Nanowire nanocomputer as a finite-state machine

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**Classification:** PHYSICAL SCIENCES: Applied Physical Sciences and Engineering

**Nanowire finite-state machine nanocomputer**

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This article contains supporting information.
Significance Statement

Fundamental limits soon may end the decades-long trend in microelectronic computer circuit miniaturization that has led to much technological and economic progress. Nanoelectronic circuits employing new materials, devices and/or fabrication methods face formidable challenges in order to provide alternatives for future microelectronics. A key advance toward overcoming these hurdles is achieved in this work through the construction of a nanoelectronic finite-state machine (nanoFSM) computer using “bottom-up” methods. The nanoFSM integrates both computing and memory elements, which are organized from individually addressable and functionally identical nanodevices, to perform clocked, multi-stage logic. Furthermore, the device density is the highest reported to date for any nanoelectronic system. Advances in logic and design in the nanoFSM are scalable and should enable more extensive nanocomputers.

Abstract

Implementation of complex computer circuits assembled from the bottom up and integrated on the nanometer scale has long been a goal of electronics research. It requires a design and fabrication strategy that can address individual nanometer-scale electronic devices, while enabling large-scale assembly of those devices into highly-organized, integrated computational circuits. We describe how such a strategy has led to the design, construction, and demonstration of a nanoelectronic finite-state machine (nanoFSM). The system was fabricated using a design-oriented approach enabled by a deterministic, bottom-up assembly process that does not require individual nanowire registration. This methodology allowed construction of the nanoFSM through modular design employing a multi-tile architecture. Each tile/module consists of two
interconnected crossbar nanowire arrays, with each cross-point consisting of a programmable nanowire transistor node. The nanoFSM integrates 180 programmable nanowire transistor nodes in three tiles or six total crossbar arrays, and incorporates both sequential and arithmetic logic, with extensive inter-tile and intra-tile communication that exhibits rigorous input/output (I/O) matching. Our system realizes the complete 2-bit logic flow and clocked control over state registration that are required for a FSM or computer. The programmable multi-tile circuit was also re-programmed to a functionally-distinct 2-bit full adder with 32-set matched and complete logic output. These steps forward and the ability of our new design-oriented deterministic methodology to yield more extensive multi-tile systems, suggest that proposed general-purpose nanocomputers can be realized in the near future.

**Keywords:** nanocomputing / nanoprocessor / nanoelectronics / assembly / bottom-up / logic circuits / transistor
It is widely agreed (1, 2) that because of fundamental physical limits, the microelectronics industry is approaching the end of its present Roadmap (1) for the miniaturization of computer circuits based upon lithographically fabricated bulk-silicon transistors. Therefore, much effort has been invested in the nanoelectronics field for the development of novel, alternative, nanometer-scale electronic device and fabrication technologies that could serve as potential routes for ever-denser and more capable systems to enable continued technological and economic advancement (3-17). These efforts has yielded simple nanoelectronic circuits (3-5, 8-17) and more complex circuit systems (6, 7) that employ novel nanomaterials but are not integrated on the nanometer scale. In this regard, building a nanocomputer that transcends the ultimate scaling limitations of conventional semiconductor electronics has been a central goal of the nanoscience field and a long-term objective of the computing industry.

A FSM is a representation for a nanocomputer in that it is a fundamental model for clocked, programmable logic circuits (18, 19) and integrates key arithmetic and memory logic elements. In general, a FSM must maintain its internal state, modify this state in response to external stimuli, and then output commands to the external environment on that basis (18, 19). A basic state transition diagram for the 2-bit four-state FSM investigated in our work (Fig. 1A) highlights the four binary representations ‘00’, ‘01’, ‘10’, and ‘11’, and the transition from one state to another triggered by a binary input signal, ‘0’ or ‘1’. Larger, more complex FSMs may be constructed using longer binary representations.

