rate > 90%;
- (d), Weighted by the square root of the year 2000 population density;
- (e), Weighted by the inverse of county land area. Estimate for the effect of PM$_{2.5}$ is for a 10µg/m$^3$ reduction; change in income is given in thousands of dollars. Changes in LC ASDR and COPD ASDR are changes in the age standardized death rate for lung cancer and chronic obstructive pulmonary disease, respectively.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Model 1</th>
<th>Model 2</th>
<th>Model 3</th>
<th>Model 4$^a$</th>
<th>Model 5$^b$</th>
<th>Model 6$^c$</th>
<th>Model 7$^d$</th>
<th>Model 8$^e$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Intercept</td>
<td>0.82±0.04</td>
<td>1.08±0.08</td>
<td>1.00±0.08</td>
<td>0.97±0.10</td>
<td>0.91±0.11</td>
<td>0.84±0.15</td>
<td>0.79±0.15</td>
<td>0.67±0.15</td>
</tr>
<tr>
<td>Reduction in PM$_{2.5}$</td>
<td>0.14±0.19</td>
<td>0.35±0.17</td>
<td>0.35±0.16</td>
<td>0.30±0.23</td>
<td>0.72±0.22</td>
<td>0.95±0.31</td>
<td>0.74±0.24</td>
<td>0.96±0.28</td>
</tr>
<tr>
<td>Change in income</td>
<td>–</td>
<td>0.013±0.017</td>
<td>0.017±0.018</td>
<td>0.005±0.018</td>
<td>0.02±0.02</td>
<td>0.01±0.03</td>
<td>0.03±0.02</td>
<td>0.05±0.02</td>
</tr>
<tr>
<td>Change in pop.</td>
<td>–</td>
<td>0.13±0.05</td>
<td>0.11±0.05</td>
<td>0.07±0.05</td>
<td>0.06±0.04</td>
<td>0.02±0.04</td>
<td>0.07±0.06</td>
<td>0.34±0.12</td>
</tr>
<tr>
<td>Change in HS%</td>
<td>–</td>
<td>-9.12±1.61</td>
<td>-7.98±1.56</td>
<td>-7.27±1.95</td>
<td>-4.42±2.60</td>
<td>-4.04±3.20</td>
<td>-1.94±3.35</td>
<td>-3.30±3.45</td>
</tr>
<tr>
<td>Change in black%</td>
<td>–</td>
<td>-6.55±2.05</td>
<td>-6.34±1.97</td>
<td>-7.86±3.07</td>
<td>-12.56±3.59</td>
<td>-8.12±2.84</td>
<td>-11.14±3.00</td>
<td>-6.21±2.97</td>
</tr>
<tr>
<td>Change in Hisp%</td>
<td>–</td>
<td>-2.16±0.47</td>
<td>-2.03±0.47</td>
<td>-2.12±0.59</td>
<td>-0.95±0.62</td>
<td>5.28±3.58</td>
<td>-3.25±0.63</td>
<td>-4.57±0.75</td>
</tr>
<tr>
<td>Change in LC ASDR</td>
<td>–</td>
<td>–</td>
<td>0.02±0.02</td>
<td>0.02±0.02</td>
<td>0.01±0.05</td>
<td>0.05±0.05</td>
<td>0.07±0.02</td>
<td>0.07±0.03</td>
</tr>
<tr>
<td>Change in COPD ASDR</td>
<td>–</td>
<td>–</td>
<td>-0.05±0.01</td>
<td>-0.05±0.02</td>
<td>-0.06±0.03</td>
<td>-0.06±0.05</td>
<td>-0.08±0.02</td>
<td>-0.06±0.02</td>
</tr>
<tr>
<td>No. of county units</td>
<td>545</td>
<td>545</td>
<td>545</td>
<td>257</td>
<td>307</td>
<td>169</td>
<td>545</td>
<td>545</td>
</tr>
</tbody>
</table>
When we re-estimated Model 3 of Table 1.2 using the square root of population density as the weight (Model 7), the estimated effect of a $10 \mu g/m^3$ reduction of PM$_{2.5}$ on life expectancy was more than double that observed in our un-weighted analysis ($0.74 [0.24]$ vs. $0.35 [0.16]$). When that same model was weighted by the inverse of county land area (Model 8), the effect was nearly triple that of the un-weighted analysis ($0.96 [0.27]$). Table 1.3 summarizes a number of our stratified and weighted analyses.

Table 1.3: **Summary of Selected Stratified Regression Analyses for 545 Counties (Dataset 1, 2000 - 2007):** (*) Corresponds to the covariate pattern in Model 3 of Table 1.2. Covariates include change in income, change in population, change in proportion of high-school graduates, change in proportion of black population, change in proportion of Hispanic population, change in lung cancer mortality rate, and change in COPD mortality rate. Analysis used: SAS 9.2, PROC SURVEYREG, clustered by MSA, using the "weight" statement, and Stata 11.0, REGRESS using the "cluster" option.

<table>
<thead>
<tr>
<th>Selected counties and analysis</th>
<th>Number of Counties</th>
<th>$\hat{\beta}$ (SE, p) for $10 \mu g/m^3$ Reduction in PM$_{2.5}$ (full model)*</th>
</tr>
</thead>
<tbody>
<tr>
<td>2000 Pop. Den. &gt;1000</td>
<td>96</td>
<td>0.86 (0.45, 0.061)</td>
</tr>
<tr>
<td>2000 Pop. Den. &gt;800</td>
<td>116</td>
<td>0.62 (0.41, 0.139)</td>
</tr>
<tr>
<td>2000 Pop. Den. &gt;600</td>
<td>145</td>
<td>0.81 (0.32, 0.014)</td>
</tr>
<tr>
<td>2000 Pop. Den. &gt;400</td>
<td>197</td>
<td>0.84 (0.27, 0.003)</td>
</tr>
<tr>
<td>2000 Pop. Den. &gt;200</td>
<td>307</td>
<td>0.72 (0.22, 0.001)</td>
</tr>
<tr>
<td>2000 Pop. Den. &lt; 200</td>
<td>238</td>
<td>-0.31 (0.22, 0.165)</td>
</tr>
<tr>
<td>2000 urban rate &gt;90%</td>
<td>169</td>
<td>0.95 (0.31, 0.003)</td>
</tr>
<tr>
<td>2000 urban rate &gt;95%</td>
<td>109</td>
<td>1.12 (0.32, 0.001)</td>
</tr>
<tr>
<td>2000 Pop. Den. &gt;200 &amp; 2000 urban rate &gt;90%</td>
<td>159</td>
<td>0.96 (0.28, 0.001)</td>
</tr>
<tr>
<td>2000 urban rate &lt;90%</td>
<td>376</td>
<td>-0.16 (0.16, 0.299)</td>
</tr>
<tr>
<td>All counties, regression weighted by square root of 2000 Pop. Den.</td>
<td>545</td>
<td>0.74 (0.24, 0.002)</td>
</tr>
<tr>
<td>All counties, regression weighted by inverse of county land area</td>
<td>545</td>
<td>0.96 (0.27, 0.001)</td>
</tr>
</tbody>
</table>

We conducted similar analyses for the 211-county dataset for 1980 to 2007 and from 2000 to 2007, the results of which are presented in Tables 4.3 and 4.4 of Appendix D,
respectively. Results for the period from 1980 to 2000 were identical to those reported by Pope et al. (2009).

Figure 1.3 summarizes the point estimates and 95% confidence interval for the effect of a $10\mu g/m^3$ decrease in PM$_{2.5}$ on life expectancy for select un-weighted and un-stratified regression models in each dataset/time period. Models fitted using Datasets 2 and 3 (left) controlled for changes in income, population, proportion of the population that is black, lung cancer death rate, and COPD death rate, corresponding to Model 4 in eTables 2a,b. Models fitted using Dataset 1 controlled for all available variables and correspond to Model 3 in Table 1.2. These estimates were fairly consistent, though estimates corresponding to the counties from Pope et al. (2009) for the period 2000 to 2007 appeared slightly larger than those from other analyses.
Figure 1.3: **Effect Estimates and Confidence Intervals for the Effect of a 10µg/m$^3$ Decrease in PM$_{2.5}$ on Life Expectancy:** Estimates A and B were obtained from Dataset 3; Estimate C was obtained from Dataset 2. Estimates A, B, and C were adjusted for changes in income, population, proportion of the population that is black, lung cancer death rate, and COPD death rate (Model 4, eTables 2a,b). Estimates D, E, and F were obtained from Dataset 1, adjusted for changes in income, population, proportion of high school graduates, proportion of the population that is black, proportion of the population that is Hispanic, lung cancer death rate, and COPD death rate (Model 3, Table 1.2). "Pope et al" refers to Pope et al. (2009).
Figure 1.3 (Continued)

A: MSA-level PM; 1980 - 2007, 211 counties included in Pope et al
B: MSA-level PM; 2000 - 2007, 211 counties included in Pope et al
C: MSA-level PM; 1980 - 2000, 211 counties exactly as reported in Pope et al
D: County-level PM; 2000 - 2007, 545 counties
E: County-level PM; 2000 - 2007, 113 counties included in Pope et al
F: County-level PM; 2000 - 2007, 432 counties not included in Pope et al
In the analyses stratified by sex, the estimated effect of a $10\mu g/m^3$ reduction in PM$_{2.5}$ for the covariate pattern corresponding to Model 3 of Table 1.2 was an additional 0.59 (0.17) years of life expectancy for women and 0.08 (0.20) years for men (P difference = 0.027). Differences by sex were also observed in stratified and weighted models, although with less precision. Sex differences were smaller in the most urban counties (urban rate > 90%). Similar results were observed for the period 1980 to 2000 in Dataset 2. Sex-specific results are presented in Table 1.4.

### Table 1.4: Comparison of Results of Select Models for Males vs. Females (Dataset 1, 2000 - 2007)

<table>
<thead>
<tr>
<th>Selected counties and analysis</th>
<th>Males: $\hat{\beta}$ (SE, p) for 10$\mu g/m^3$ Dec. in PM$_{2.5}$ (full model)*</th>
<th>Females: $\hat{\beta}$ (SE, p) for 10$\mu g/m^3$ Dec. in PM$_{2.5}$ (full model)*</th>
</tr>
</thead>
<tbody>
<tr>
<td>All counties</td>
<td>0.08(0.20, 0.681)$^\dagger$</td>
<td>0.59(0.17, 0.001)$^\dagger$</td>
</tr>
<tr>
<td>2000 Pop. Density &gt; 200</td>
<td>0.44(0.25, 0.084)</td>
<td>0.85(0.24, 0.001)</td>
</tr>
<tr>
<td>2000 Pop. Density &lt; 200</td>
<td>-0.55(0.27, 0.043)</td>
<td>-0.06(0.24, 0.805)</td>
</tr>
<tr>
<td>2000 urban rate &gt; 90%</td>
<td>0.81(0.37, 0.033)</td>
<td>1.07(0.28, &lt;0.001)</td>
</tr>
<tr>
<td>2000 urban rate &lt; 90%</td>
<td>-0.44(0.20, 0.025)</td>
<td>0.08(0.19, 0.664)</td>
</tr>
<tr>
<td>All counties, regression weighted by square root of 2000 Pop. Den.</td>
<td>0.57(0.29, 0.047)</td>
<td>0.87(0.22, &lt;0.001)</td>
</tr>
<tr>
<td>All counties, regression weighted by inverse of county land area</td>
<td>0.74(0.30, 0.013)</td>
<td>1.14(0.30, &lt;0.001)</td>
</tr>
</tbody>
</table>

Effect estimates were not highly sensitive to the inclusion of the estimated change in smoking prevalence. Table 1.5 summarizes the results for the inclusion/exclusion of the smoking prevalence variable across several models. For example, when Model 3 in Table 1.2 was re-estimated for the 383 counties with matching smoking prevalence data,
a reduction of 10$\mu$g/m$^3$ was associated with an increase in life expectancy of 0.49 (0.19) years without including change in smoking prevalence in the model, and 0.47 (0.19) when including those changes. Similar results for smoking were observed in our stratified and weighted models, as well as in our models for men and women separately.
Table 1.5: **Comparison of PM$_{2.5}$ Effect Estimates from Selected Models for Inclusion of Smoking Variable Versus No Inclusion of Smoking Variable:** Covariates include change in income, change in population, change in high-school graduates, change in proportion of black population, change in proportion of Hispanic population, change in lung cancer mortality rate, change in COPD mortality rate. Analysis used: SAS 9.2, PROC SURVEYREG, clustered by MSA, using the "weight" statement, and Stata 11.0, REGRESS using the "cluster" option.

<table>
<thead>
<tr>
<th>Selected counties and analysis</th>
<th>No. Counties</th>
<th>Full model, with smoking: $\hat{\beta}$ (SE, p) per 10µg/m$^3$ PM$_{2.5}$</th>
<th>Full model, no smoking: $\hat{\beta}$ (SE, p) per 10µg/m$^3$ PM$_{2.5}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>All Counties</td>
<td>383</td>
<td>0.47(0.19, 0.013)</td>
<td>0.49(0.19, 0.011)</td>
</tr>
<tr>
<td>2000 population density</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>(persons per square mile)</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>&gt;800</td>
<td>110</td>
<td>0.52(0.43, 0.230)</td>
<td>0.53(0.43, 0.221)</td>
</tr>
<tr>
<td>&gt;600</td>
<td>139</td>
<td>0.68(0.30, 0.028)</td>
<td>0.68(0.30, 0.027)</td>
</tr>
<tr>
<td>&gt;400</td>
<td>187</td>
<td>0.71(0.26, 0.007)</td>
<td>0.70(0.25, 0.007)</td>
</tr>
<tr>
<td>&gt;200</td>
<td>272</td>
<td>0.67(0.22, 0.003)</td>
<td>0.65(0.22, 0.004)</td>
</tr>
<tr>
<td>&lt;200</td>
<td>111</td>
<td>-0.50(0.30, 0.100)</td>
<td>-0.39(0.30, 0.193)</td>
</tr>
<tr>
<td>2000 urban rate</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>&gt;90%</td>
<td>157</td>
<td>0.76(0.28, 0.009)</td>
<td>0.76(0.28, 0.008)</td>
</tr>
<tr>
<td>&gt;95%</td>
<td>101</td>
<td>1.01(0.31, 0.002)</td>
<td>0.98(0.32, 0.003)</td>
</tr>
<tr>
<td>&lt;90%</td>
<td>226</td>
<td>-0.14(0.20, 0.483)</td>
<td>-0.13(0.20, 0.513)</td>
</tr>
<tr>
<td>2000 population density &amp; 2000 urban rate</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>&gt;200 &amp; &gt;90%</td>
<td>100</td>
<td>0.95(0.32, 0.004)</td>
<td>0.93(0.32, 0.005)</td>
</tr>
<tr>
<td>Regression weighted by square root of 2000 population density (All counties)</td>
<td>383</td>
<td>0.77(0.24, 0.002)</td>
<td>0.76(0.25, 0.003)</td>
</tr>
<tr>
<td>Regression weighted by inverse of county land area (All counties)</td>
<td>383</td>
<td>0.81(0.26, 0.002)</td>
<td>0.74(0.27, 0.007)</td>
</tr>
<tr>
<td>Sex</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Men</td>
<td>383</td>
<td>0.20(0.23, 0.389)</td>
<td>0.22(0.23, 0.343)</td>
</tr>
<tr>
<td>Women</td>
<td>383</td>
<td>0.71(0.20, 0.001)</td>
<td>0.72(0.20, &lt;0.001)</td>
</tr>
</tbody>
</table>
1.4 Discussion

Data on air pollution and life expectancy from 545 US counties in 2000 and 2007 show that recent declines in PM$_{2.5}$ to relatively low levels continue to prolong life expectancy in the US. These benefits are largest among the most urban and densely populated counties. These associations were estimated controlling for socioeconomic and demographic variables as well proxy variables for and direct measures of smoking prevalence.

In previous studies, a $10\mu g/m^3$ decrease in PM$_{2.5}$ has been associated with gains from 0.42 to 1.51 years of life expectancy\textsuperscript{(Tainio et al. (2007); Pope et al. (2009))}. Here, a decrease of $10\mu g/m^3$ in PM$_{2.5}$ was associated with an increase in life expectancy of 0.35 (0.16) for 545 counties for the period from 2000 to 2007. An increase in life expectancy of 0.56 (0.19) was estimated for the same 211 counties included in the Pope et al. (2009) analysis but extended to the period 1980 to 2007. The estimated effect in those 211 counties from 2000 to 2007 was equal to 1.00 (0.32). Stratified and weighted analyses within the 545 counties from 2000 to 2007 yielded larger estimates between 0.72(0.22) and 1.12(0.32) - broadly in agreement with those previously reported.

From 2000 to 2007, the average increase in life expectancy across the counties in this study was 0.84 years, and the average decrease in PM$_{2.5}$ in those same counties was $1.56\mu g/m^3$. While PM$_{2.5}$ reductions presumably account for some of the improvements in life expectancy over this period, it is only one of many contributing factors. Other factors may include improvements in the prevention and control of the chronic diseases of adulthood, particularly cardiovascular diseases (CVD) and stroke (Yeh et al. (2011); Shrestha (2005)), and changes in the risk factors associated with them, including medical advances, declines in smoking, and decreases in blood pressure and cholesterol (Shrestha (2005)). Given the well-established link between air pollution and CVD mortality(Pope et al. (1995, 2002, 2004)), and changes in other CVD risk factors, issues of multicausality and competing risk make it difficult to quantify exactly the changes in life expectancy
attributable to reductions in PM$_{2.5}$. However, if we consider one of our more conservative effect estimates (Model 3, Table 1.2) the $1.56\mu g/m^3$ reduction in PM$_{2.5}$ accounts for about 0.055 years ($1.56 \times 0.0354$) of additional life expectancy, or roughly 7% of the increase in life expectancy. Using the estimate from our most urban counties (Model 6, Table 1.2), the increase in life expectancy attributable to the average reduction in PM$_{2.5}$ was 0.148 years ($1.56 \times 0.095$), or as much as 18% of the total increase.