Previous efforts have yielded circuit elements that perform simple logic functions using small numbers of individual nanoelectronic devices (8-17), but have fallen far short of
demonstrating the combination of arithmetic and register elements required to realize a FSM. Specifically, integration of distinct functional circuit elements necessitates the capability to fabricate and precisely organize circuit systems that interconnect large numbers of addressable nanometer-scale electronic devices in a readily extensible manner. As a result, implementation of a nanoFSM via bottom-up assembly of individually addressable nanoscale devices has been well beyond the state of the art. Moreover, it represents a general gap between the current single-unit circuits and modular architectures for increasing complex and functional nanoelectronic systems (8, 20-24). Below we describe how we overcome the above challenges in design, assembly and circuit fabrication for the realization of a nanoFSM in programmable multi-tile architecture, which also provides a general paradigm for further cascading nanoelectronic systems from the bottom-up.

**Results and Discussion**

To realize the nanoFSM we adopt a bottom-up compatible strategy using common circuit modules or tiles that are interconnected and programmed for distinct logic functions (21, 22). This strategy contrasts conventional circuit designs, which require different layouts for the distinct logic elements. Within the context of this bottom-up paradigm our architecture for the nanoFSM interconnects three programmable nanowire tiles (Fig. 1B). Following fabrication, the common tiles or modules are differentiated by programming with tile-1 programmed to perform arithmetic operations, and tile-2 and tile-3 programmed to function as the register elements for the first and second digits of the state, respectively. Each tile in Fig. 1B consists of two programmable nanowire transistor arrays, where each cross-point in the arrays corresponds to a programmable transistor node having an active (transistor) or inactive (resistor) state. The output
of first array serves as the input to the second array such that the two-level NOR structure of each tile can be programmed to yield complete Boolean logic (21, 22), and thus the necessary arithmetic and register elements of the nanoFSM.

The 3-tile FSM design (Fig. 1B) represents a very substantial step forward in complexity compared to previous work (8-17), given the large number of individual nanowires that must be organized in an efficient and scalable manner and the stringent demands on individual logic devices with respect to input and output (I/O) voltage matching and control over threshold voltage variation. It also represents the first experimental implementation of a bottom-up multi-tile or modular circuit architecture (8, 20-24).

We have made a general breakthrough in bottom-up organization by implementing a new deterministic fabrication methodology (Fig. 1C; Fig. S1), which enables for the first time a design-oriented fabrication of the nanoFSM from post-growth nanoscale elements. Our approach involves one initial patterning step with all subsequent steps registered to this initial pattern including the assembly and interconnection of individual nanowire elements in the 3-tile/6-array nanoFSM design. First, discrete periodic anchoring sites are defined based on the 3-tile circuit design (Fig. 1C, I; Fig. S1). Second, nanocombing (25, 26) of germanium/silicon (Ge/Si) core/shell nanowires (27) yields nanowires anchored at each site and aligned along the combing direction (Fig. 1C, II; Figs. S1A, B and S2). Third, the laterally-periodic arrays of nanowires are trimmed registered to the initially-patterned anchoring sites (Fig. 1C, III; Figs. S1A, C). Fourth, electrical contacts are made by registering to the initial anchoring sites (x-axis) and the trimmed length (y-axis) without nanowire registration (Fig. 1C, IV; Fig. S1D).
The nanoFSM circuit and chip were completed by deposition of dielectric layers, metal gate-lines, and interconnects to I/O pads for measurements (*Materials and Methods*). A scanning electron microscope (SEM) image of a crossbar array (Fig. 1D) highlights the high fidelity of the 10 pairs of electrodes with equal 1 µm pitch connecting to each of the well-aligned and periodic nanowires in the array. The high degree of alignment in all arrays prevents crossing of neighboring nanowires, which is critical for achieving uniform gate response at cross-point nodes. Focusing on the overall nanoFSM structure (Fig. 1E) reveals additional key features. First, regular I/O lines as a consequence of the near-deterministic assembly allow for layout and subsequent assembly of the 3-tile/6-array circuit in accordance with our 3-tile design versus typical post-assembly design (9-16) (following nanowire registration). Second, a high yield of single-nanowire devices was achieved: for the 72 pairs of contacts made in the six arrays, 43 (60%) were single-nanowire devices, with the remainder double-nanowire (22%) and vacancies (18%). The initial circuit design took this yield into account by including sufficient contacts, such that each tile contained ample single-nanowire devices for the actual circuit. For even larger tiled circuits, peripheral routing logic elements could be integrated to yield systematic defect-tolerant crossbar architecture (28).