An interesting aspect of this study was how pronounced the PM$_{2.5}$ effect was for the original 211 counties from 2000 to 2007. Given that they were originally selected simply on the availability of matching pollution data, what is special about these counties that results in larger estimates of the effect of PM$_{2.5}$ on life expectancy? The stratified and weighted analyses suggest plausible explanations. For instance, the 211 counties were all in metropolitan areas, and the stratified analyses suggest that the effect of PM$_{2.5}$ on life expectancy is greatest in the most urban counties. One possible reason is that the composition of PM$_{2.5}$ is different in urban areas (Louie et al. (2005)), causing PM$_{2.5}$ to have a larger health impact. Another possibility is the "non-metropolitan mortality penalty" - the recent phenomenon in which mortality rates are higher in rural compared with urban areas (Cossman et al. (2010)). While it is not clear why the mortality gap between metro and non-metro areas has widened, some hypotheses include greater improvements in standards of care in metro areas, changes in uninsurance rates, changes in disease incidence, and changes in health behaviors (Cossman et al. (2010)). These, however, would be valid explanations only if they occurred at different rates in metropolitan areas compared with rural areas. If so, then perhaps failure to include variables that captured one or more of these differences could explain the different estimates of the effect of PM$_{2.5}$ on life expectancy.

Alternatively, metropolitan areas are more densely populated than non-metro areas. Our models that stratified by population density showed that the effect of PM$_{2.5}$ on life expectancy is greatest in the most densely populated study areas (those with a population density of at least 200 people per square mile) - possibly suggesting a role
for differential exposure misclassification. That is, in densely populated areas, it is more likely that any two people from the same area are exposed to the same level of PM$_{2.5}$ with perhaps less exposure misclassification. This possibility was supported in our models weighted by the square root of population density and the inverse of land area, which placed more weight on the most densely populated counties and the smallest counties. In these models the effect of a 10µg/m$^3$ decrease in PM$_{2.5}$ on life expectancy was much larger than the equivalent un-weighted analysis.

Another interesting finding was the difference in the effect of changes in PM$_{2.5}$ on men and women. Findings in the literature regarding the effects of air pollution by sex for long-term exposure have been mixed. Studies using the ACS and Harvard Six-Cities cohorts show no significant difference in pollution-related mortality between men and women (Dockery et al. (1993); Pope et al. (1995); Krewski et al. (2000); Pope et al. (2002, 2004); Laden et al. (2006)). Studies using a Medicare cohort have reported different effects by age and region, but did not stratify by sex (Eftim et al. (2008); Greven et al. (2011); Zeger et al. (2008)). In a study using the Adventist Health cohort, Chen et al. (2005) reported a large effect of PM$_{2.5}$ on fatal coronary heart disease (CHD) in women but no association in men. Similarly, in separate studies, Ostro et al. (2010) using a cohort of women (California Teachers’ Study), reported associations between particulate matter and cardiovascular mortality, while Puett et al. (2011) using a cohort of men (Male Health Professionals), found no association with all-cause mortality or fatal CHD. For our main analysis using all 545 counties, we find a larger effect of PM$_{2.5}$ on women, suggesting that reductions in PM$_{2.5}$ are more beneficial to gains in life expectancy for women. Models fitted using data for the period from 1980 - 2000 as in Pope et al. (2009) showed similar results. Future work should investigate more thoroughly the possibility of different PM$_{2.5}$-mortality associations for men versus women.

One factor that appeared to play no role in the PM$_{2.5}$ and life expectancy relationship, however, was baseline PM$_{2.5}$ level. This is in agreement with the findings by Pope et al. (2009) and implies that, while we may see differences across levels of population
density, urban rate, and land area, this is not due to these areas having a higher or lower baseline PM$_{2.5}$ level. Furthermore, this finding suggests that there is no clear threshold below which further reductions in PM$_{2.5}$ levels provide no benefit (eAppendix, eTable 3). The fact that our results were not sensitive to the inclusion of direct measures of change in smoking prevalence suggests that the estimated gains in life expectancy for a $10\mu g/m^3$ reduction in PM$_{2.5}$ are not a result of confounding due to changes in smoking prevalence.

Table 1.6: Summary of Selected Regression Analyses Stratified by Baseline PM$_{2.5}$ Levels for 545 Counties (Dataset 1, 2000 - 2007): (*) Corresponds to the covariate pattern in Model 3 of Table 1.2. Covariates include change in income, change in population, change in proportion of high-school graduates, change in proportion of black population, change in proportion of Hispanic population, change in lung cancer mortality rate, and change in COPD mortality rate. Analysis used: SAS 9.2, PROC SURVEYREG, clustered by MSA, using the "weight" statement, and Stata 11.0, REGRESS using the "cluster" option.

<table>
<thead>
<tr>
<th>Selected counties and analysis</th>
<th>Number of Counties</th>
<th>$\beta$ (SE, p) for $10\mu g/m^3$ Reduction in PM$_{2.5}$ (full model)*</th>
</tr>
</thead>
<tbody>
<tr>
<td>2000 PM$_{2.5}$ &lt; 10mg/m$^3$</td>
<td>100</td>
<td>-0.28(0.39, 0.482)</td>
</tr>
<tr>
<td>2000 PM$_{2.5}$ &lt; 12mg/m$^3$</td>
<td>186</td>
<td>0.50(0.27, 0.065)</td>
</tr>
<tr>
<td>2000 PM$_{2.5}$ &lt; 14mg/m$^3$</td>
<td>301</td>
<td>0.61(0.21, 0.004)</td>
</tr>
<tr>
<td>2000 PM$_{2.5}$ &lt; 16mg/m$^3$</td>
<td>430</td>
<td>0.36(0.19, 0.064)</td>
</tr>
<tr>
<td>2000 PM$_{2.5}$ &lt; 18mg/m$^3$</td>
<td>511</td>
<td>0.47(0.18, 0.009)</td>
</tr>
<tr>
<td>2000 PM$_{2.5}$ &gt; 18mg/m$^3$</td>
<td>34</td>
<td>0.85(0.82, 0.314)</td>
</tr>
<tr>
<td>2000 PM$_{2.5}$ &gt; 16mg/m$^3$</td>
<td>115</td>
<td>0.87(0.38, 0.023)</td>
</tr>
<tr>
<td>2000 PM$_{2.5}$ &gt; 14mg/m$^3$</td>
<td>244</td>
<td>0.28(0.27, 0.305)</td>
</tr>
<tr>
<td>2000 PM$_{2.5}$ &gt; 12mg/m$^3$</td>
<td>359</td>
<td>0.15(0.21, 0.462)</td>
</tr>
<tr>
<td>2000 PM$_{2.5}$ &gt; 10mg/m$^3$</td>
<td>445</td>
<td>0.27(0.18, 0.126)</td>
</tr>
</tbody>
</table>

Unlike previous cross-sectional analyses [Evans et al. (1984); Özkaynak and Thurston (1987)], we were able to estimate the association between county-specific temporal changes in PM$_{2.5}$ levels and county-specific temporal changes on life expectancy adjusted by temporal changes in several potential confounding factors. By looking at within-county temporal changes, we reduce the potential bias due to unmeasured confounding. Further, by estimating clustered robust standard errors at the MSA level, we took a conservative approach in accounting for potential spatial correlation between neighboring counties.
Our analysis has the strengths of using some of the largest available datasets, and applying relatively simple analyses. Additionally, we improved on the original analysis by constructing a dataset with PM$_{2.5}$ measured at the county level, in contrast to the more coarse MSA-level readings used in previous studies \cite{Pope2002, Pope2009}.

The analysis is limited, however, in its ability to control for all potential unmeasured confounding. Additionally, in comparing selected years, we do not fully exploit potentially informative data between those years. Furthermore, sophisticated analyses of the U.S. Medicare population by Greven et al. \cite{Greven2011} did not observe associations between "local" trends in PM$_{2.5}$ levels and "local" trends in mortality in 814 zip code level locations in the U.S. for the period 2000 - 2006. "Local" trends were defined as the difference between monitor-specific trends and national trends. The Medicare cohorts, however, consisted only of people age 65 and older, whereas our life expectancy calculations integrate over all ages. Also, other studies using Medicare based cohorts have found significant associations between PM$_{2.5}$ and overall mortality \cite{Eftim2008, Zeger2008}. Future work is needed to investigate whether these differences among studies are due to differences in statistical models, data sources, or populations studied.

It is also worth considering whether life expectancy was the most appropriate outcome to consider in our model. Because life expectancies are calculated from age-specific mortality rates, perhaps a model with age-specific mortality rates as the outcome would be more appropriate, allowing the age groups most affected by PM$_{2.5}$ exposure to be pinpointed precisely.

In summary, our study reports strong evidence of an association between recent further reductions in fine-particulate air pollution and improvements in life expectancy in the United States, especially in small, densely populated urban areas.
A Closer Look at Exposure Decomposition in Long-term Air Pollution Studies: A Distributed Lag Approach

Andrew W. Correia and Francesca Dominici

Department of Biostatistics
Harvard University
2.1 Background

In the environmental epidemiology literature, there has been a great deal of work on assessing the impacts of air pollution exposure on various health outcomes. These studies range from short-term daily time-series studies {Dominici et al. (2002, 2003)}, to long-term cohort studies {Pope et al. (1995); Dockery et al. (1993)}, to long-term population based studies {Pope et al. (2009); Correia et al. (2013)}. Due to the nature of the research question of interest and the data available to researchers to answer those questions, the majority of these studies are observational. In general, caution is urged when interpreting parameter estimates from observational studies, as it is very difficult to properly control for every potential confounder (measured and unmeasured) in an observational study {Christenfeld et al. (2004); Greenland and Morgenstern (2001)}. Therefore, a major concern in environmental epidemiology is bias due to residual confounding, and indeed in both long-term and short-term studies, some critics argue that the estimated effect estimates of air pollution on mortality and morbidity are unreliable due to the difficulty of fully controlling for all potential confounders {Vedal (1997); Moolgavkar (1994, 2005)}.

Recent work by Janes et al., 2007 and Greven et al., 2011 has attempted to overcome issues of residual confounding by decomposing the air pollution exposure variable into a "local" term and a "global" term, where under certain assumptions, differences in the estimated effects of the "local" and "global" terms implies unmeasured confounding. The approach taken in these two papers has been somewhat controversial, as the models fitted via the exposure decomposition approach have estimated a null effect of air pollution on mortality at the "local" level - quite a contrast to the majority of literature on the subject. However, a thorough investigation of the modeling approach in Janes et al., 2007 and Greven et al., 2011 and a discussion as to why the results in those papers stand in contrast to the majority of the literature on air pollution and mortality has, to our knowledge, not been undertaken. The outline of this paper is as follows: 1) We will begin by focusing on the simpler approach presented in Janes et al., 2007, and discussing its methodology and modeling assumptions; 2) we illustrate the implications of those modeling assumptions
via simulation studies; 3) we then discuss the approach in Greven et al., 2011, showing how the modeling assumptions in that paper relate to those in Janes et al., 2007, and also how the simulation results apply to the Greven model; 4) we propose a model that is a combination of the Janes and Greven models, which also integrates a distributed lag on the "local" exposure term to more adequately model the temporal relationship between PM$_{2.5}$ and mortality; and 5) we close with a discussion.

2.2 Overview of Methodology and Modeling Assumptions

In Janes et al., 2007, the authors’ aim is to estimate the effect of PM$_{2.5}$ on mortality in 113 US counties from 1999 to 2002 in the Medicare population. A particular county’s monthly PM$_{2.5}$ level is calculated as the average of PM$_{2.5}$ over the preceding year - that is, the average PM$_{2.5}$ level over the past 12 months, including the current month. Mortality counts in a given month for any county are simply the sum of the number of deaths in that county for the given month; these monthly counts are not given by an average of mortality counts over the preceding year. The authors then stratify individuals into one of six different age-sex strata. It is assumed that the causal model for the effect of PM$_{2.5}$ on mortality in each age-sex stratum is given by:

$$
\log\text{E}(Y_{ct}^c) = \log(N_{ct}^c) + \delta_0^c + \delta_1 PM_{ct}^c;
$$

where $Y_{ct}^c$ and $N_{ct}^c$ are the mortality counts and number of people at risk, respectively, for each county $c$ and month $t$; the $\delta_0^c$ are county-specific random intercepts; and $\delta_1$ is the association between month-to-month variation in PM$_{ct}^c$ and month-to-month variation in mortality.

Because estimates from Model 2.1 are likely to be confounded by variables trending in a similar fashion to PM$_{2.5}$ and mortality, Janes and colleagues introduce another popular model in the environmental epidemiology literature in which temporal con-
founding is addressed, at least in part, by a smooth function of time. Specifically:

\[
\text{logE}(Y^c_t) = \log(N^c_t) + \beta_0^c + \beta_1 PM^c_t + s(t; d),
\]  

(2.2)

where \(\beta_0^c\) and \(\beta_1\) are defined analogously to \(\delta_0^c\) and \(\delta_1\), respectively, and \(s(t; d)\) is a natural cubic spline with \(d\) degrees of freedom. From Model 2.2, Janes et al., 2007 propose:

\[
\text{logE}(Y^c_t) = \log(N^c_t) + \eta_0^c + \eta_1 \widehat{PM}_t + \eta_2 (PM^c_t - \widehat{PM}_t) + s^*(t; d - 1),
\]  

(2.3)

where \(\widehat{PM}_t\) is the annual average in \(PM_{2.5}\) for month \(t\) across all counties and \(s^*(t; d - 1)\) is orthogonal to both \(\widehat{PM}_t\) and \(PM^c_t\).

Predicted values from Models 2.2 and 2.3 are equivalent. However, Janes et al., 2007 point out that because Model 2.3 estimates the association between \(PM_{2.5}\) and mortality at both a national scale and a local scale, we are able to detect unmeasured confounding via large differences between the estimates of \(\eta_1\) and \(\eta_2\) - if there is no confounding or measurement error, \(\eta_1\) and \(\eta_2\) should be equal; if there is confounding, it is more likely to be at the global-level (\(\eta_1\)) than at the local level (\(\eta_2\)). Additionally, the authors state that the random, county-specific intercepts in the model control for unmeasured county-specific characteristics that do not vary with time (i.e. they control for unmeasured spatial confounding).

In summary, the modeling assumptions given in Janes et al., 2007 (and, generally, in Greven et al., 2011 as well) are as follows:

1. The true causal model for the effect of \(PM_{2.5}\) on mortality is given by Model 2.1.

2. Absent confounding and measurement error, if the causal link between mortality and \(PM_{2.5}\) is given by Model 2.1 then the estimates of \(\eta_1\) and \(\eta_2\) in Model 2.3 should be equal.
3. Estimates should not be biased as a result of spatial confounding due to the inclusion of random, county-specific intercepts.

4. Mortality in month $t$ has a causal relationship with PM$_{2.5}$ levels averaged over the past twelve months up to and including $t$.

5. The estimate of $\eta_2$ is less likely to be confounded than the estimate of $\eta_1$.

Since one cannot ever know the true underlying causal model, we assume that item 1 is correct. Further, for reasons outlined in Janes et al., 2007 and Greven et al., 2011, we will proceed under the assumption that item 5 is correct as well. Then, given the proposed causal model (2.1), we test assumptions 2, 3 and 4 via simulation in the following section. Because the model in Greven et al., 2011 is much more computationally intensive, we conduct our simulations based on the model presented in Janes et al., 2007 and then discuss how those simulation results relate to the Greven model.

2.3 Simulation Study

2.3.1 Equality of $\eta_1$ and $\eta_2$

To test assumption 2, we first simulated data based on Model 2.1 with $\delta_1 = 0.009$ and with $\delta_0^c = -5.75$ for all $c$ using real PM$_{2.5}$ and population data - the same PM$_{2.5}$ and population data used in Greven et al., 2011, where it is described in more detail. We then analyzed the simulated data with Model 2.3 to be sure that we do indeed observe $\eta_1 \approx \eta_2$ in this simplest scenario. Note that because we assume $\delta_0^c = -5.75$ for all $c$, we fit Model 2.3 with a fixed intercept ($\eta_0$) instead of a random intercept ($\eta_0^c$). This is only to improve computational speed and has no impact on assessing the validity of assumption 2. Also note that we set $\delta_1 = 0.009$, as this corresponds roughly to the average estimate across strata in the non-decomposed model in Janes et al., 2007, and it is also roughly the average effect-estimate of a number of short-term studies summarized in Table 1 of Pope and Dockery, 2006. As this study explores mostly temporal variability, much like many
short-term studies, we believe this is a realistic, though perhaps conservative value for $\delta_1$ given the results in the literature for other long-term studies (Table 2, Pope and Dockery, 2006). Throughout this paper, the degrees of freedom parameter for the cubic spline in Models 2.2 and 2.3, $d$, is taken to be 16 as in Janes et al., 2007.

Results under this basic simulation assuming no confounding are given in Table 2.1 below. Indeed, though estimates of $\eta_1$ are a bit more variable than those of $\eta_2$, we see that, on average, $\eta_1 \approx \eta_2$ when there is no confounding.

Table 2.1: Performance of Model 2.3 Under the Assumption of no Confounding: $\eta_1$ is the global parameter and $\eta_2$ is the local parameter.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Avg. Estimate</th>
<th>Avg. SE</th>
<th>Avg. p-value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\eta_1$</td>
<td>$9.02 \times 10^{-3}$</td>
<td>$4.61 \times 10^{-3}$</td>
<td>0.150</td>
</tr>
<tr>
<td>$\eta_2$</td>
<td>$9.02 \times 10^{-3}$</td>
<td>$8.31 \times 10^{-4}$</td>
<td>&lt; 0.001</td>
</tr>
</tbody>
</table>

**Temporal Confounding**

We then simulate under Model 2.1 again, but with the addition of a confounder, $U_t$, trending only at the national level. That is, $U_t$ was generated to be correlated with both the outcome and $\hat{PM}_t$, but $U_t$ is not correlated with $(PM_t - \hat{PM}_t)$. Outcome data was generated via the following model:

$$\log(E(Y^{c}_t)) = \log(N^{c}_t) + \delta_0 + \delta_1 PM_t + \delta_2 U_t,$$

where $\delta_2 = 0.15$. Simulated data is again modeled under Model 2.3. Results are summarized in Table 2.2 below:

Here, we see that with a strong influence from a "global" confounder, the estimate of $\eta_1$ is indeed inflated, though the estimate of $\eta_2$ remains an accurate estimate of the
Table 2.2: **Performance of Model 2.3 Under the Assumption of Global-scale Temporal Confounding:** \(\eta_1\) is the global parameter and \(\eta_2\) is the local parameter.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Avg. Estimate</th>
<th>Avg. SE</th>
<th>Avg. p-value</th>
</tr>
</thead>
<tbody>
<tr>
<td>(\eta_1)</td>
<td>(8.44 \times 10^{-2})</td>
<td>(7.52 \times 10^{-3})</td>
<td>&lt; 0.001</td>
</tr>
<tr>
<td>(\eta_2)</td>
<td>(9.09 \times 10^{-3})</td>
<td>(1.38 \times 10^{-3})</td>
<td>&lt; 0.001</td>
</tr>
</tbody>
</table>

true effect. The same is true when outcomes are generated from a model with a positive interaction effect between \(\widehat{PM_t}\) and \(U_t\).