This single-nanowire device yield, nanowire pitch and gate-line pitch (400 nm) results in 1.8 transistors /µm² or 1.8×10⁸/cm², at least 3-fold increase in the density compared to other post-assembly design strategies (9, 10, 13, 16). We note that the 10-fold improvement in nanowire alignment and 10-fold reduction in defect density (e.g., crossing nanowires) by nanocombing (25) compared with typical shear printing assembly methods used previously (16) enable both the increase in circuit density and the multi-tile circuits in this work. Last, regular
I/O lines of the nanoFSM (Fig. 1E) undergo fan-out (Fig. S3) to yield a ca. 4×4 mm$^2$ chip with 204 contact pads that mate to a probe card for testing.

The nanoFSM (Fig. 1B) requires extensive intra- and inter-tile signal flows, which require strict I/O voltage matching of the transistor nodes in fabricated 3-tile structures (Fig. 1E). In this regard, we have characterized the voltage-out ($V_{out}$) versus voltage-in ($V_{in}$) characteristics of all of the individual nodes in the nanoFSM configured as inverters (Fig. S4). Specifically, the Al$_2$O$_3$-ZrO$_2$-Al$_2$O$_3$ dielectric layer (Materials and Methods) introduced as a charge trapping medium (16, 29) can be programmed with a large gate input (e.g., +8 / -8 V) to accumulate/deplete charge and thereby shift the transistor threshold (Fig. S4). In this way, representative $V_{out}$ versus $V_{in}$ data show a large hysteresis (Fig. 2A), in which the transistor node behaves as an active transistor (red) or an inactive resistor (blue) in a logic input range of 0 – 3 V (gray region) following the programming step. We define a circuit threshold voltage, $V_c$, as the value of $V_{in}$ at which the inverter $V_{out}$ is reduced to 1/10 of the supply voltage, $V_d$, and sets the minimum $V_{in}$ for the inverter to output 0. I/O matching requires $V_c \leq V_d$, so that the output 1 (~$V_d$) is sufficient to serve as the input to drive the next element in the circuit without signal loss.

We optimized the Ge/Si core/shell nanowire synthesis and device fabrication steps to control $V_c$ and meet the design metric $V_c \leq V_d$, where the principle challenges were minimizing positive shifts of $V_c$ in the active state and achieving threshold uniformity (Fig. S5). Significantly, a map of the measured $V_c$ values from the 3-tile nanoFSM circuit (Fig. 2B) highlights the high yield of transistor nodes capable of gain or I/O matching. For the 190 transistor nodes in the three tiles, 177 out of 190 nodes (93%) meet the $V_c \leq V_d$ criteria, with an average $V_c \pm 1$ s.d. (standard deviation) of 0.9 ± 0.7 V at $V_d = 2$ V. Last, a histogram for these same 190 nodes
programmed to the inactive state (Fig. S6) demonstrates that 100% have $V_c > 3.5 \text{ V}$ ($V_c \pm 1 \text{ s.d.}$ of $6.2 \pm 0.5 \text{ V}$), which is outside the upper limit (3V) of the logic window.

The operation of the FSM circuit, which had been verified by simulations prior to fabrication, was programmed (Fig. S7) as shown in Fig. 1B, with $A_1A_0$, $C_{\text{in}}$ and CLK representing the 2-bit state, control input and clock signal, respectively. In this architecture, tile-1 is configured as a half adder that computes the summation of $A_1A_0 + C_{\text{in}}$. Its output $A'_1A'_0$ is the new state, where $A'_0 = A_0 \oplus C_{\text{in}}$, $A'_1 = A_1 \oplus (A_0 \cdot C_{\text{in}})$, and “$\oplus$” and “$\cdot$” represent XOR and AND logic, respectively. The computed $A'_0$ and $A'_1$ values are input to tile-2 and tile-3, which are configured as D flip-flops (DFFs). The DFFs register the new state on the rising edge of the synchronized CLK, and then this registered state is instantly fed back as input to the half adder to compute the next-level state. We first characterized the performance of the three ‘component’ tiles in the nanoFSM; these results demonstrated that the half adder and DFF (Figs. S8 and S9) exhibited correct logic. For example, the DFF, which was not demonstrated previously in bottom-up circuits, involves two intra-tile feedback loops covering six of the seven functional nanowires in the circuit, and thus is substantially more complex and requires more stringent I/O matching and transistor uniformity than demonstrated circuits with single feedback loops (14-16). The fulfillment of rigorous I/O matching is reflected in the accurate logic flow and matching of the output $Q$ to the input $D$ and clock signal $CLK$ (Fig. S9B). Moreover, the programmed DFF showed no obvious degradation after 10 h in ambient environment (Fig. S9C), thus demonstrating robustness and nonvolatility of the programmed tiles.

We have investigated the logic flow and fidelity of the nanoFSM for a variety of $C_{\text{in}}$ and CLK sequences by continuously recording $A_0$ (V) and $A_1$ (V). First, for a constant control input $C_{\text{in}} = 1$ (Fig. 3A), the state $A_1A_0$ underwent a complete logic circle from $00 \rightarrow 01 \rightarrow 10 \rightarrow 11 \rightarrow 00$, 


with each transition triggered by the CLK rising edge. The capability to fully-control and lock
the state by varying $C_{in}$ is shown for $t = 38 - 190$ s. For example, for $C_{in} = 0$ ($t = 38 - 55$ s), the
state $A_1A_0 = 00$ was locked and not triggered to the next level at the two consecutive rising edges
of CLK ($t = \sim 45, 54$ s). As the control input changed to $C_{in} = 1$, the state was unlocked and
moved to $A_1A_0 = 01$ at the rising edge of CLK ($t = \sim 63$ s). This high fidelity in the control is
shown for all the other states of 01, 10 and 11, which were locked when $C_{in} = 0$ and continued in
the logic loop when $C_{in} = 1$ ($t = 66 - 190$ s). The robustness of the nanoFSM was further tested
by inputting a more irregular control waveform (Fig. 3B), during which the states were
intermittently locked. For example, the lock of the state 01 with $C_{in} = 0$ ($t = 57 - 69$ s) was
followed by a continuous transition from $01 \rightarrow 10 \rightarrow 11$ with $C_{in} = 1$ ($t = 69 - 85$ s) before the state
11 was locked with $C_{in} = 0$ ($t = 85 - 101$ s). Similar logic flow is shown for the transition from
$00 \rightarrow 01 \rightarrow 10$ ($t = 111 - 165$ s). Overall, the complete logic fidelity and arbitrary state control in
these measurements highlight the successful implementation of a cascaded 3-tile nanoFSM
circuit.

To investigate the feasibility of extending the number of cascaded tiles, we
reprogrammed the circuit to a 2-bit full adder. Because a multi-bit full adder can be realized by
serial interconnection of 1-bit full adders (31) (Fig. 4A), this output from successive
interconnected tiles provides a critical measure of capability to extend the cascade. The high
yield of transistor nodes capable of I/O matching (Fig. 2B) was exploited to reprogram the two
DFFs of the nanoFSM such that the 2-bit full adder circuit contains a distinct configuration of
active nodes (i.e., beyond the minimum changes required to realize the adder logic). In this
cascaded 2-tile circuit (Fig. 4B), each 1-bit full adder computes the sum $S_i = A_i \oplus B_i \oplus C_i$ and
carry-out $C_{i+1} = A_i \cdot B_i + A_i \cdot C_i + B_i \cdot C_i$ ($i = 1, 2$; “+” denotes OR logic), with the computed $C_{i+1}$ and
complementary /C_{i+1} serving as the input to the higher-bit adder. Overall, the 2-bit full adder computes the summation of A_1A_0 + B_1B_0 + C_0, with S_0, S_1 the first, second digits of the sum and C_2 the carry-out. Significantly, examination of the values for the complete 32-element truth table (Fig. 4C) demonstrates that the complete logic outputs for S_0, S_1, C_2 and /C_2 are correct, and that their average logic-1 output voltages 2.43 ± 0.03, 2.39 ± 0.12, 2.34 ± 0.08 and 2.43 ± 0.06 V, respectively, are well-matched (slightly enhanced) relative to the common logic input 1 value, 2.3 V. These results strongly validate the feasibility of implementing >2-bit full adders by cascading a larger number of tiles.