**Spatial Confounding**

In this section we test assumption 3 - that the estimates of \(\eta_1\) and \(\eta_2\) should not be impacted by confounders that do not vary with time to due to the inclusion of location-specific intercepts. Thus, consider a new confounder, \(U^c\), that only varies spatially and is constant across time. Outcome data is generated by:

\[
\log \mathbb{E}(Y^c_t) = \log(N^c_t) + \delta_0^c + \delta_1^c PM_t^c + \delta_2^c U^c_t, \tag{2.5}
\]

where \(\delta_0^c = -6.25\) for all \(c\), \(\delta_1 = 0.009\), and \(\delta_2 = -0.15\). \(U^c\) is generated such that \(\text{Corr}(U^c, \widehat{PM}_t^c) \approx 0.25\), and \(\widehat{PM}_t^c = (1/T) \sum_t PM_t^c \forall c\). We again model this outcome data via Model 2.3, but this time allowing for estimation of location-specific intercepts, \(\eta_0^c\). Results are summarized in Table 2.3 below.

Table 2.3: **Performance of Model 2.3 Under the Assumption of Spatial Confounding:** \(\eta_1\) is the global parameter and \(\eta_2\) is the local parameter.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Avg. Estimate</th>
<th>Avg. SE</th>
<th>Avg. p-value</th>
</tr>
</thead>
<tbody>
<tr>
<td>(\eta_1)</td>
<td>(1.04 \times 10^{-2})</td>
<td>(7.57 \times 10^{-3})</td>
<td>0.166</td>
</tr>
<tr>
<td>(\eta_2)</td>
<td>(-6.12 \times 10^{-3})</td>
<td>(3.04 \times 10^{-3})</td>
<td>0.052</td>
</tr>
</tbody>
</table>

We can see that, despite allowing for the estimation of location-specific intercepts, the average estimate of \(\eta_2\) is severely biased, while the estimate of \(\eta_1\) is only slightly
biased, suggesting that assumption 3 - that estimates are not susceptible to spatial con-
founding - does not hold. In other words, in the presence of unmeasured spatial con-
founding, even if we introduce into the model a county-specific random intercept, the 
estimate of the local effect can be severely biased.

Spatial and Global Temporal Confounding

In this section, we assume there exists both a spatial confounder, $U^c$, and a "global" 
temporal confounder, $U_t$. Outcome data is generated by:

$$
\log E(Y_{ct}) = \log(N_{ct}) + \delta_0 c + \delta_1 PM_{ct} + \delta_2 U^c + \delta_3 U_t,
$$

(2.6)

where $\delta_0 = -8.22$ for all $c$, $\delta_1 = 0.009$, $\delta_2 = -0.15$, and $\delta_3 = 0.15$. Confounders $U^c$ and $U_t$ are generated such that $\text{Corr}(U^c, PM^c) \approx 0.25$, and $\text{Corr}(U^t, PM^t) \approx 0.3$. Outcome data is 
again modeled via Model 2.3, again allowing for the estimation of location-specific 
intercepts, $\eta_0^c$. Results are summarized in Table 2.4 below:

Table 2.4: Performance of Model 2.3 Under the Assumption of Spatial and Global-scale 
Temporal Confounding: $\eta_1$ is the global parameter and $\eta_2$ is the local parameter.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Avg. Estimate</th>
<th>Avg. SE</th>
<th>Avg. p-value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\eta_1$</td>
<td>$6.83 \times 10^{-2}$</td>
<td>$7.40 \times 10^{-3}$</td>
<td>$&lt; 0.001$</td>
</tr>
<tr>
<td>$\eta_2$</td>
<td>$-6.09 \times 10^{-3}$</td>
<td>$3.04 \times 10^{-3}$</td>
<td>$0.054$</td>
</tr>
</tbody>
</table>

Results for the local term, $\eta_2$, are very similar to the previous case with only spatial 
confounding, which is to be expected since the local and global PM$_{2.5}$ terms are orthogo-
nal. We also observe that the global term, $\eta_1$, becomes inflated due to the global temporal 
confounder, as in the earlier simulation with only temporal confounding at the global 
level. Thus, in the case of global temporal confounding together with spatial confound-
ing, we observe that both the local and global terms can be quite biased. It is also possible 
in this situation, since the local and global terms are each affected separately by the spa-
tial and global temporal confounding, that both estimates could similar in magnitude but both be biased as a result of different sources of confounding.

**Spatio-temporal Confounding**

Now, suppose instead that confounding takes place at the local level and varies with time. Specifically, we generate $U_t^c$ to be correlated with $PM_t^c$ ($\text{Corr}(PM_t^c, U_t^c) \approx 0.25$) and generate outcome data via the following model:

$$\log E(Y_t^c) = \log(N_t^c) + \delta_0^c + \delta_1^c PM_t^c + \delta_2^c U_t^c,$$

(2.7)

again with $\delta_1 = 0.009$, $\delta_2 = 0.15$, and $\delta_0 = -7.35$ for all $c$. Analyzing this data under Model 2.3 allowing for the estimation of location-specific intercepts yields the following results (Table 2.5):

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Avg. Estimate</th>
<th>Avg. SE</th>
<th>Avg. p-value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\eta_1$</td>
<td>$3.27 \times 10^{-2}$</td>
<td>$7.86 \times 10^{-3}$</td>
<td>0.002</td>
</tr>
<tr>
<td>$\eta_2$</td>
<td>$2.99 \times 10^{-2}$</td>
<td>$1.46 \times 10^{-3}$</td>
<td>&lt; 0.001</td>
</tr>
</tbody>
</table>

In this instance, we observe that $\eta_1 \approx \eta_2$. Because of this, however, we would incorrectly assume that the estimates are not confounded, though they are, in fact, biased upward - both more than $3 \times$ higher than the truth, 0.009.

### 2.3.2 Size of the Window for Averaging Monthly Air Pollution

**Two-month Rolling Mean vs 12-month Rolling Mean**

In this section, we test the implications of assumption 4 being incorrect. Recall that assumption 4 assumes that mortality at time $t$ is associated with the average $PM_{2.5}$ over
the past 12 months. First, we investigate what happens if the true causal relationship between PM$_{2.5}$ and mortality only exists at, say, a two-month window as opposed to the 12-month window assumed in Janes et al., 2007 and Greven et al., 2011.

Consider, again, outcome data generated via Model 2.1 with no confounding and with $\delta_0$ and $\delta_1$ as described above. However, we generate that outcome data with $PM_t^c = (PM_{t,raw}^c + PM_{t-1,raw}^c)/2$, where $PM_{t,raw}^c$ is the raw, observed PM$_{2.5}$ level in county $c$ at time $t$, not averaged over any previous or future months’ values. We then model this outcome data using Model 2.3, but with $PM_t^c = \frac{1}{12}\sum_{i=0}^{11} PM_{t-i,raw}^c$, as in Janes et al., 2007 and Greven et al., 2011. Results are given in Table 2.6 below:

Table 2.6: Performance of Model 2.3 Under the Assumption of a Mis-specified Rolling Mean: $\eta_1$ is the global parameter and $\eta_2$ is the local parameter.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Avg. Estimate</th>
<th>Avg. SE</th>
<th>Avg. p-value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\eta_1$</td>
<td>$9.21 \times 10^{-3}$</td>
<td>$5.95 \times 10^{-4}$</td>
<td>$&lt; 0.001$</td>
</tr>
<tr>
<td>$\eta_2$</td>
<td>$8.82 \times 10^{-3}$</td>
<td>$2.55 \times 10^{-4}$</td>
<td>$&lt; 0.001$</td>
</tr>
</tbody>
</table>

Surprisingly, the mis-specified $PM_t^c$ that incorporates information from ten extra, uninformative months actually performs quite well, and $\eta_1$ and $\eta_2$ are indeed nearly the same and very near the truth of 0.009. As in the previous section, the estimate of the local term, $\eta_2$, was very robust to the inclusion of a “global” confounder, and remained unbiased. Thus, it appears that mis-specifying the length of the rolling mean is not terribly serious offense with regards to accurately estimating the regression coefficients.

Generating Data with a Distributed Lag

Suppose now that the association between PM$_{2.5}$ and mortality is best captured by a distributed lag model:

$$\logE(Y_t^c) = \log(N_t^c) + \delta_0^c + \sum_{l=0}^{q} \delta_l^c PM_{t-l}^c,$$  \hspace{1cm} (2.8)

where $q$ is the maximum lag we will consider and $l$ is the amount of lag, ranging from 0
to $q$. In other words, we assume not only that pollution at time $t$ affects mortality at time $t$, but also that pollution levels at times $t-1, t-2, \ldots, t-q$ impact mortality at time $t$.

Model 2.8 above is known as an *unconstrained* distributed lag model - one simply calculates the lagged values of the exposure and plugs them directly into the regression. If the successive values of the exposure are highly correlated, however, estimates of the the $\delta_i$’s will be very unstable. To overcome this, it’s useful to constrain the $\delta_i$’s to increase efficiency of the estimated lag parameters [Schwartz (2000)]. The most popular approach for constraining the regression coefficients is that of Almon, 1965, where the shape of the distributed lag (see figure below for an example) is fit by some polynomial function of degree $p$. Alternative choices include constraining the shape of the distributed lag with a piecewise natural cubic spline [Corradi and Gambetta, 1976; Zanobetti et al., 2000], B-splines of an arbitrary degree, or simple moving averages (as was done in Janes et al. (2007) and Greven et al. (2011)), among others [Gasparrini et al. (2010)].

Now, let’s suppose that the relationship between PM$_{2.5}$ and the relative risk (RR) of mortality is described by Figure 2.1. Here, we see some initial mortality displacement, or "harvesting" [Schwartz (2001)], followed by a (only partially pictured) sustained but modest long-term increase in the RR of mortality after around 13 months.

We generated outcome data under Model 2.8 so that the relationship between PM$_{2.5}$ and mortality is described by Figure 2.1, with $\delta_0$ constant across all $c$; we then fit that data under Model 2.3. Results are summarized below:

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Avg. Estimate</th>
<th>Avg. SE</th>
<th>Avg. p-value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\eta_1$</td>
<td>$6.93 \times 10^{-3}$</td>
<td>$2.74 \times 10^{-3}$</td>
<td>0.066</td>
</tr>
<tr>
<td>$\eta_2$</td>
<td>$3.71 \times 10^{-4}$</td>
<td>$2.76 \times 10^{-4}$</td>
<td>0.278</td>
</tr>
</tbody>
</table>

In this simulation, we observe $\eta_1 >> \eta_2$ (more than 18× greater). However, there is no confounding under this simulation, only a distributed lag where the relationship is given by that of Figure 2.1. Model 2.3 does relatively well in capturing the overall
Figure 2.1: **Example of Distributed Lag Relationship and Corresponding Cumulative Distributed Lag**: Plots of the relative risk of mortality by lag (a) and cumulative relative risk of mortality by lag (b).
Figure 2.1 (Continued)

(a) Relative risk for a 10µg/m³ increase in PM$_{2.5}$ by lag

(b) Cumulative relative risk for a 10µg/m³ increase in PM$_{2.5}$ by lag
RR over the entire 15-month lag (estimated, on average, to be $6.36 \times 10^{-4}$), but it is unable to tell us anything about the large bump in the RR of mortality that exists out until just after 5 months. Thus, if the true relationship between PM$_{2.5}$ and mortality over time is given by a similar distributed lag, the model specified by Janes et al., 2007 - and the accompanying assumptions for that model - would lead to a conclusion that the estimates are confounded, and that, on average, the local effect estimate is not statistically significant. The model would also fail to identify any bumps in mortality that are a function of mortality displacement over the duration of the lag window.

### 2.4 Extensions to Greven et al

In Greven et al., 2011, the authors begin with individual-level data, and wish to fit the proportional hazards model:

$$h^c(a,t) = h^c(a) \exp(x^c_t \beta),$$

where $h^c(a,t)$ denotes the hazard of dying at age $a$ and time $t$ for location $c$, $h^c(a)$ is a location-specific baseline hazard, and $x^c_t$ is average PM$_{2.5}$ exposure for county $c$ at time $t$ as described above. Age $a$ takes on integer values from 65 to 89; subjects age 90 or older are pooled into the same age group, $I(a \geq 90)$. Due to computational constraints given the size of the data set (18.2 million individuals across 814 different locations), the authors instead opt to fit the log-linear regression model:

$$\log\text{E}(Y^c_{at}) = \log(N^c_{at}) + \log(h^c(a)) + x^c_t \beta,$$  \hspace{1cm} (2.9)

which is equivalent to the originally proposed survival model, under a piecewise exponential assumption, with regard to likelihood-based inference [Holford (1980);
Laird and Olivier (1981). From Eq. 2.9, the authors then propose a model where $x_i^c$ is decomposed:

$$
\log E(Y_{a,t}^c) = \log(N_{a,t}^c) + \log(h^c(a)) + (x_i^c - \bar{x}_t - \bar{x}^c + \bar{x})\beta_1 + (\bar{x}_t - \bar{x})\beta_2,
$$

(2.10)

where the goal is to, as in Janes et al., 2007, identify unmeasured confounding via large differences between the estimates of $\beta_1$ and $\beta_2$. Estimating the parameters in Model 2.10 directly is computationally demanding, as there are still roughly 1.4 million observations across all locations and times combined, and there is a need to directly estimate the log-hazard $\log(h^c(a))$ for all 814 locations, $c$, separately to control for spatial confounding. Thus, the model is fitted using a backfitting algorithm [Buja et al. (1989)], which iterates between Step 1: estimating the PM$_{2.5}$ effect for all locations - $\beta_1$ and $\beta_2$ - including the previous iteration’s estimated hazard as an offset, and Step 2: separately estimating the log-hazard function for each location with $(x_i^c - \bar{x}_t - \bar{x}^c + \bar{x})\beta_1 + (\bar{x}_t - \bar{x})\beta_2$ as an offset.

Model 2.10 is very similar to Model 2.3; all of the simulation results above for the model in Janes et al. apply to this model except for one: Because a log-hazard function is estimated separately for each location via the backfitting algorithm, the location-specific hazard functions eliminate all purely spatial variation, which means that the estimate of $\beta_1$ can not be confounded by variables that vary only across locations. This approach is similar to fitting a separate model for each location, $c$, and then pooling the $\beta_1^c$ estimates across all locations; clearly no location-specific variables can be identified in that case because they would be absorbed into the intercept term since they are constant over time.

Consider the following – for any fixed time point, $t = T$, Model 2.10 is given by:

$$
\log E(Y_{a,t=T}^c) = \log(N_{a,t=T}^c) + \log(h^c(a)) + (x_i^c - \bar{x}_{t=T} - \bar{x}^c + \bar{x})\beta_1 + (\bar{x}_{t=T} - \bar{x})\beta_2.
$$

(2.11)

Now, $\bar{x}_{t=T}$ and $\bar{x}$ are constant across $c$. Thus, Eq. 2.11 can be rewritten as:
\[
\log E(Y_{a,t=T}^c) = \log(N_{a,t=T}^c) + \log(h^c(a)) + (x_{t=T}^c - \bar{x}^c - \Delta \bar{x}_{t=T}) \beta_1.
\] (2.12)

However, this model contains two terms that are constant with respect to \( c \) – the location specific indicator, \( \log(h^c(a)) \), and, because \( t \) is fixed at \( t = T \), \( (x_{t=T}^c - \bar{x}^c - \Delta \bar{x}_{t=T}) \) – which means \( \beta_1 \) is not identifiable. Thus, \( \beta_1 \) is only estimable via temporal variations, which means that it is not susceptible to bias via purely spatial confounders. Therefore, the results from the "spatial confounding" and "spatio-temporal confounding" sections above do not apply to the Greven et al., 2011 model.

For some confounder \( U_t^c \) to bias the local effect \( \beta_1 \), it would have to be associated with county-specific deviations in both \( \text{PM}_{t}^c \) and mortality from each of their respective national trends. An example would be if communities which showed larger decreases in \( \text{PM}_{2.5} \) than the national average also consistently showed larger decreases in smoking rates than the national average, and vice versa [Greven et al., 2011]. While possible, this type of confounding is certainly less likely than variables trending in a similar fashion on the national level, which is why these analyses focus more on the local effect estimates.