**Conclusions**

The multi-tile nanoFSM and 2-bit full adder programmable circuits demonstrated above highlight several distinct features compared to previous circuits based on bottom-up-assembled elements (8-17). First, the complexity is more than 3-fold in terms of number of devices (180 transistor elements) compared to all the previous work (9-17), with the density of devices in the nanoFSM also much greater. This complexity is further enhanced in terms of circuit functionality by incorporation for the first time of both sequential and combinational logic elements. Second, this work provides the first concrete demonstration of tile integration and multiple inter-tile I/O critical to cascaded multi-tile architectures (8, 20-24) and complex circuits in general. In particular, the successful clocked operation of the nanoFSM required eight inter-tile and intra-tile feedback loops with matched I/O values, as opposed to a maximum of one demonstrated previously in single functional units (14-16). Third, instead of using an assembly-limited bottom-up fabrication strategy in all previous work (9-16), our high-precision, deterministic, bottom-up methodology has implemented for the first time a design-oriented circuit fabrication strategy that has been so successful in the conventional electronics industry. Taken together, we believe that
these results represent a significant leap in scaling-up electronic circuits from the bottom up. Our work suggests strongly that general-purpose nanoprocessors (20-24) can be realized in the near future.

Materials and Methods

Synthesis of Ge/Si core/shell nanowires. The Ge/Si nanowires were synthesized by the Au-nanocluster-catalyzed vapor-liquid-solid method described previously (27). The growth substrate (600 nm SiO₂/Si) dispersed with gold nanoparticles (10 nm, Ted Pella) was placed in a quartz-tube reactor system. The Ge core was synthesized at 255 ºC and 450 Torr, with 30 sccm germane (GeH₄, 10% in H₂) and 200 sccm H₂ as the reactant and carrier gas, respectively. The growth time was 50 min, yielding an average length of ~ 40 µm. The epitaxial Si shell was grown immediately after the growth of Ge core, at 460 ºC and 5 Torr for 2 min, with 5 sccm silane (SiH₄) as the reactant gas, and yielded nanowires with an overall diameter of 15 nm.

Deterministic nanocombing of nanowires. First, the device substrate (600 nm SiO₂/Si) was spin-coated with a thin layer (~ 25 nm) of poly(methyl methacrylate) (PMMA 950-C2, 1: 8 (v:v) diluted in ZEP-A, Microchem). Based on the layout of the circuit design, electron-beam lithography was employed to define arrays of exposed SiO₂ windows (300 nm × 10 µm) in the form of narrow stripes (Fig. S1A-1). The exposed stripes of SiO₂ surface were then functionalized with tetramethylammonium ions by rinsing the substrate in Microposit MF-319 developer for 50 s, followed by washing in deionized water (30 s). This process selectively enhances the SiO₂-surface affinity to nanowires. The functionalized substrate was then brought into contact with the nanowire-growth substrate at a constant pressure of ~ 5 N/cm², with ~ 40 µL heavy mineral oil (#330760, Sigma-Aldrich) added between the surfaces as lubricant. The growth substrate was moved along the longitudinal direction of the stripes at a constant velocity of ~ 5 mm/s, with the device substrate fixed (Fig. S1A-2). During this process, the protruding parts of nanowires were effectively anchored to the stripes of SiO₂ surface, with the rest length being drawn out over the resist (combing) surface. The weak interaction between the combing surface and nanowires maximizes the aligning shear force, resulting in the effective alignment of
nanowires on the combing surface. The modulated lateral confinement in the anchoring stripes can produce a high yield of single-nanowire anchoring events, resulting in well-aligned and periodic single-nanowire arrays on the resist surface. The heavy mineral oil was then removed by drops of octane along the combing direction. A cleaning method by using acetone vapor was employed for the effective removal of the resist layer underneath the nanowires without disturbing their arrangement.

**Fabrication of logic tiles.** A trimming process, which involved sacrificial mask (400 nm PMMA 950-C2) definition by electron-beam lithography and nanowire etching by reactive ion etching (Surface Technology Systems) using SF₆ as etchant gas, was employed to define nanowire arrays with at predefined length (Fig. S1A-4-6). The source and drain contacts of the nanowires were defined by electron-beam lithography followed by the thermal evaporation of metal contacts (Cr/Ni, 1/40 nm) and lift-off process. The dielectric layers were deposited by atomic-layer deposition, followed by top-gate definition by electron-beam lithography, thermal evaporation of metals (Cr/Au, 4/65 nm) and lift-off process.