Another key distinction to make between the two models is the decomposition of \( \text{PM}_{t}^c \) in each model. In Janes et al. (2007), the modeling approach decomposes the exposure \( x_t^c \) into \( (x_t^c - \bar{x}_t) \) and \( (\bar{x}_t - \bar{x}) \). In Greven et al., the exposure \( x_t^c \) is decomposed into \( [(x_t^c - \bar{x}_t) - (\bar{x}^c - \bar{x})], (\bar{x}_t - \bar{x}), \) and \( (\bar{x}^c - \bar{x}) \), where \( (\bar{x}^c - \bar{x}) \) gets absorbed into the location-specific hazard. Interestingly, while the "local" terms in each model should have similar interpretations [Greven et al., 2011], it appears that they do not. For the data used by Greven and colleagues, we calculated both exposure decompositions - call \( (x_t^c - \bar{x}_t) \equiv x_{J,\text{local}} \) and call \( [(x_t^c - \bar{x}_t) - (\bar{x}^c - \bar{x})] \equiv x_{G,\text{local}} \). \( \text{Corr}(x_{J,\text{local}}, x_{G,\text{local}}) = 0.27 \) and \( \text{Corr}(x_{G,\text{local}}, \text{PM}_{t}^c) = 0.26 \), while \( \text{Corr}(x_{J,\text{local}}, \text{PM}_{t}^c) = 0.98 \). Clearly, the local term in the Janes decomposition is more representative of the raw \( \text{PM}_{2.5} \) levels that we want to make inference about. Also consider the Table 2.8 below, in which we present the results for our most basic simulation under no confounding, but using the Greven decomposition instead of the Janes decomposition.
Table 2.8: **Performance of Model 2.10 Under no Confounding**: $\beta_2$ is the global parameter and $\beta_1$ is the local parameter.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Avg. Estimate</th>
<th>Avg. SE</th>
<th>Avg. p-value</th>
</tr>
</thead>
<tbody>
<tr>
<td>$\beta_2$</td>
<td>$9.29 \times 10^{-3}$</td>
<td>$6.71 \times 10^{-3}$</td>
<td>0.284</td>
</tr>
<tr>
<td>$\beta_1$</td>
<td>$8.72 \times 10^{-3}$</td>
<td>$4.95 \times 10^{-3}$</td>
<td>0.188</td>
</tr>
</tbody>
</table>

Here, we see that while the local estimate is generally unbiased for the true effect of 0.009, it is not nearly as precise as the estimate obtained using the Janes decomposition. In fact on average, neither the local nor the global term in this decomposition is statistically significant - and this is absent any confounding at all! Thus, we propose an approach using the Janes decomposition but with the modeling approach of Greven to reanalyze the data from Greven et al., 2011. Additionally, because our parameter of interest - the coefficient on the local exposure term - is estimated solely via temporal variations, we propose the inclusion of a distributed lag for the local exposure to more precisely determine how and when longer-term PM$_{2.5}$ exposure can impact mortality.

2.5 Methods

2.5.1 Statistical Approach

Due to the large number of individuals in the data set (described briefly in the previous section, and in slightly more detail in the next section), fitting an individual-level model is not feasible. Thus, the data was aggregated to the zip code level, pooling the number of individuals and death counts for each zip code, enabling us to fit:

$$\log \text{E}(Y_{at}^c) = \log(N_{at}^c) + \log(h^c(a)) + (x_t^c - \bar{x}_t)\beta_1 + (\bar{x}_t - \bar{x})\beta_2,$$

(2.13)

where $\bar{x}_t$ denotes the national trend in annual average PM$_{2.5}$, calculated as the fitted values of a linear regression with PM$_t^c$ as the outcome and a smooth function of time with 16 degrees of freedom as the predictor [Janes et al., 2007]. In this data set, the
correlation between \((x_i^c - \bar{x}_t)\) and \((\bar{x}_t - \bar{x})\) is less than \(10^{-15}\), implying that the terms are essentially orthogonal. Therefore, potential confounders trending at the national-level cannot bias the estimate of \(\beta_1\). While it is possible for \(\beta_1\) to be confounded by local trends, this - as we discussed in the previous section - is less likely. Because \(\beta_2\) is likely to be confounded, and because we believe it is less likely for \(\beta_1\) to be confounded, we focus our attention primarily on the estimate of \(\beta_1\).

Further, it is reasonable to believe that the current month’s PM\(_{2.5}\) exposure is associated not only with the current month’s mortality, but that it may be associated with the mortality rate in subsequent months as well. To account for this, we impose a lag on \((x_i^c - \bar{x}_t)\). Call \((x_i^c - \bar{x}_t) \equiv x_{t,\text{local}}^c\); then the model we fit is given by:

\[
\log E(Y_{at}^c) = \log(N_{at}^c) + \log(h^c(a)) + \sum_{l=0}^{q} \eta_l x_{t-l,\text{local}}^c + (\bar{x}_t - \bar{x}) \gamma. \tag{2.14}
\]

Because lagged values of the exposure \(x_{t-l,\text{local}}^c\) will be highly correlated with one another, directly estimating the \(\eta_l\) will be difficult. To overcome this, we assume the shape of the distributed lag is given by some smooth function, which we estimate via piecewise natural cubic splines [Corradi and Gambetta, 1976; Zanobetti et al., 2000]. Because previous work has suggested that the effects of long-term exposure to PM\(_{2.5}\) are primarily felt within 0 to 2 years [Schwartz et al. (2008)], we specified a lag of \(q = 20\) months. Additionally, because successive monthly PM\(_{2.5}\) levels are so highly correlated and because we want to avoid an unrealistically wiggly function of the \(\eta_l\), we only place internal knots at \(l = (5, 10, 15)\). Further, note that because we believe the estimate for the global term will be biased, we do not impose a lag on that term since the estimates of the lagged "global" effects will also likely be biased.

In Model 2.14 we estimate the log-hazard, \(\log(h^c(a))\), separately for each location, allowing us to eliminate spatial variability from the problem and thus eliminate the possibility of confounding due to factors that vary only across locations. Because this greatly increases the dimensionality of the problem, however, we estimate the parameters in
Model 2.14 via a backfitting algorithm \cite{Greven2011, Buja1989}. The algorithm consists of two steps at each iteration, \( j \) - the first, in which the parameters \( \eta_l \) and \( \gamma \) are estimated given the previous iteration’s log-hazard, \( \log(\mathcal{h}(a))^{(j-1)} \), and the log of the risk set, \( \log(N^c_{at}) \), as an offset; and the second, in which the location-specific hazards are estimated separately for each location with \( \log(N^c_{at}) + \sum_{l=0}^{q} \eta_l^{(j)} x_{t-l,\text{local}} + (\bar{x}_t - \bar{x}) \gamma^{(j)} \) included as the offset. We run the algorithm until a stopping criteria is reached; here, we stop the algorithm if the \( l2 \) norm of the difference between the current iteration’s parameter estimates and the previous iteration’s parameter estimates is less than \( 10^{-6} \). Once convergence is achieved, conclude with step 1 one last time.

2.6 Results

The dataset used in this study is identical to that used in \cite{Greven2011}. Specifically, our data consists of monthly ambient \( \text{PM}_{2.5} \) measures linked with Medicare mortality data for the period 2000 - 2006. \( \text{PM}_{2.5} \) data was obtained from the EPA monitoring network and is from 814 monitor locations across the continental United States, chosen solely on the basis of availability. Each of the 814 locations has \( \text{PM}_{2.5} \) readings for at least four years, where each of the four years includes data from at least 10 months. Long-term \( \text{PM}_{2.5} \) exposure in month \( t \) is defined as the average exposure over the previous 12 months up to and including \( t \).

Air pollution data was linked to Medicare mortality data as follows: The same monitor-level reading was assigned to all Medicare enrollees residing in a zip code whose geographical centroid is within a 6 mile radius of the monitor. The Medicare data consists of time of death, precise up to the month, as well as demographic data - age, gender, and race. The study population consists of 18.2 million Medicare enrollees and 3.2 million deaths over the entire period 2000 - 2006. More information can be found about this data in \cite{Greven2011} and at \url{http://www.resdac.umn.edu/Medicare}.

The estimated lagged RR of local monthly \( \text{PM}_{2.5} \) exposure on mortality is given by
Figure 2.2 below. The local relative risk (RR) associated with a $10\mu g/m^3$ increase in PM$_{2.5}$ does not drop to zero until just before 5 months, though the only lag that is statistically significantly different from zero is the 2-month lag. The cumulative RR of a $10\mu g/m^3$ increase in PM$_{2.5}$ over the entire 20 month lag, however, is 1.055, CI = (1.052, 1.059); this corresponds to a log-RR of 0.0540($\pm$0.0018). Consistent with previous results under this type of model specification, the estimate for the global term is much larger. Here, the log-RR associated with a $10\mu g/m^3$ increase in PM$_{2.5}$ is 0.3780($\pm$0.0096), very comparable to the original estimate of 0.4313($\pm$0.0084) reported in Greven et al., 2011.

Note also that these results were not highly sensitive to different specifications of the knots in the distributed lag. As a check, we re-estimated the cumulative RR over the entire $q = 20$ month lag with only two internal knots at $l = (6.66, 13.33)$. The shape of the distributed lag curve was very similar to that observed in Figure 2.2, and the estimated cumulative RR was 1.054, CI = (1.051, 1.058). Even completely doing away with the lag did not do much to change the estimated RR. That is, we used Model 2.13 to estimate the local effect, $\beta_1$, and found that for a $10\mu g/m^3$ increase in PM$_{2.5}$, the estimated RR of mortality was 1.052, CI = (1.049, 1.056), a very slight decrease from the estimates obtained using the distributed lag models.

We also fit models that additionally controlled for local seasonality by including in Model 2.14 location-specific indicators for month. However the estimated relative risks were not impacted at all by the inclusion of these terms, suggesting that our estimates of the local association between PM$_{2.5}$ and mortality are not biased due to local seasonality issues.
Figure 2.2: **Plot of the Estimated RR of Mortality Associated with a 10µg/m³ Increase in PM$_{2.5}$**: Here we see the estimated RR of mortality associated with a 10µg/m³ increase in PM$_{2.5}$ plotted as a function of the lagged PM$_{2.5}$ exposure. The association fades relatively quickly, suggesting that a lag shorter 20 months is likely to be sufficient.
Figure 2.2 (Continued)
Another concern in fitting this model is that the local and global terms are approximately orthogonal to each other. Consider Table 2.9 below, which is the model based correlation matrix corresponding to Model 2.14. Focusing on only the second column in Table 2.9 we see that the largest correlation between a "Local PM" cubic spline basis vector and the "Global PM" variable is 0.033. All other spline bases have a correlation with Global PM less than 0.01. Table 2.10 shows the model-based correlation matrix corresponding to Model 2.13. Here, the correlation between the local and global PM_{2.5} variables is -0.019. By comparison, the model-based correlation between the local and global PM_{2.5} variables in Greven et al. (2011) is -0.017.
Table 2.9: **Model-based Correlation Matrix Corresponding to Model 2.14:** The five "Local PM" variables correspond to the five vectors that define the location of the knots for the piecewise cubic spline used to implement the distributed lag in Model 2.14.

<table>
<thead>
<tr>
<th></th>
<th>Intercept</th>
<th>Global PM</th>
<th>Local PM 1</th>
<th>Local PM 2</th>
<th>Local PM 3</th>
<th>Local PM 4</th>
<th>Local PM 5</th>
</tr>
</thead>
<tbody>
<tr>
<td>Intercept</td>
<td>1</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Global PM</td>
<td>-0.015</td>
<td>1</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Local PM Basis 1</td>
<td>0.002</td>
<td>0.004</td>
<td>1</td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Local PM Basis 2</td>
<td>-0.001</td>
<td>0.002</td>
<td>-0.827</td>
<td>1</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Local PM Basis 3</td>
<td>0.003</td>
<td>-0.003</td>
<td>0.659</td>
<td>-0.871</td>
<td>1</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Local PM Basis 4</td>
<td>-0.007</td>
<td>-0.007</td>
<td>-0.707</td>
<td>0.309</td>
<td>-0.425</td>
<td>1</td>
<td></td>
</tr>
<tr>
<td>Local PM Basis 5</td>
<td>0.002</td>
<td>0.033</td>
<td>0.088</td>
<td>0.343</td>
<td>-0.608</td>
<td>-0.172</td>
<td>1</td>
</tr>
</tbody>
</table>
Table 2.10: **Model-based Correlation Matrix Corresponding to Model 2.13:** We observe virtually no correlation between the local and global PM$_{2.5}$ variables in our non-lagged model, (2.13)

<table>
<thead>
<tr>
<th></th>
<th>Global PM</th>
<th>Local PM</th>
</tr>
</thead>
<tbody>
<tr>
<td>Global PM</td>
<td>1.000</td>
<td>-0.019</td>
</tr>
<tr>
<td>Local PM</td>
<td>-0.019</td>
<td>1.000</td>
</tr>
</tbody>
</table>

2.7 Discussion

In this work, we investigated why recent models proposed by Janes et al. (2007) and Greven et al. (2011) that attempt to adjust for and identify confounding in air pollution studies by decomposing the exposure variable into two approximately orthogonal pieces of information - a local and a global exposure term - did not detect any association between PM$_{2.5}$ and mortality at the local level in their studies. We conducted a number of simulation studies on the model proposed by Janes et al. (2007) to examine which, if any, of their modeling assumptions were violated and what the implications of those violations were. We identified that the local PM$_{2.5}$ effect estimates were in fact still susceptible to residual spatial confounding, despite the underlying modeling assumption that they would not be due to the inclusion of location-specific random intercepts. We also identified that if the true exposure response relationship is given by a lagged relationship, then the association between PM$_{2.5}$ and mortality could be severely biased, both globally and locally.

We did not directly test the modeling assumptions in the Greven framework, but rather, using the knowledge we gained through the simulation results pertaining to the Janes model, we were able to identify what particular scenarios could cause biased estimates in the Greven model. We saw that, generally, all of the modeling assumptions in the Greven paper did hold true, and its main advantage over the model described in Janes et al. (2007) is that the Greven model completely eliminates spatial variation (and thus the possibility of confounding due to spatially varying covariates) by estimating...
location-specific hazard functions separately for each location. However, the estimates in the Greven model could still be biased if the true exposure response relationship is given by a lagged relationship. Additionally, while the decomposition in the Greven model does create two approximately orthogonal exposures - one local and one global - the local variable in the Greven model performed more poorly in our simulations with regards to bias and MSE than did the local exposure term specified by Janes and colleagues. It is also a more difficult quantity to interpret given the more complicated decomposition. The claim made by Greven et al. (2011) is that their decomposition is such that the approximate orthogonality of the local and global exposure terms is more closely orthogonal than the terms in the Janes decomposition. In our model, we found that this is in fact true, though not by as much as one would hope. The model-based correlation between the local and global terms in Greven model is -0.017, while for the Janes decomposition in the Greven model framework that correlation is -0.019.

However, this work should not be interpreted as a criticism of the Janes and Greven papers, but rather as a fusion of the two. Indeed, both approaches have their strengths and weaknesses; here, we ultimately combined those two approaches into one, attempting to keep only the strong points of each. In doing so, we constructed a model that: 1) effectively controls for spatial confounding by eliminating all spatial variation, and thus does not allow the parameter estimates to be informed by underlying differences among locations; 2) decomposes the exposure estimate into two orthogonal pieces of information - a "local" exposure and a "global" exposure - as a means to adjust for and identify residual confounding; 3) can identify an exposure-response relationship for lagged values of the exposure; and 4) is not sensitive to adjustment for local seasonality.

In this paper, we estimated that a $10\mu g/m^3$ increase in PM$_{2.5}$ was statistically significantly associated (across all models) with anywhere between a 5.2% and 5.5% increase in the risk of mortality. The estimates were consistent across lagged and non-lagged models, as well as for different specifications of the lagged models. Generally speaking, these estimates are largely consistent with those estimated in previous studies examining the
impact of long-term PM$_{2.5}$ exposure on mortality {Pope and Dockery (2006)}.

What is interesting to consider is why Greven et al. (2011) and Janes et al. (2007) did not observe any association between PM$_{2.5}$ and mortality at the local level. There are many possible reasons. First, consider the Janes study. We showed via simulation that the modeling approach in Janes et al. (2007) was susceptible to spatial confounding. In previous work that exploited purely spatial information, we have seen that the PM$_{2.5}$ effect on mortality is smaller in models that don’t adjust for other covariates than in models adjusting for key socioeconomic and demographic variables over a similar time period {Correia et al. (2013)}. Thus, it is possible that the estimates from the Janes study were simply biased downward as a result of residual confounding. It’s also possible that the span of the study 2000 - 2002 was not enough time to observe an association, and the study was simply underpowered due to the relatively little change in PM$_{2.5}$ levels over such a short period of time.

In the Greven study, we know that confounding due to location-specific variables is not possible. While confounding due to local trends is possible, that same confounding would also affect the estimates in our model - yet, we observe a positive and statistically significant association in this study, whereas the Greven analysis, using the same data used here, does not. Thus, we will assume that local confounding is also not the reason why no association was observed in the Greven analysis. This means that the only other plausible explanation would be the different exposure decomposition used in our study compared to the original analysis by Greven et al. (2011). In our simulation, we showed that the Greven decomposition suffers from a larger MSE than the Janes decomposition, and on average - absent confounding - the local estimate under the Greven decomposition was not statistically significant. Thus, it seems that by further orthogonalizing the local and global exposure variables, Greven and colleagues were left with a variable that was no longer as strong a predictor of the outcome as the simpler decomposition, while not gaining a substantial amount with respect to further orthogonalizing the local and global terms. Here, we revert to the original decomposition from Janes et al. (2007), which
still achieves approximate orthogonality of the local and global terms for the purposes of Model 2.13, and also which has a local term that is a stronger predictor of the association between PM$_{2.5}$ and mortality.
Exposure to Aircraft Noise and Hospital Admissions for Cardiovascular Diseases: A Large National Multi-Airport Population Cohort Study

Andrew W. Correia¹, Junenette L. Peters², Jonathan I. Levy², Steven Melly³, and Francesca Dominici¹

¹ Department of Biostatistics, Harvard University
² Department of Environmental Health, Boston University School of Public Health
³ Department of Environmental Health, Harvard School of Public Health
3.1 Introduction

Aircraft noise has been associated with physiological responses and psychological reactions (Bluhm and Eriksson (2011); Hatfield et al. (2001)), such as sleep disturbances, sleep-disordered breathing, nervousness, and annoyance (Hatfield et al. (2001); Rosenlund et al. (2001)); however, the relationship of aircraft noise to direct health effects is less well established. Recent literature, primarily from one multicenter European study, has provided growing evidence for a relationship between aircraft noise and hypertension outcomes, including incidence of hypertension (Eriksson et al. (2010)), self-reported hypertension (Rosenlund et al. (2001)), increased blood pressure (Haralabidis et al. (2008); Jarup et al. (2008); Haralabidis et al. (2011)), and antihypertensive medication use (Bluhm and Eriksson (2011); Greiser et al. (2007); Franssen et al. (2004); Floud et al. (2011)). This is supported by a broader literature which evaluated the cardiovascular effects of noise and found substantial evidence for biological plausibility and positive associations between noise and hypertension, myocardial infarction (MI), and ischemic heart disease (IHD) (Babisch and Kim (2011)). Potential biological mechanisms may include induced release of stress hormones (Ising and Kruppa (2004); Spreng (2000); Selander et al. (2009)) and indirect effects on sympathetic activity, which is associated with adverse metabolic outcomes (Selander et al. (2009); Grassi (2006b,a); Mancia et al. (2006)).

However, few studies of the relationship between aircraft noise and cardiovascular disease (CVD) have been conducted to date (Bluhm and Eriksson (2011)), in part because studies surrounding a small number of airports are not typically adequately powered. To our knowledge, only one study in Switzerland has examined CVD mortality, finding an association between airport noise and MI mortality (Huss et al. (2010)). No major study has been conducted to date to estimate the association between long-term exposure to aircraft noise and hospital admissions for cardiovascular outcomes. Appropriately characterizing this association requires sufficient number of airports with large surrounding populations, applying statistical methods that can combine findings across airports and account for potential confounders both at the individual and the area level.
In this study, we leverage the large and nationally representative United States (US) population of Medicare enrollees to evaluate the CVD implications of airport-related noise in the US. Specifically, this study aims to evaluate the relationship between average residential exposure to aircraft noise and hospital admission for cardiovascular-related diseases in the population \( \geq 65 \) years of age residing near airports in the contiguous US. Understanding the link between aircraft noise and CVD outcomes is important in characterizing the potential benefits of intervention strategies [Stansfeld and Crombie (2011)].

3.2 Methods

The cohort for this study was taken from 2009 US Medicare enrollees \( \geq 65 \) years of age. Information obtained for enrollees includes date of death and hospitalization records, which contain date of hospitalization, length of hospital stay, the associated International Classification of Diseases (ICD) primary and secondary diagnostic and procedure codes, and the costs billed to Medicare. Additional individual-level data include age, gender, race, and zip code of residence.

Cause-specific hospitalizations for five cardiovascular outcomes were considered based on ICD, Ninth Revision (ICD-9) codes for primary diagnosis: heart failure (HF) (ICD-9 428); heart rhythm disturbances (ICD-9 426 to 427); cerebrovascular events (ICD-9 430 to 438); IHD (ICD-9 410 to 414, 429); and peripheral vascular disease (ICD-9 440 to 448). A variable for total CVD admissions was calculated as the sum of these causes.

3.2.1 Noise Exposure Estimates

We used 2009 noise contours developed for 89 airports in the contiguous US. Noise contours were provided to us by the US Federal Aviation Administration (FAA) who, in turn, used the Integrated Noise Model (INM) version 7.0a [Federal Aviation Administration - Office of Environment and Energy (2007)]. Given our interest in characterizing noise on a continuous scale with high spatial resolution, the FAA ran the INM in a mode...
that estimates noise exposure for each census block centroid surrounding each airport out to a minimum of 45 dB. The noise descriptor used was Day-Night Sound Level (DNL), which adds a 10 dB "penalty" to nighttime (i.e., 2200-0700 hr) [Miedema et al. (2000)].

Medicare data provides residential information at the zip code level only. Therefore, we used the noise exposure measures in combination with 2010 US Census data on population counts, both at the census block level, to obtain aggregated measures of exposure to aviation-related noise at the zip code tabulation area (ZCTA) level. Specifically, to calculate the aggregated measures of noise exposure, we assumed that the study population is uniformly distributed within a census block. We then overlaid noise estimates by census block along with estimates of the population $\geq 65$ years of age by census block, based on U.S. Census 2010 Summary File 1 (SF1) Table P12. For ZCTAs that included census blocks below 45 dB, we assumed that those blocks were exposed to 45 dB. The ZCTAs for which no census blocks had noise estimates above 45 dB were omitted from the analysis. We then constructed a number of candidate exposure metrics for each ZCTA, but focused on two in particular: 1) population-weighted average noise among the census blocks within each ZCTA, where each census block was weighted by the age $\geq 65$ population, and 2) the 90th percentile noise exposure among the census blocks within each ZCTA that contain non-zero population age $\geq 65$.

More formally, for each ZCTA, we calculated the population-weighted noise exposure, $x_z$, as: $x_z = \frac{1}{\text{pop}_z} \sum_j p_j \times x_j$, where $j$ indexes the census blocks in ZCTA $z$, $p_j$ is the number of individuals age $\geq 65$ in census block $j$, $x_j$ is the estimated noise exposure at the centroid of census block $j$, and $\text{pop}_z$ is the total number of individuals age $\geq 65$ in ZCTA $z$. For blocks that were split by the 45 dB contour line, noise exposure was estimated as the population exposed to over 45 dB - estimated as the fraction of $p_j$ inside the contour line - multiplied by $x_j$, plus the estimated population outside of the contour line multiplied by 45 dB.
3.2.2 Statistical Methods

We estimate the effect of aircraft noise exposure on hospital admissions for all cardiovascular outcomes and for separate outcomes of cerebrovascular disease, IHD, and HF. Preliminary analyses indicated that heart rhythm disturbances and peripheral vascular disease were too infrequent to include as stand-alone outcomes.

Individual-level control variables included age (> 75 or ≤ 75), gender (male or female), and race (white [non-Hispanic] or non-white). We also used ZCTA-level Census 2000 data to characterize variables that might proxy for other potential confounders (% black, % Hispanic, % graduated high school, median household income), using a subset given high correlations among the variables. We also obtained ZCTA-level average yearly fine particulate matter (PM$_{2.5}$) and ozone levels from the US Environmental Protection Agency’s Air Quality System database where available.

For each ZCTA included into the analysis, we calculate the number of cause-specific admissions and the number of people at risk (Medicare enrollees) stratified by age/gender/race. Each ZCTA represented part of a cluster of other ZCTAs around one of the 89 airports. We then fit hierarchical Poisson models to data aggregated at the ZCTA level with airport-specific random intercepts and slopes. The models can be described in two stages. First, we specified a Poisson regression model for ZCTA-level counts to estimate risk of CVD admissions associated with exposure to aircraft noise separately for each airport, adjusted for individual-level and ZCTA-level confounders. Second, we combined information across airports and accounted for clustering by specifying airport-specific random effects. Our main analysis (combined CVD) was run in R (version 2.15.0) under a fully Bayesian approach, enabling us to estimate both airport-specific effects and overall fixed effects.

Specifically, we fit the following model:
\[
\log(E[Y^A_{z,s}]) = \log(N^A_{z,s}) + \beta_A^0 + \beta_A^1I(\text{age} > 75) + \beta_A^2I(\text{sex} = M) \\
+ \beta_A^3I(\text{race} = \text{nonwhite}) + \beta_A^4(x^A_z - \bar{x}) + \gamma^T W^A_z,
\]

(3.1)

where \(Y^A_{z,s}\) and \(N^A_{z,s}\) are the number of CVD hospitalizations and total population, respectively, for age/sex/race strata \(s\) in ZCTA \(z\) in airport \(A\); \(x^A_z\) is the noise exposure variable for ZCTA \(z\) in airport \(A\) (either population weighted noise or the 90th percentile of noise among the blocks in ZCTA \(z\)), and \(W^A_z\) is the vector of potentially confounding SES, demographic, or air quality variables for ZCTA \(z\) in airport \(A\).

Let \(\beta^A = (\beta_0^A, \beta_1^A, \beta_2^A, \beta_3^A, \beta_4^A)^T\); we specify our fully Bayesian approach as follows:

\[
\beta^A \sim \mathcal{N}_5(\theta, \Sigma),
\theta \sim \mathcal{N}_5(\mu_0, \Lambda_0),
\Sigma \sim \mathcal{IW}(\eta_0, S_0),
\gamma \propto 1,
\]

(3.2)

where \(\mathcal{N}_5(\alpha, V)\) denotes a 5-dimensional multivariate normal distribution with mean vector \(\alpha\) and covariance matrix \(V\), and \(\mathcal{IW}(\eta, W)\) denotes an inverse Wishart distribution with \(\eta\) degrees of freedom and scale matrix \(W\). In specifying our priors by Eq. 3.2, we are able to take advantage of the conjugacy of the normal and inverse Wishart distributions and compute our posteriors for \(\theta\) and \(\Sigma\) using a standard Gibbs sampling algorithm [Casella and George (1992)]. Indeed, it is straightforward to show that full conditional posterior distributions for \(\theta\) and \(\Sigma\) are given by:

\[
P(\theta \mid \cdot) \sim \mathcal{N}_5\left((\Lambda_0^{-1} + n_A \Sigma^{-1})^{-1}(\Lambda_0^{-1} \mu_0 + n_A \Sigma^{-1} \bar{\beta}^A), (\Lambda_0^{-1} + n_A \Sigma^{-1})^{-1}\right),
\]

\[
P(\Sigma \mid \cdot) \sim \mathcal{IW}\left(\eta_0 + n_A, (S_0 + [\beta^A_{\text{mat}} - \theta_{\text{mat}}]^T[\beta^A_{\text{mat}} - \theta_{\text{mat}}])^{-1}\right),
\]

(3.3)
where \( n_A \) is the total number of airports in our dataset (89), \( \beta_{mat}^A \) is an \( n_A \times p \) matrix, where each row corresponds to an airport-specific vector of parameter estimates \( \beta^A \), \( \theta_{mat} \) is also an \( n_A \times p \) matrix, where each row is equal to \( \theta \), and \( p = \text{Length}(\theta) = 5 \).

Because the location-specific effects, \( \beta^A \), and fixed effects, \( \gamma \), do not have conjugate priors relative to the Poisson likelihood implied by Eq. 3.1, however, we cannot derive a closed form for the full conditional posterior distributions of \( \beta^A \) and \( \gamma \). Thus, we include in our Gibbs sampler a Metropolis step in order to estimate the posterior distributions of each \( \beta^A \) and the \( \gamma \).

Selecting appropriate values for \( \mu_0 \), \( \Lambda_0 \), and \( S_0 \) can be a difficult problem, particularly in the absence of explicit prior data (Hoff (2009)). However, using unit information priors (Kass and Wasserman (1995)), a type of weakly informative prior, provides a way of obtaining reasonable estimates for these hyperparameters. To obtain estimates of \( \mu_0 \) and \( \Lambda_0 \), the population mean and covariance, respectively, of the \( \beta^A \)'s, we follow the strategy outlined in Hoff (2009) and fit Eq. 3.1 separately for each airport with at least 20 surrounding ZCTAs. This gives us 42 different airport-specific MLE estimates, \( \tilde{\beta}_a \). The unit information prior for \( \theta \), then, would be given by the multivariate normal distribution described in Eq. 3.2 where \( \mu_0 = \frac{1}{42} \sum_a \tilde{\beta}_a \) and \( \Lambda_0 \) set equal to the sample covariance of the \( \tilde{\beta}_a \). We also set \( S_0 \) equal to the sample covariance matrix, and we choose \( \eta_0 = p + 2 \).

For each cardiovascular outcome (combined CVD hospitalizations, and separate sub-analyses for cerebrovascular disease, ischemic heart disease and heart failure hospitalizations), we constructed three hierarchical models (as in Eq. 3.1) for each of the two noise metrics (population-weighted noise exposure and 90th percentile of noise exposure). These three different models are characterized by which covariates enter the model along with noise exposure to control for potential confounding. Models 1 controlled for individual-level variables (age, gender, and race) only. Models 2 additionally controlled for ZCTA-level SES and demographic variables (% Hispanic and median household income), and Models 3 added pollution variables (PM\(_{2.5}\) and ozone) to Model 2. For Models 2 and 3, the ZCTA-level SES, demographic, and air pollution variables enter Eq. 3.1 as a
column the matrix $W^A_z$; for Model 1, $W^A_z = 0$. In the interest of computational time, the cause-specific analyses - that is, our sub-analyses for each of the single CVD hospitalization outcomes as opposed to our main outcome of interest, total CVD hospitalizations - were run using the glmer() function in the linear mixed effects models package (lme4) in R, which fits the hierarchical Poisson models (Eq. 3.1) in a frequentist framework by a Laplace approximation of the log-likelihood [Bates (2012)]. We note that overall effect-estimates, $\theta$, obtained using the lme4 package in R are nearly identical to those obtained via our fully Bayesian approach, though we opt for the fully Bayesian approach in our main analysis of total CVD hospitalizations as this allowed us to estimate not only the overall effect of noise exposure on CVD hospitalizations, but also to estimate the airport-specific effect estimates as well as their standard errors and credible intervals.

3.3 Results

There were totals of 2,218 ZCTAs (779 with PM$_{2.5}$ and ozone data) and 6,027,363 Medicare enrollees residing within the 45 dB contour level of the 89 airports. The number of ZCTAs within the 45 dB contour level ranged from seven to 107 across the airports. The number of Medicare enrollees in these ZCTAs ranged from 8,556 to 482,200 across the airports. Table 3.1 summarizes the population characteristics of this cohort, and Figure 1 provides a map presenting the 89 airports.

Results for the nationally aggregated relative risk of a CVD hospitalization for each one dB increase in population-weighted noise exposure and in 90$^{th}$ percentile of noise exposure are displayed in Figure 3.2. For the 90$^{th}$ percentile of noise exposure variable, controlling for age, gender, and race, an increase of one dB in the 90$^{th}$ percentile of noise within a ZCTA was associated with an increase of 0.29% (95% CI 0.08 to 0.49) in the relative risk of having a CVD hospitalization (Model 1). In Model 2, which additionally controls for ZCTA-level SES and demographic variables, the log-relative risk of having a CVD hospitalization was only marginally significant (relative risk 0.16% (95% CI -0.02 to 0.34)). In Model 3, adding pollution variables to Model 2, an increase in the 90$^{th}$ per-
Table 3.1: **Distribution of Zip Code Tabulation Area (ZCTA) Level Exposure for 2,218 ZCTAs and Risk Factor Data for Approximately Six Million Medicare Enrollees in 2009**: Values are the $25^{th}$, $50^{th}$ (Median), and $75^{th}$ percentiles for each variable across all ZCTAs. (*) 1165 ZCTAs with data on PM$_{2.5}$. (†) 779 ZCTAs with data on ozone - a proper subset of the 1165 ZCTAs with data on PM$_{2.5}$.

<table>
<thead>
<tr>
<th>Characteristics</th>
<th>25$^{th}$%</th>
<th>Median</th>
<th>75$^{th}$%</th>
</tr>
</thead>
<tbody>
<tr>
<td>% &gt; 75 years old (among population $\geq$ 65)</td>
<td>37.3</td>
<td>42.7</td>
<td>47.7</td>
</tr>
<tr>
<td>% Black</td>
<td>1.8</td>
<td>5.5</td>
<td>20.2</td>
</tr>
<tr>
<td>% Hispanic</td>
<td>2.1</td>
<td>6.2</td>
<td>19.8</td>
</tr>
<tr>
<td>Median household income (thou. $)</td>
<td>34.9</td>
<td>45.1</td>
<td>57.3</td>
</tr>
<tr>
<td>% graduated high school</td>
<td>72.8</td>
<td>82.9</td>
<td>90</td>
</tr>
<tr>
<td>PM$_{2.5}$ ($\mu g/m^3$)*</td>
<td>9.1</td>
<td>10.2</td>
<td>11.3</td>
</tr>
<tr>
<td>Ozone (ppm)†</td>
<td>0.022</td>
<td>0.025</td>
<td>0.028</td>
</tr>
<tr>
<td>Population-weighted noise (dB, DNL)</td>
<td>45.1</td>
<td>45.9</td>
<td>48.6</td>
</tr>
<tr>
<td>90th percentile of noise among populated census blocks (dB, DNL)</td>
<td>47.5</td>
<td>50.3</td>
<td>54.5</td>
</tr>
<tr>
<td>Hospital admission rate per 100,000 individuals</td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>Cerebrovascular events (stroke)</td>
<td>677.3</td>
<td>1093.4</td>
<td>2229.4</td>
</tr>
<tr>
<td>Ischemic heart disease</td>
<td>885.7</td>
<td>1429.8</td>
<td>2915.3</td>
</tr>
<tr>
<td>Heart failure</td>
<td>260.5</td>
<td>420.5</td>
<td>857.4</td>
</tr>
<tr>
<td>Heart rhythm disturbances</td>
<td>547.1</td>
<td>883.1</td>
<td>1800.6</td>
</tr>
<tr>
<td>Peripheral vascular disease</td>
<td>364.7</td>
<td>588.7</td>
<td>1200.4</td>
</tr>
</tbody>
</table>
Figure 3.1: **Map of the Locations of the 89 Airports in the Contiguous US Included in this Analysis.**
centile of noise of one dB was associated with an increase of 0.34% (95% CI 0.02 to 0.68) in the log-relative risk of having a CVD hospitalization. Airport-specific and aggregated relative risks (for Model 3) of having a CVD hospitalization per one dB increase in the 90th percentile of noise exposure are displayed in Figure 3.3.
Figure 3.2: Overall Estimates (averaged across the 89 airports) of the Relative Risk of Hospitalization for Cardiovascular Disease Associated with a One dB (DNL) Increase in Both Exposure Variables (population-weighted noise exposure and 90th percentile noise exposure) for Each of the Models: Model 1 controls for individual demographics (age, gender, and race); Model 2 additionally controls for zip-code level socioeconomic status and demographics (% Hispanic and median household income); Model 3 adds to Model 2 by also controlling for fine particulate matter and ozone levels.
Figure 3.2 (Continued)

![Graph showing percent increase in risk of CVD hospitalization for 1 dB increase in noise exposure. The graph compares models across different noise exposure metrics: population weighted noise exposure and 90th percentile noise exposure. The x-axis represents the noise exposure levels, and the y-axis represents the percent increase in risk. Three models are compared, labeled as Model 1, Model 2, and Model 3. Each model shows a different trend in the percent increase in risk.](image-url)
Figure 3.3: Airport-specific and Overall Estimates of the Relative Risk of Hospitalization for Cardiovascular Disease Associated with a One dB (DNL) Increase in the 90th Percentile Noise Exposure among Census Blocks within ZCTAs: This model controls for individual demographics (age, gender, and race), zip-code level socioeconomic status and demographics (% Hispanic and median household income), and average yearly fine particulate matter and ozone levels (Model 3). Airport-specific estimates are arranged from lowest to highest estimates.
Figure 3.3 (Continued)

Percent Increase in Risk of CVD Hospitalization for 1 dB Increase in Noise

Overall

Individual Airport Estimates
In contrast, for the population-weighted noise exposure, while there was an estimated 0.67% increase (95% CI 0.23% to 1.09%) in the overall relative risk of having a CVD hospitalization for a one dB increase in noise in Model 1, after controlling for SES, demographic, and pollution variables (Models 2 and 3), this association was no longer statistically significant. Figure 3.4 shows the airport-specific and aggregate results for Model 3 for population-weighted noise. The standard errors of the airport-specific estimates are generally larger than for the models using the 90th percentile of noise within a ZCTA, potentially due in part to the relatively limited variability of population-weighted noise across ZCTAs within the dataset (Table 3.1).
Figure 3.4: Airport-specific and Overall Estimates of the Relative Risk of Hospitalization for Cardiovascular Disease Associated with a One dB (DNL) Increase in Population-weighted Noise Exposure among Census Blocks within ZCTAs: This model controls for individual demographics (age, gender, and race), zip-code level socio-economic status and demographics (% Hispanic and median household income), and average yearly fine particulate matter and ozone levels (Model 3). Airport-specific estimates are arranged from lowest to highest estimates.
Percent Increase in Risk of CVD Hospitalization for 1 dB Increase in Noise

Overall

Individual Airport Estimates

Figure 3.4 (Continued)
Considering sub-categories of CVD outcomes, we observed generally consistent patterns among models. For example, in Model 1, an increase in the 90\textsuperscript{th} percentile of noise of one dB was associated with cerebrovascular disease and HF, with a marginal association for IHD. Relative risk estimates were similar across outcomes (Figure 3.5). For Model 2, relative risk estimates for all three outcomes declined in magnitude and lost statistical significance. Inclusion of pollution variables (Model 3) led to stable or increased relative risk estimates for all three outcomes, relative to Model 2. These estimates lacked statistical significance other than for IHD but were similar in magnitude to the estimates from Model 1. For the population-weighted noise exposure, a similar pattern was observed (Figure 3.5).
Figure 3.5: Airport-specific and Overall Estimates of the Relative Risk of Hospitalization for Cardiovascular Disease Associated with a One dB (DNL) Increase in Population-weighted Noise Exposure among Census Blocks within ZCTAs: This model controls for individual demographics (age, gender, and race), zip-code level socioeconomic status and demographics (% Hispanic and median household income), and average yearly fine particulate matter and ozone levels (Model 3). Airport-specific estimates are arranged from lowest to highest estimates.
Figure 3.5 (Continued)

Percent Increase in Risk of Hospitalization for 1 dB Increase in Noise

Population Weighted Noise Exposure

90th Percentile Noise Exposure

Cerebrovascular  IHD  HF  Cerebrovascular  IHD  HF

-1.5  -1.0  -0.5  0.0  0.5  1.0  1.5  2.0

M1  M2  M3

M1  M2  M3

M1  M2  M3

M1  M2  M3

M1  M2  M3

M1  M2  M3

M1  M2  M3

M1  M2  M3

M1  M2  M3
3.4 Sensitivity Analyses

The results outlined in the previous section suggesting a positive and statistically significant association between exposure to noise from airports and CVD hospitalizations among elderly US residents residing in ZCTAs surrounding airports could have a large impact on policy regarding noise mitigation strategies at and around airports in the US. Thus, we felt it was appropriate to perform a number of sensitivity analyses to be sure that the associations observed under Eq. 3.1 were robust to a number of modeling assumptions. Since we saw the strongest associations between noise and CVD hospitalizations using the 90\textsuperscript{th} percentile of noise variable, all models and sensitivity analyses discussed in the section will only consider the 90\textsuperscript{th} percentile noise variable as the exposure.

3.4.1 Residual Spatial Confounding

As always, a primary concern with any observational study is bias due to residual confounding \cite{Christenfeld2004, Greenland2001}. While we do our best to obtain information on potentially confounding SES and demographic variables from the US Census, the possibility for residual confounding due to some unmeasured covariate remains. Broadly speaking, there are two sources of variability in our dataset and thus two avenues for our effect estimates to be affected by residual confounding: 1) Within airport variation, and 2) Between airport variation. Within airport variability is characterized by variations in the covariates in Eq. 3.1 among the ZCTAs within a particular airport. Between airport variability is characterized by variations in the covariates across all of the airports in our study. Our first goal was to determine which of those two sources of variability contributed more to the estimated association between noise exposure and CVD hospitalizations in order to identify which sources of variation would most likely be responsible if our estimates were indeed biased due to confounding.

We began, as in the previous chapter, by decomposing our noise exposure variable in Eq. 3.1 into a "local" and "global" exposure term. Specifically, we recast Eq. 3.1 as:
\[
\log(E[Y^A_{z,s}]) = \log(N^A_{z,s}) + \beta^A_0 + \beta^A_1 I(\text{age} > 75) + \beta^A_2 I(\text{sex} = M) \\
+ \beta^A_3 I(\text{race} = \text{nonwhite}) + \beta^A_4 (x^A_{z,s} - \bar{x}^A) + \beta^A_5 (\bar{x}^A - \bar{x}) + \gamma^T W^A_{z,s},
\]

where the \(\beta^A_4\) estimate the noise-CVD relationship using within airport variability and \(\beta^A_5\) estimates the noise-CVD relationship using between airport variability. Under the covariate pattern specified by Model 3 (controlling for SES and air pollution variables), we estimated the overall effect, \(\beta^A_4 = \theta_4\) of Eq. 3.1 to be 0.0034 with a p-value of 0.04. Under that same covariate pattern in Eq. 3.4, we estimate \(\beta^A_4 = \theta_4 = 0.0033 (p = 0.046)\) and \(\beta^A_5 = -0.0020 (p = 0.904)\), demonstrating that the overall noise effect estimate in Eq. 3.1, \(\theta_4\), is largely informed by "local" within airport variation. This result is somewhat intuitive; it tells us that, overall, populations surrounding airports tend to share similar characteristics across all airports, though within any particular airport the populations therein and their exposures to noise are quite varied. Because of this, we focus our attention on within-airport characteristics that could cause our estimates of the noise-CVD association (and the standard errors of those estimates) to be biased.

Given the nature of the data - ZCTAs nested in airports located throughout the US - a natural concern is that of unaccounted for spatial correlation among neighboring ZCTAs in the same airport. While the random effects defined in Eq. 3.1 impose a correlation structure among all ZCTAs that share a common airport, the imposed correlation structure is largely non-spatial as it essentially borrows information equally across all ZCTAs surrounding the airport, as opposed to a more localized approach that accounts for the relative closeness of the ZCTAs (Waller and Carlin (2010)). Thus, an important question to answer first is whether, in fitting a standard Poisson GLM, we observe significant spatial correlation in the residuals. Note that residual spatial correlation would imply 1) that our model is missing some unmeasured covariates that, at least partially, explain how our outcome (total CVD hospitalizations) is correlated across locations (Wakefield (2007)), and 2) that we are violating the basic GLM assumption of uncorrelated observations (Breslow (1995)).
To examine these possibilities more closely, we focused individually on five of the larger airports in our dataset, chosen both because of their size (number of surrounding ZCTAs) and because their airport-specific estimates are varied - some positive, some negative. Additionally, because more than half of our ZCTAs are lost due to missingness when we control for PM$_{2.5}$ and ozone, we focus only on models controlling for SES and demographic variables (Model 2) for the remainder of this section. We loosely proceed as in Wakefield, 2007, Section 3.

We begin by fitting Eq. 3.1 above separately for each of the 5 selected airports under a naive Poisson model, a quasi-Poisson likelihood allowing for overdispersion, and a ZCTA-level random intercept model. Table 3.2 summarizes the estimates and standard errors of the log relative risk of the noise-CVD association at each of the five airports under the Poisson, quasi-Poisson, and random intercept models. Table 3.2 also includes a column indicating the magnitude of spatial correlation among the residuals under the naive Poisson model and whether that correlation is statistically significant. To estimate residual spatial correlation, we use Moran’s I test statistic \{Moran (1950); Bivand et al. (2008)\}, which, while not the only method of testing for statistically significant spatial correlation, is easily the most widely used. \{Cliff and Ord (1972)\}. For a vector of observations, $x$, across $n$ different locations, Moran’s I is given by:

$$\frac{n}{\sum_i \sum_j w_{ij}} \sum_i \sum_j w_{ij} (x_i - \bar{x})(x_j - \bar{x}) \sum_i (x_i - \bar{x})^2,$$

where $w_{ij}$ is the $ij^{th}$ entry in an $n \times n$ adjacency matrix $W$, and where $w_{ii} = 0$, and $w_{ij} = 1$ if locations $i$ and $j$ are neighbors - commonly defined as locations $i$ and $j$ sharing a common border. While there are other ways of defining $W$ \{Cliff and Ord (1972)\}, this is a fairly standard approach \{Besag et al. (1991); Waller and Carlin (2010)\} and is the form we will adopt here as well. Note that Moran’s I can take on any value between -1 and 1, and it can be loosely interpreted analogously to Pearson’s correlation coefficient.

Two things are very obvious from Table 3.2: 1) There is a considerable amount of...
Table 3.2: Estimates and Standard Errors for $\beta_4^A$ for Five Airports in our Study under Different Poisson Models: Moran’s I calculated under the naive Poisson model. (*) Indicates that Moran’s I is statistically significant.

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>0.0142</td>
<td>0.0142</td>
<td>0.0054</td>
<td>0.0148</td>
<td>0.0056</td>
<td>0.033</td>
</tr>
<tr>
<td>B</td>
<td>0.0086</td>
<td>0.0086</td>
<td>0.0042</td>
<td>0.0098</td>
<td>0.0051</td>
<td>0.014</td>
</tr>
<tr>
<td>C</td>
<td>-0.0096</td>
<td>-0.0096</td>
<td>0.0026</td>
<td>-0.0071</td>
<td>0.0041</td>
<td>0.021</td>
</tr>
<tr>
<td>D</td>
<td>-0.0007</td>
<td>-0.0007</td>
<td>0.0022</td>
<td>-0.0010</td>
<td>0.0022</td>
<td>-0.094</td>
</tr>
<tr>
<td>E</td>
<td>0.0018</td>
<td>0.0018</td>
<td>0.0023</td>
<td>-0.0003</td>
<td>0.0034</td>
<td>0.006</td>
</tr>
</tbody>
</table>

overdispersion in each airport - indicated by the much larger standard errors in the quasi-Poisson and random intercept models, and 2) After including noise exposure, individual-level risk factors (age, sex, and race), and SES and demographic variables, there does not appear to be any residual spatial correlation to speak of - indicated by the consistently small (near zero) and non-significant Moran’s I statistics. This lack of residual spatial correlation was also confirmed by examining variograms [Diggle et al. (1994); Bivand et al. (2008)] of the residuals for each of the airports, which also displayed no obvious trends. Across all airports, however, there is a high degree of spatial correlation in both the raw ZCTA-level mortality rates as well as the ZCTA-level noise exposures. Thus, at least with regards to local spatial variation, the results in Table 3.2 suggest that our models explain the local mortality rates relatively well.

While the effect estimates across all models for each of the airports are relatively consistent, there is one exception. Notice that the sign of the noise-CVD association flips at Airport E from the Poisson and quasi-Poisson models to the random intercept model. Why might this have happened? Recall that ZCTA-level random intercepts allow for information to be borrowed across all ZCTAs, and they also impose a correlation structure among the observations within a ZCTA. Also recall that there are 8 different age/sex/race strata for each ZCTA, meaning there are 8 different observations for each ZCTA. Though the overdispersion parameter in the quasi-Poisson model is able to broadly handle the extra variability created by having multiple observations in each ZCTA, it is not able to borrow strength globally as the random intercept model can [Waller and Carlin (2010)].
This suggests that the naive and quasi-Poisson estimate of $\beta_A^4$ for Airport E was likely inflated due to some number of outlying ZCTAs with a small number of observations that were pulled more closely to the global mean via the inclusion of the random intercept [Waller and Carlin (2010)]. Indeed, upon closer inspection of the data, we see that two of the 3 highest noise exposures at Airport E were found in ZCTAs with two of the highest observed age/sex/race specific mortality rates in Airport E; however, those mortality rates occurred in strata consisting of only 32 and 33 people, respectively. For reference, the median within-ZCTA population of an age/sex/race stratum in Airport E was 268. Because among the three models considered in Table 3.2, the random intercept model appears to be the most flexible in its ability to both account for extra variability and borrow strength globally, we opt to base our inference on the noise-CVD relationship for Airports A - E on the random intercept model.

### 3.4.2 Modeling Spatial Dependency

Based on the results displayed in Table 3.2, it does not appear as though modeling spatial correlation is necessary. However, it is an interesting exercise to investigate what would happen to our estimates, $\beta_A^4$, if we choose to model spatial dependency anyway. Consider the intrinsic conditional autoregressive (ICAR) approach to modeling spatial dependence in a Poisson regression like those we have considered throughout this section. An ICAR model would take the following general form:

$$
\log(E[Y_i]) = \log(N_i) + X_i \beta + u_i,
$$

where $u_i$ are spatially correlated random effects are conditionally defined as follows [Besag et al. (1991)]:

$$
u_i \mid u_j \neq i \sim \mathcal{N}\left(\frac{\sum_{j \neq i} w_{ij} u_j}{\sum_{j \neq i} w_{ij}}, \frac{1}{\tau u \sum_{j \neq i} w_{ij}}\right),
$$
where $w_{ij}$ have the same interpretation as before in the Moran’s I statistic, and $\tau_u$ is a conditional precision parameter, the magnitude of which determines the amount of spatial variation; a "large" value of $\tau_u$ suggests that the estimated residual spatial dependency is small (Wakefield (2007); Hodges and Reich (2010)). The model induces spatial dependence because it imposes that each $u_i$ is a weighted average of its neighbors, $j$.

It is recommended that a non-spatial random effect always be included along with the ICAR random effects because the ICAR model cannot take on a limiting form that allows non-spatial variability (Wakefield (2007)); such a model is known as a convolution model (Besag et al. (1991); Waller and Carlin (2010)), which takes the following general form:

$$\log(E[Y_i]) = \log(N_i) + X_i \beta + u_i + v_i,$$

where $v_i$ is a non-spatial random effect given by $v_i \sim N(0, \tau_v)$, $u_i$ is defined as in Eq. 3.6, and $\tau_v$ is precision parameter for the non-spatial random effects, $v_i$. Fitting these models is straightforward using the freely available WinBUGS software, which we use to fit Eq. 3.7 separately for each of Airports A - E. Table 3.3 below summarizes the ICAR results side-by-side with the random intercept results shown in Table 3.2.

<table>
<thead>
<tr>
<th>Airport</th>
<th>ICAR</th>
<th>ICAR Std. Error</th>
<th>Rand. Int.</th>
<th>Rand. Int. Std. Error</th>
<th>$\tau_u$</th>
<th>$\tau_v$</th>
<th>Moran’s I</th>
</tr>
</thead>
<tbody>
<tr>
<td>A</td>
<td>0.0151</td>
<td>0.0083</td>
<td>0.0148</td>
<td>0.0056</td>
<td>158.67</td>
<td>64.71</td>
<td>-0.247*</td>
</tr>
<tr>
<td>B</td>
<td>0.0087</td>
<td>0.0057</td>
<td>0.0098</td>
<td>0.0051</td>
<td>172.18</td>
<td>91.70</td>
<td>0.023</td>
</tr>
<tr>
<td>C</td>
<td>-0.0028</td>
<td>0.0045</td>
<td>-0.0071</td>
<td>0.0041</td>
<td>64.75</td>
<td>97.61</td>
<td>0.004</td>
</tr>
<tr>
<td>D</td>
<td>-0.0019</td>
<td>0.0034</td>
<td>-0.0010</td>
<td>0.0022</td>
<td>262.92</td>
<td>150.50</td>
<td>0.096</td>
</tr>
<tr>
<td>E</td>
<td>-0.0027</td>
<td>0.0041</td>
<td>-0.0003</td>
<td>0.0034</td>
<td>43.58</td>
<td>116.80</td>
<td>0.081</td>
</tr>
</tbody>
</table>

Table 3.3: Estimates and Standard Errors for $\beta_4^A$ for Five Airports in our Study under an ICAR Model and a Random Intercept Model: Moran’s I calculated under the ICAR model. (*) Indicates that Moran’s I is statistically significant.
It is interesting to see which effect estimates and standard errors change the most under the ICAR model. Effect estimates in Airports A, B, and D are the most consistent between the ICAR and random intercept models. This is expected, as Hodges and Reich (2010) show that if the ratio $\tau_u/\tau_v$ is large, then it is unlikely that the spatially correlated random effects will bias the parameter estimates. On the other hand, for Airports C and E, we see that the noise-CVD effect estimates change quite a bit. This, however, should not be unexpected as $\tau_u/\tau_v$ is relatively small compared to the other airports [Hodges and Reich (2010)].

Moran’s I statistic calculated for the residuals of the ICAR model at each airport actually increased in magnitude across 4 of the 5 airports. Most notably, we now observe a large, statistically significant negative correlation in the residuals at Airport A. Why this happens is not clear, particularly since $\tau_u$ is quite large, suggesting little spatial dependence in the data. Interestingly, though, the standard error of the ICAR estimate for Airport A was inflated more than that of any other airport, which - together with the residual spatial correlation - perhaps suggests some sort of over-adjustment for spatial dependence.

For completeness, we also fit the convolution model and the random intercept model to the entire dataset for all 89 airports at once. Specifically, we compared the following:

\[
\log(E[Y_{A,z,s}]) = \log(N_{A,z,s}) + \beta_0 + \beta_1 I(\text{age} > 75) + \beta_2 I(\text{sex} = M) \\
+ \beta_3 I(\text{race} = \text{nonwhite}) + \beta_4 (x_{2,z} - \bar{x}) + \gamma^T W_{2,z} + v_z + u_z,
\]

and

\[
\log(E[Y_{A,z,s}]) = \log(N_{A,z,s}) + \beta_0^A + \beta_1^A I(\text{age} > 75) + \beta_2^A I(\text{sex} = M) \\
+ \beta_3^A I(\text{race} = \text{nonwhite}) + \beta_4^A (x_{2,z} - \bar{x}) + \gamma^T W_{2,z} + v_z,
\]

82
where $v_z$ and $u_z$ are defined as they were previously. Note that we do not specify airport-specific terms for $\beta_0, \ldots, \beta_4$ in the convolution model (Eq. 3.8), as attempts to do so yielded unreasonably inflated standard errors, likely as a result of overfitting with regards to modeling the spatial dependence within airports. We do, however, specify the airport-specific effects in the random intercept model (Eq. 3.9), as this allows us to impose a broad correlation structure on all ZCTAs surrounding the same airport.

In estimating the overall effect of noise on CVD hospital admissions, the results for Eqs. 3.8 and 3.9 were quite similar. In the convolution model, we estimated log relative risk of 0.0011 (se = 0.0011, CI = [-0.0010, 0.0031]) for a 1 dB increase in noise on CVD hospitalization rates. Similarly, in the ZCTA-level random intercept model, we estimated a log relative risk of 0.0010 (se = 0.0009, CI = [-0.0007, 0.0027]). These are actually relatively consistent with the overall estimate from Model 2 in our main analysis, which yielded a log relative risk of 0.0016 (CI = [-0.0002, 0.0034]). This is encouraging, as it suggests that the original models specified by Eq. 3.1 were not severely biased due to some unaccounted for residual spatial correlation. However, because we observed significant overdispersion locally at the five airports in our sensitivity analysis, it appears as though Eq. 3.9 is preferable to Eq. 3.1. Further, because of the inconsistencies that can arise locally when specifying the ICAR model, we believe that Eq. 3.9 is preferable Eq. 3.8 as well.

Generally speaking, the results from this section are relatively consistent with previous research done in this area. Despite the substantial amount of work required to set up and fit a model with spatially correlated random effects, the results from such a model are not vastly different than a well thought-out and executed non-spatial random-effects model that place an emphasis on obtaining the appropriate variables to control for confounding. Indeed, Wakefield (2003) argues that in spatial regression studies, more effort should be placed on confounding/within-area modeling than spatial dependence, as the latter will be of secondary importance. Our results are also consistent with Hodges and Reich (2010) and Reich et al. (2006), who show that it is a fallacy that including spatially correlated random effects will "control for unmeasured spatial confounding," and that the
inclusion of spatially correlated random effects will "remove bias from the estimate of the parameter of interest, $\beta$, and generally be conservative." We saw this to be true in our subanalyses of the five airports, which confirmed the notion that the spatially correlated random effects only haphazardly adjust the estimate of $\beta$ - particularly when $\tau_u/\tau_v$ is "small" - and are not necessarily conservative {Hodges and Reich (2010)}. We conclude this section as did Wakefield (2007): "For spatial regression fitting, an appropriate mean model is more important than the choice of any particular inferential paradigm."

### 3.4.3 Threshold Effects and Non-linearity in the Exposure Response Curve

We additionally performed basic analyses to determine whether there might be a threshold for the effect of noise on CVD hospitalizations. Briefly, to examine the existence of a threshold, we fit Eq. 3.9 above, but with noise exposure categorized as being in the lower 33rd percentile, the middle 33rd percentile, or the upper 33rd percentile. Specifically, the model takes the form:

$$
\log(E[Y_{z,s}]) = \log(N_{z,s}) + \beta_0^A + \beta_1^A I(age > 75) + \beta_2^A I(sex = M) + \beta_3^A I(race = \text{nonwhite}) + \beta_4^A I(x^A_z < x^{(33)}) + \beta_5^A I(x^A_z > x^{(66)}) + \gamma^T W^A_z + v_z,
$$

(3.10)

where $x^{(33)}$ and $x^{(66)}$ denote the 33rd and 66th percentiles, respectively, of the noise exposure distribution; the observations for which $x^A_z < x^{(33)}$ act as the reference group. Denote the reference group as "low exposure," the middle 33rd percentile as "medium exposure," and the upper 33rd percentile as "high exposure." We estimated $\beta_5$, the overall log relative risk of CVD hospitalization associated with being in a high exposure ZCTA compared to a low exposure ZCTA to be 0.0199 (se = 0.0097, CI = [0.0009, 0.0389]), and $\beta_4$, the log relative risk of CVD hospitalization associated with being in a medium exposure ZCTA compared to a low exposure ZCTA, was estimated to be 0.0066 (se = 0.0104, CI = [-0.0138, 0.0270]). This suggests that there is likely a threshold below which
there is no effect of noise on CVD hospitalizations, as we are unable to detect a significant difference in the relative risk of CVD hospitalizations between low and medium exposure ZCTAs, though we observe a large difference between low exposure ZCTAs and high exposure ZCTAs.

The fact that a threshold likely exists also suggests that the exposure response curve is probably not linear, as it is less likely to be true that after a certain point the exposure response curve switches from zero to some linear relationship with a constant slope than it is that the true relationship gradually and smoothly changes as noise exposure increases. More work is needed to investigate both of these issues.

3.5 Discussion

We evaluated the relationship between residential exposure to aircraft noise and hospitalization for CVD in older US adults. In models only controlling for individual demographics, we found that this association is positive and statistically significant using both of our noise exposure metrics. Furthermore, the positive association generally persisted when accounting for ZCTA-level SES and demographic variables, and regional air pollution - particularly for the 90th percentile of noise exposure variable. Positive associations were also observed for individual cardiovascular hospitalization outcomes, but statistical power was reduced and relationships were often attenuated after controlling for demographic and air pollution variables.

We observed heterogeneity in the relationship between ambient aircraft noise and cardiovascular hospitalization across airports, consistent with prior research {Floud et al. (2011)}. As proposed elsewhere {Floud et al. (2011)}, our observed heterogeneity may reflect differences across the country in sound transmission from outdoors to indoors (where most exposure would be anticipated to occur). This could include structural attributes of the housing stock or the frequency of open windows. Airport-specific differences may also reflect different degrees of soundproofing that have occurred around
various airports in terms of the type of soundproofing program, the area (radii) covered, and the time since soundproofing, as these could influence personal exposures and spatial patterns of risk. In addition, Job and Hatfield (2001) proposed that the "soundscape" (presence of other sources of noise), "enviroscape" (physical environment in which noise occurs) and "psychscape" (individual psychology) can influence reaction to noise, leading to differences in health effects [Hatfield et al. (2001)].

Our findings add to previous literature in several key ways. First, we investigated the noise-cardiovascular hospitalization relationship across gradients of airport noise exposure levels across the largest number of airports studied to date, using statistical techniques that allowed us to estimate airport-specific effects while maximizing information from each airport for a pooled estimate. Second, we leveraged administrative data capturing the majority of older US adults, who represent an age group at greater risk for CVD. To our knowledge, this is also the largest studied population of US elderly living near airports to date. We thus had a large number of events, increasing our power to detect relationships. Third, we evaluated the relation of noise with cardiovascular hospitalization as the outcome, which, to our knowledge, has been rarely considered in previous noise studies. An ecological study of 62 municipalities around an airport in Amsterdam found no clustering of cardiovascular hospitalizations in areas close to the airport [Babisch (2006)], but we improve on this study by assessing the relation for individual at-risk subjects. Fourth, we accounted for the potential confounding of air pollution.

The estimated associations of similar magnitude across several CVD-specific outcomes are broadly consistent with the literature. For example, in areas with more aircraft noise, there were more subjects under medical treatment for heart trouble and with "pathological heart shape" [Knipschild (1977)]. A 2009 review of epidemiological studies found sufficient evidence of positive relationships among aircraft noise and high blood pressure and cardiovascular medication use [Babisch and Kamp (2009)]. One study included in this review investigated the relationship between aircraft noise and incidence of hypertension and found a positive association, particularly in older subjects [Eriks-
son et al. (2007). Hypertension is not typically a primary reason for hospital admission, so it was not specifically included in our analyses, but hypertension is associated with multiple cardiovascular sequelae that would contribute to hospitalizations.

In addition, although aircraft-related noise has a different profile from traffic-related noise, our findings are consistent with the noise-CVD health literature. For example, in models controlling for individual characteristics, ZCTA-level SES and demographics, and air pollution, we found the strongest association (positive and statistically significant) with IHD hospitalizations, consistent with conclusions of an expert report regarding likely mechanisms of noise-related health effects (Babisch and Kim (2011)). Our findings were also consistent with studies looking jointly at noise and air pollution. For example, Beelen et al. (2009) found excess cardiovascular mortality in the highest category of noise, which was reduced slightly after controlling for air pollution. Huss et al. (2010) found that the association between aircraft noise and mortality from MI was not attenuated with adjustment for air pollution. de Kluizenaar et al. (2007) found that after controlling for PM$_{10}$, the relationship between road traffic noise and hypertension became marginally significant. We found that controlling for air pollution increased the relative risk for both noise exposure metrics (relative to Model 2).

There are multiple limitations with our analysis, related in part to limitations with the population database. Although using the Medicare data allowed us to cover nearly the entire US elderly population, this database was developed for administrative purposes and has been shown to be subject to misclassification (Losina et al. (2003); Kiyota et al. (2004)) and geographic variability in evaluation and management (Havranek et al. (2004); Baicker et al. (2004)). Geographic variation has been linked to characteristics of providers and hospital variation (Havranek et al. (2004)). It is conceivable (although unlikely) that these characteristics may also relate to physical and social factors such as housing stock and community organization and involvement around noise mitigation and thus, they might contribute to heterogeneity in the noise-cardiovascular hospitalization relationship. We only used primary diagnosis, which should reduce misclassification
of outcomes {Dominici et al. (2006)}, and our analyses of combined CVD outcomes are unlikely to have significant misclassification. Previous studies investigating the relation of particulate pollution and cardiovascular hospitalization found no evidence of effect modification by underlying diagnosis rates; however, this test was not performed specific to our noise-related risk estimates.

Other limitations of the Medicare data include limited individual data on risk factors. For example, we were not able to control for smoking and diet, strong risk factors for CVD. These variables would only confound the noise-CVD hospitalization association if there were significant correlations between noise exposures and these risk factors. Noise contours, however, display fairly sharp gradients and skew as a function of prevailing wind directions, given runway orientation and arrival/departure patterns. Thus, we believe behavioral characteristics would unlikely be similarly patterned in space, unless property values were strongly tied to airport noise and socioeconomic patterns therefore followed noise contours. We are, however, able to control for a number of ZCTA-level SES and demographic variables - among which was median household income - allowing us to broadly control for potential confounding due to socioeconomic patterns. Our estimates were generally robust to area-level SES covariates, but we lacked the individual-level addresses and SES characteristics to formally address this question. In addition, our ZCTA-level SES and demographic variables were taken from Census 2000 data because only limited SES information from Census 2010 was available at the ZCTA-level at the time of our analysis. We thus assumed that patterns of ZCTA-level SES typically remained similar over that time. More generally, the availability of only ZCTA-level address information can lead to exposure misclassification. Noise gradients are substantial at close proximity to airports, and we were unable to differentiate among individuals’ noise exposure within zip codes. However, the use of a study population closely aligned with census data (given near-universal enrollment in Medicare) allowed us to reasonably estimate a representative ZCTA-resolution population exposure, with error most likely to be Berksonian with unbiased regression coefficients and inflated standard errors.
Using INM to predict noise exposure also has limitations. INM uses average annual input conditions. Therefore, values may lack precision because certain local acoustical variables, such as humidity effects, ground absorption, individual aircraft directivity patterns and sound diffraction around terrain or buildings, are not averaged or may not be explicitly modeled [Federal Aviation Administration - Office of Environment and Energy (2007)]. That said, INM is well-established internationally [Eriksson et al. (2010)], and is the required noise assessment tool in the US for airport noise compatibility planning and environmental assessments and impact statements. Each of our derived exposure metrics had its own inherent limitations, with the population-weighted average potentially reducing the contrast between ZCTAs and the 90th percentile of noise exposure not capturing the exposure profile of the entire ZCTA.

We were, however, able to conduct a number of sensitivity analyses to test the robustness of our results to various statistical assumptions. In particular, we showed that 1) the majority of the information responsible for estimating the relationship between exposure to noise and CVD hospitalization rates comes from variability within airports, with little contribution from between-airport variability; 2) despite the fact that most of the variability comes from within-airport variation, our estimates do not appear to biased as a result of residual spatial confounding, as our airport-specific residuals did not exhibit significant spatial correlation; 3) even if we do choose to include spatially correlated errors in our model, though airport-specific estimates could potentially be biased, the overall estimate of the association between noise exposure and CVD hospitalization rate was relatively stable across various modeling assumptions; and 4) initial exploratory work into the possibility of a threshold below which there is no significant association between CVD hospitalizations and noise exposure suggests that a threshold may exist.

In summary, despite some data-related limitations, we found that airport noise, particularly characterized by the 90th percentile of noise exposure among census blocks within ZCTAs, is statistically significantly associated with higher relative risk of cardiovascular hospitalization among older subjects. This relationship remained after control-
ling for individual data, ZCTA-level SES and demographics, and air pollution variables. Our results provide evidence of a potential adverse effect of airport noise on cardiovascular health, and further research should refine these associations and strengthen causal interpretation by investigating modifying factors at the airport or individual level.
Appendix

Appendix A: Life Expectancy Calculation

County-level life expectancies in Dataset 1 were calculated by applying a mixed-effects spatial Poisson model to mortality data from the National Center for Health Statistics (NCHS) and population data from the U.S. Census to obtain robust estimates of the number of deaths in each county {Kulkarni et al. (2011)}. These estimated counts are then used to calculate county life expectancies using standard life table techniques, which we discuss in more detail below. Specifically, the model is given by:

\[
\log E(y_{rjt}) = \beta_0 + \beta_1 \text{income}_{jt} + \beta_2 \text{education}_j + \beta_3 \sigma^\text{post}_j + \beta_4 \text{race} + \gamma_j t + \mu_j
\]  

(4.1)

where \( y_{rjt} \) is the death count for race \( r \) within county \( j \) in year \( t \); \( \text{income}_{jt} \) is county per-capita income for year \( t \); \( \text{education}_j \) is the percent of adults within county \( j \) having completed high school in the 2000 census data; and race is a dummy variable for three race groups (white, black, and other). \( \sigma^\text{post}_j \) is a geospatial component, calculated as the average of the posterior mode of the county random intercept for counties adjacent to county \( j \) to account for residual spatial patterns, the values of which were derived from first running as a prior step the same model above without the geospatial component to derive the posterior values of the county random effect. Similarly, \( \mu_j \) is the posterior value of the county random intercept. Lastly, \( \gamma_j \) is a random slope on time, \( t \), for each county {Kulkarni et al. (2011)}.

These estimated counts, which are more robust due to the borrowing of information across space and time, are then used to calculate county life expectancies using standard life table techniques. Briefly, the estimated death counts within each age stratum, or interval, are divided by the mid-year population in that interval, providing us with an age-specific death rate for each age interval. This age-specific death rate is then used
together with a term that estimates the average number of years lived by persons who
die in each particular age interval - a term which, when expressed as a fraction, is often
estimated as \( \frac{1}{2} \) - to estimate the probability of dying within each age interval. Using this
age interval-specific probability of dying, one can then project the mortality experience
of a hypothetical cohort that experiences the same age-specific probabilities of dying as
our observed population. This is done for all counties. More details on calculating life
expectancy in the life table setting are available in various texts {Chiang (1968); Keyfitz
and Flieger (1990); Preston et al. (2001)}. Note then, that the hierarchical model only pro-
vides more robust estimates of the death counts within each age interval for each county,
which often times can be small and unstable for smaller counties. The actual process of
calculating life expectancy in a life table setting does not change.

**Appendix B: Datasets 2 and 3 - Variables and Data Sources**

The variables in Dataset 2 (211 counties, 1980 - 2000) were: life expectancy, \( PM_{2.5} \),
per capita income, population, and proportions of the population who were high school
graduates, who had not lived in that county 5 years earlier (5-year in-migration), who
had an urban residence, and who reported they were white, black, or Hispanic. Age-
standardized death rates for lung cancer and chronic obstructive pulmonary disease
(COPD) were included in the dataset to account for smoking prevalence in the popu-
lation. Each variable had a value for both 1980 and 2000. This data and its sources are
described in more detail elsewhere {Pope et al. (2009)}.

The variables in Dataset 3 (211 counties, 2007) were the same as those in Dataset 2,
and the data sources for these data were identical to those of the 545 county dataset with
two exceptions: 1) proportion of the population that did not live in the county 5 years
earlier, and 2) proportion of the population with an urban residence; these two variables
are only available from the decennial Census, so we used year 2000 values as a proxy for
2007. Additionally, as in Dataset 1, due to the availability of NCHS data, 2005 death rates
were used as a proxy for 2007.
Yearly average PM\textsubscript{2.5} for 2007 was calculated at the MSA level by averaging the yearly county-level PM\textsubscript{2.5} readings for all counties in a given MSA. We calculated both population-weighted and non-weighted averages. Combining Datasets 2 and 3 enabled us to extend the analysis in Pope et al.\textsuperscript{5} to the periods 1980 - 2007, and 2000 - 2007. When we exclusively analyzed the 211 counties in Pope et al. (2009) regardless of the time period, we did so with PM\textsubscript{2.5} calculated at the MSA level for all counties, consistent with the original analysis. We also note that per capita income in Dataset 2 was obtained from the U.S. Census, while per capita income in Dataset 3 was obtained from the Bureau of Economic Analysis (BEA). BEA per capita income estimates were consistently higher than Census estimates, thus, for consistency we also obtained BEA per capita income estimates for 1980 and 2000, and results for the 211 counties from Pope et al. (2009) for the periods 1980 - 2007 and 2000 - 2007 were obtained using BEA per capita income estimates. When re-analyzing Dataset 2 (1980 - 2000), we obtained results using Census per capita income estimates as in Pope et al. (2009) and also using BEA per capita income estimates. When adjusting for changes in per capita income, the effect of PM\textsubscript{2.5} on life expectancy was not sensitive to the choice of the income variable.

We additionally note that the estimated counts used to calculate life expectancy in Dataset 3 for the year 2007 (described above in Section A) were calculated using a slightly different method than the one used to calculate the estimated death counts used to calculate life expectancy for the 211 counties in Pope et al. (2009) for the periods 1980 and 2000 (Dataset 2) {Kulkarni et al. (2011); Ezzati et al. (2008)}. However, the two methods are only substantially different in locations with very small populations (pop < 7000) {Kulkarni et al. (2011)}, which is not the case here as all of these counties are in metropolitan areas, and no counties had a year 2007 population less than 22,000. For the year 2000, where we have life expectancy estimates for the 211 counties using both methods, the correlation between the two was greater than 0.98.
Appendix C: Results from Cross-sectional Analyses

For Dataset 1 (545 counties, 2000 - 2007), simple models including only PM$_{2.5}$ as a predictor estimated an increase in life expectancy of $2.09 \pm 0.19$ and $2.63 \pm 0.28$ years for a $10 \mu g/m^3$ decrease in PM$_{2.5}$ in 2000 and 2007, respectively ($p < 0.001$ for both). Models controlling for population, per capita income, proportion of the population that is black or Hispanic, and death rates for lung cancer and COPD showed markedly smaller associations, with PM$_{2.5}$ estimates of $0.33 \pm 0.11$ ($p = 0.005$) and $0.39 \pm 0.17$ ($p = 0.021$) years for 2000 and 2007, respectively.

Similarly, a cross-sectional analysis of the year 2007 of the 211 counties in Pope et al. (2009) gave a simple estimate of $2.80 \pm 0.64$ ($p < 0.001$). PM$_{2.5}$ effects were attenuated when controlling for population, per capita income, proportion of the population that was black or Hispanic, and death rates for lung cancer and COPD (estimate $= 0.30 \pm 0.38$; $p = 0.44$). Cross-sectional analyses for the 211 counties for the years 1980 and 2000 were no different than originally reported (Pope et al. (2009)). In all datasets, however, additionally controlling for proportion of the population who are high school graduates shrank estimates of the effect of PM$_{2.5}$ towards zero, and yielded much higher p-values ($0.200 < p < 0.946$).

Appendix D: Additional Tables
Table 4.1: **Summary Characteristics of the 211 Counties Analyzed for the Years 1980 to 2007**: (*) 2005 death rates are used as a proxy for 2007 death rates. † Indicates values from the 2000 Census are used as a proxy for 2007 values.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Mean(SD)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Life Expectancy (yr.)</td>
<td></td>
</tr>
<tr>
<td>1980</td>
<td>74.32 (1.52)</td>
</tr>
<tr>
<td>2007</td>
<td>78.12 (1.86)</td>
</tr>
<tr>
<td>Change</td>
<td>3.80 (1.21)</td>
</tr>
<tr>
<td>PM$_{2.5}$ (µg/m$^3$)</td>
<td></td>
</tr>
<tr>
<td>1980</td>
<td>20.62 (4.36)</td>
</tr>
<tr>
<td>2007</td>
<td>12.44 (2.17)</td>
</tr>
<tr>
<td>Reduction</td>
<td>8.18 (3.00)</td>
</tr>
<tr>
<td>Per Capita Income (in thousands of $)</td>
<td></td>
</tr>
<tr>
<td>1980</td>
<td>20.39 (3.65)</td>
</tr>
<tr>
<td>2007</td>
<td>33.64 (8.58)</td>
</tr>
<tr>
<td>Change</td>
<td>13.25 (5.68)</td>
</tr>
<tr>
<td>Population (in hundreds of thousands)</td>
<td></td>
</tr>
<tr>
<td>1980</td>
<td>3.83 (8.47)</td>
</tr>
<tr>
<td>2007</td>
<td>5.17 (10.49)</td>
</tr>
<tr>
<td>Change</td>
<td>1.34 (2.91)</td>
</tr>
<tr>
<td>5-year In-migration (% of pop.)</td>
<td></td>
</tr>
<tr>
<td>1980</td>
<td>0.25 (0.10)</td>
</tr>
<tr>
<td>2007†</td>
<td>0.24 (0.08)</td>
</tr>
<tr>
<td>Change</td>
<td>-0.01 (0.06)</td>
</tr>
<tr>
<td>Urban Residences (% of pop.)</td>
<td></td>
</tr>
<tr>
<td>1980</td>
<td>0.58 (0.33)</td>
</tr>
<tr>
<td>2007†</td>
<td>0.78 (0.22)</td>
</tr>
<tr>
<td>Change</td>
<td>0.20 (0.18)</td>
</tr>
<tr>
<td>HS Graduates (% of pop.)</td>
<td></td>
</tr>
<tr>
<td>1980</td>
<td>0.68 (0.11)</td>
</tr>
<tr>
<td>2007</td>
<td>0.87 (0.05)</td>
</tr>
<tr>
<td>Change</td>
<td>0.19 (0.14)</td>
</tr>
<tr>
<td>Black Population (% of pop.)</td>
<td></td>
</tr>
<tr>
<td>1980</td>
<td>0.097 (0.118)</td>
</tr>
<tr>
<td>2007</td>
<td>0.116 (0.128)</td>
</tr>
<tr>
<td>Change</td>
<td>0.019 (0.069)</td>
</tr>
<tr>
<td>Hispanic Population (% of pop.)</td>
<td></td>
</tr>
<tr>
<td>1980</td>
<td>0.035 (0.072)</td>
</tr>
<tr>
<td>2007</td>
<td>0.088 (0.101)</td>
</tr>
<tr>
<td>Change</td>
<td>0.053 (0.053)</td>
</tr>
<tr>
<td>Deaths from Lung Cancer (no./ 10,000 pop.)*</td>
<td></td>
</tr>
<tr>
<td>1980</td>
<td>14.38 (2.95)</td>
</tr>
<tr>
<td>2007</td>
<td>15.25 (3.37)</td>
</tr>
<tr>
<td>Change</td>
<td>0.87 (3.27)</td>
</tr>
<tr>
<td>Deaths from COPD (no./ 10,000 pop.)*</td>
<td></td>
</tr>
<tr>
<td>1980</td>
<td>7.92 (1.85)</td>
</tr>
<tr>
<td>2007</td>
<td>11.99 (3.24)</td>
</tr>
<tr>
<td>Change</td>
<td>4.07 (3.13)</td>
</tr>
</tbody>
</table>
Table 4.2: **Summary Characteristics of the 211 Counties Analyzed for the Years 2000 to 2007:** (∗), 2005 death rates are used as a proxy for 2007 death rates.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Mean(SD)</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Life Expectancy (yr.)</strong></td>
<td></td>
</tr>
<tr>
<td>2000</td>
<td>77.04 (1.82)</td>
</tr>
<tr>
<td>2007</td>
<td>78.12 (1.86)</td>
</tr>
<tr>
<td>Change</td>
<td>1.08 (0.64)</td>
</tr>
<tr>
<td><strong>PM$_{2.5}$ (µg/m$^3$)</strong></td>
<td></td>
</tr>
<tr>
<td>2000</td>
<td>14.10 (2.86)</td>
</tr>
<tr>
<td>2007</td>
<td>12.44 (2.17)</td>
</tr>
<tr>
<td>Reduction</td>
<td>1.67 (1.25)</td>
</tr>
<tr>
<td><strong>Per Capita Income (in thousands of $)</strong></td>
<td></td>
</tr>
<tr>
<td>2000</td>
<td>31.69 (8.01)</td>
</tr>
<tr>
<td>2007</td>
<td>33.64 (8.58)</td>
</tr>
<tr>
<td>Change</td>
<td>1.95 (2.70)</td>
</tr>
<tr>
<td><strong>Population (in hundreds of thousands)</strong></td>
<td></td>
</tr>
<tr>
<td>2000</td>
<td>4.82 (10.13)</td>
</tr>
<tr>
<td>2007</td>
<td>5.17 (10.49)</td>
</tr>
<tr>
<td>Change</td>
<td>0.35 (0.79)</td>
</tr>
<tr>
<td><strong>HS Graduates (% of pop.)</strong></td>
<td></td>
</tr>
<tr>
<td>2000</td>
<td>0.869 (0.050)</td>
</tr>
<tr>
<td>2007</td>
<td>0.875 (0.046)</td>
</tr>
<tr>
<td>Change</td>
<td>0.006 (0.015)</td>
</tr>
<tr>
<td><strong>Black Population (% of pop.)</strong></td>
<td></td>
</tr>
<tr>
<td>2000</td>
<td>0.115 (0.130)</td>
</tr>
<tr>
<td>2007</td>
<td>0.116 (0.128)</td>
</tr>
<tr>
<td>Change</td>
<td>0.001 (0.028)</td>
</tr>
<tr>
<td><strong>Hispanic Population (% of pop.)</strong></td>
<td></td>
</tr>
<tr>
<td>2000</td>
<td>0.068 (0.093)</td>
</tr>
<tr>
<td>2007</td>
<td>0.088 (0.101)</td>
</tr>
<tr>
<td>Change</td>
<td>0.019 (0.016)</td>
</tr>
<tr>
<td><strong>Deaths from Lung Cancer (no./ 10,000 pop.)</strong></td>
<td></td>
</tr>
<tr>
<td>2000</td>
<td>16.73 (3.27)</td>
</tr>
<tr>
<td>2007</td>
<td>15.25 (3.37)</td>
</tr>
<tr>
<td>Change</td>
<td>-1.48 (1.96)</td>
</tr>
<tr>
<td><strong>Deaths from COPD (no./ 10,000 pop.)</strong></td>
<td></td>
</tr>
<tr>
<td>2000</td>
<td>12.37 (2.71)</td>
</tr>
<tr>
<td>2007</td>
<td>11.99 (3.24)</td>
</tr>
<tr>
<td>Change</td>
<td>-0.38 (2.15)</td>
</tr>
</tbody>
</table>
Table 4.3: **Results of Selected Regression Models for MSA-Level Analysis, 1980 - 2007**: (a), Included only counties with a 1986 population ≥ 100,000; (b), Included only counties with the largest 1986 population in the MSA. Changes in LC ASDR and COPD ASDR are changes in the age standardized death rate for lung cancer and chronic obstructive pulmonary disease, respectively.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Model 1</th>
<th>Model 2</th>
<th>Model 3</th>
<th>Model 4</th>
<th>Model 5</th>
<th>Model 6&lt;sup&gt;a&lt;/sup&gt;</th>
<th>Model 7&lt;sup&gt;b&lt;/sup&gt;</th>
<th>Model 8&lt;sup&gt;b&lt;/sup&gt;</th>
</tr>
</thead>
<tbody>
<tr>
<td>Intercept</td>
<td>3.01±0.32</td>
<td>1.38±0.23</td>
<td>2.58±0.34</td>
<td>2.56±0.35</td>
<td>2.58±0.35</td>
<td>2.62±0.42</td>
<td>1.69±0.70</td>
<td>1.27±0.68</td>
</tr>
<tr>
<td>Reduction in PM&lt;sub&gt;2.5&lt;/sub&gt;</td>
<td>0.99±0.39</td>
<td>0.83±0.20</td>
<td>0.57±0.19</td>
<td>0.64±0.18</td>
<td>0.56±0.19</td>
<td>0.60±0.22</td>
<td>1.02±0.36</td>
<td>1.13±0.36</td>
</tr>
<tr>
<td>Change in income</td>
<td>–</td>
<td>0.10±0.02</td>
<td>0.08±0.01</td>
<td>0.09±0.01</td>
<td>0.09±0.01</td>
<td>0.08±0.01</td>
<td>0.15±0.03</td>
<td>0.13±0.02</td>
</tr>
<tr>
<td>Change in pop.</td>
<td>–</td>
<td>0.09±0.04</td>
<td>0.06±0.03</td>
<td>0.07±0.02</td>
<td>0.06±0.02</td>
<td>0.06±0.03</td>
<td>0.04±0.03</td>
<td>0.03±0.03</td>
</tr>
<tr>
<td>Change in mig. rate</td>
<td>–</td>
<td>3.27±1.13</td>
<td>3.66±1.00</td>
<td>–</td>
<td>3.57±0.89</td>
<td>5.45±1.80</td>
<td>3.95±2.35</td>
<td>4.97±2.27</td>
</tr>
<tr>
<td>Change in urban rate</td>
<td>–</td>
<td>-0.31±0.30</td>
<td>-0.10±0.29</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>-2.80±2.64</td>
<td>–</td>
</tr>
<tr>
<td>Change in HS%</td>
<td>–</td>
<td>1.25±0.83</td>
<td>0.19±0.65</td>
<td>–</td>
<td>–</td>
<td>–</td>
<td>-1.79±1.30</td>
<td>–</td>
</tr>
<tr>
<td>Change in black%</td>
<td>–</td>
<td>-1.97±0.76</td>
<td>-3.05±0.66</td>
<td>-3.29±0.74</td>
<td>-3.02±0.62</td>
<td>-3.71±1.21</td>
<td>-8.79±2.74</td>
<td>-8.80±2.79</td>
</tr>
<tr>
<td>Change in Hisp%</td>
<td>–</td>
<td>2.66±1.48</td>
<td>1.86±1.12</td>
<td>–</td>
<td>1.85±1.11</td>
<td>1.97±1.28</td>
<td>2.32±2.57</td>
<td>4.13±2.13</td>
</tr>
<tr>
<td>Change in LC ASDR</td>
<td>–</td>
<td>–</td>
<td>-0.07±0.03</td>
<td>-0.06±0.03</td>
<td>-0.07±0.03</td>
<td>-0.11±0.03</td>
<td>-0.09±0.05</td>
<td>-0.10±0.05</td>
</tr>
<tr>
<td>Change in COPD ASDR</td>
<td>–</td>
<td>–</td>
<td>-0.10±0.04</td>
<td>-0.10±0.03</td>
<td>-0.10±0.04</td>
<td>-0.06±0.04</td>
<td>-0.01±0.07</td>
<td>0.01±0.07</td>
</tr>
<tr>
<td>No. of county units</td>
<td>211</td>
<td>211</td>
<td>211</td>
<td>211</td>
<td>211</td>
<td>127</td>
<td>51</td>
<td>51</td>
</tr>
</tbody>
</table>
Table 4.4: Results of Selected Regression Models for MSA-Level Analysis, 2000 - 2007: (a), Included only counties with a 1986 population $\geq$ 100,000; (b), Included only counties with the largest 1986 population in the MSA. Changes in LC ASDR and COPD ASDR are changes in the age standardized death rate for lung cancer and chronic obstructive pulmonary disease, respectively.

<table>
<thead>
<tr>
<th>Variable</th>
<th>Model 1</th>
<th>Model 2</th>
<th>Model 3</th>
<th>Model 4</th>
<th>Model 5</th>
<th>Model 6&lt;sup&gt;a&lt;/sup&gt;</th>
<th>Model 7&lt;sup&gt;b&lt;/sup&gt;</th>
<th>Model 8&lt;sup&gt;b&lt;/sup&gt;</th>
</tr>
</thead>
<tbody>
<tr>
<td>Intercept</td>
<td>0.98±0.05</td>
<td>0.84±0.10</td>
<td>0.83±0.09</td>
<td>0.79±0.07</td>
<td>0.83±0.05</td>
<td>0.83±0.08</td>
<td>0.94±0.19</td>
<td>0.81±0.12</td>
</tr>
<tr>
<td>Reduction in PM$_{2.5}$</td>
<td>0.66±0.34</td>
<td>1.28±0.36</td>
<td>1.09±0.35</td>
<td>1.05±0.36</td>
<td>1.00±0.32</td>
<td>1.58±0.48</td>
<td>1.55±0.54</td>
<td>1.60±0.53</td>
</tr>
<tr>
<td>Change in income</td>
<td>-</td>
<td>0.02±0.02</td>
<td>0.02±0.02</td>
<td>0.02±0.02</td>
<td>-</td>
<td>-</td>
<td>-0.03±0.03</td>
<td>-</td>
</tr>
<tr>
<td>Change in pop.</td>
<td>-</td>
<td>0.14±0.09</td>
<td>0.13±0.08</td>
<td>0.13±0.07</td>
<td>0.13±0.07</td>
<td>0.08±0.06</td>
<td>0.05±0.06</td>
<td>0.08±0.05</td>
</tr>
<tr>
<td>Change in HS%</td>
<td>-</td>
<td>-4.90±3.15</td>
<td>-3.47±3.03</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-12.35±7.05</td>
<td>-</td>
</tr>
<tr>
<td>Change in black%</td>
<td>-</td>
<td>-10.06±2.28</td>
<td>-9.69±2.14</td>
<td>-9.67±2.07</td>
<td>-10.28±2.43</td>
<td>-20.35±3.90</td>
<td>-33.15±5.46</td>
<td>-29.32±5.13</td>
</tr>
<tr>
<td>Change in Hisp%</td>
<td>-</td>
<td>0.19±2.75</td>
<td>-1.26±3.03</td>
<td>-</td>
<td>-</td>
<td>-</td>
<td>-3.09±5.88</td>
<td>-</td>
</tr>
<tr>
<td>Change in LC ASDR</td>
<td>-</td>
<td>-</td>
<td>-0.03±0.02</td>
<td>-0.03±0.02</td>
<td>-0.03±0.02</td>
<td>-0.00±0.05</td>
<td>0.04±0.05</td>
<td>0.03±0.05</td>
</tr>
<tr>
<td>Change in COPD ASDR</td>
<td>-</td>
<td>-</td>
<td>-0.05±0.02</td>
<td>-0.05±0.02</td>
<td>-0.05±0.02</td>
<td>-0.07±0.05</td>
<td>-0.03±0.05</td>
<td>-0.03±0.05</td>
</tr>
<tr>
<td>No. of county units</td>
<td>211</td>
<td>211</td>
<td>211</td>
<td>211</td>
<td>211</td>
<td>127</td>
<td>51</td>
<td>51</td>
</tr>
</tbody>
</table>
References


106