**Growth of dielectric layers.** The trilayer Al₂O₃-ZrO₂-Al₂O₃ (2-5-5 nm) dielectric structure was grown by atomic-layer deposition at 200 ºC, with trimethylaluminum {Al(CH₃)₃}, tetrakis(dimethylamino)zirconium {Zr[N(CH₃)₂]₄} and water as precursors. Specifically, one Al₂O₃-growth cycle consisted of one water-vapor pulse (0.015 s), N₂ purge (8 s), one Al(CH₃)₃ pulse (0.015 s), and N₂ purge (8 s). One ZrO₂-growth cycle consisted of one water-vapor pulse (0.015 s), N₂ purge (8 s), one Zr[N(CH₃)₂]₄ pulse (0.25 s), and N₂ purge (8 s). A deposition sequence of 25 cycles Al₂O₃, 55 cycles ZrO₂ and 55 cycles Al₂O₃ was performed.

**Programming and testing of the circuits.** The circuit chip was mounted in a probe station (Model 12561B, Cascade Microtech). A custom-designed 204-pin probe card (Accuprobe) with BNC interface was used to electrically access the device arrays. A computer-controlled analog I/O system (2 × PXI-6723, 2 × PXIe-6358 in a PXIe-1065 chassis, National Instruments), featuring 64 analog-voltage output channels and 24 analog-voltage input channels, was used for the electrical characterization. For each nanowire, an external resistor (8-15 MΩ, Vishay) was used as illustrated in dashed box in Fig. 4A. The resistance value of the load resistor was chosen to be at least one order of magnitude larger than the “ON” resistance of the active transistor node.
(< 1 MΩ). Simplified circuit schemes without showing the load resistors are presented in Figs. 1, 4 and Figs. S7-9. The detailed programming scheme for each tile is described in Fig. S7. The tiles were programmed sequentially, with the interconnection between the tiles connected subsequently through an external switch box for the testing of the logic functionalities. For the logic outputs, drain voltages of 2.3-2.7 V were used for the DFF, FSM and 2-bit full adder demonstrated in Fig. S9 and Figs. 3, 4. Source voltages of -1 V were used for the DFF and FSM, 0 V for the 2-bit full adder. The input gate voltages were 0 V for logic 0, 2.3-3V for logic 1 as specified for each circuit in the main context.

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References


Figure Legends
**Fig. 1. Architecture and fabrication of FSM.** (A) Logic diagram of the FSM with the gray circles represent the states. Upon triggering, the straight arrows indicate the transition of the current state to the next one for an input of 1; the curved arrows indicate maintaining the current state for an input of 0. (B) Schematic of the 3-tile circuit of the nanoFSM. Each tile consists of two blocks and each block consists of a nanowire array (vertical) with lithography-defined top gate lines (horizontal). A_1A_0, C_in and CLK correspond to the 2-bit state, control and clock signal, respectively. The green dots indicate the programmed active transistor nodes. For simplicity, the circuit only shows the drain contacts (blue) but not the source contacts or load resistors. The arrows indicate external wirings, with the red ones indicating feedback loops. (C), Deterministic fabrication scheme. Key steps include: (I) definition of the anchoring sites (gray stripes); (II) single-nanowire anchoring to the specific anchoring sites with highly directional alignment; (III) nanowire trimming to yield uniform lengths; (IV) definition of contacts (light blue) and gates (orange) to the trimmed nanowires (dark blue) without registration. (D), SEM image of a 10×10 nanowire array from the nanoFSM circuit. The horizontal lines are metal gates with the top and bottom pads the source and drain contacts. Scale bar, 1 µm. (E), SEM image of the entire 3-tile/6-array nanoFSM circuit. The red enclosed region corresponds to the image area shown in (D). Scale bar, 10 µm.

**Fig. 2. Programmable transistors and threshold-voltage map.** (A) Characteristic output vs. input (V_{out} vs. V_{in}) from a programmable transistor node in the nanoFSM circuit; Fig. S4 provides additional details. The black arrows indicate the sweep directions of V_{in}. The red and blue curved correspond to programmed active transistor
and inactive resistor states (inset schematics). The grey region indicates the 0-3 V logic window. (B) Spatial map of the threshold voltage $V_c$ (at $V_d = 2$ V) in the active state for all the 190 transistor nodes used for the 3-tile circuit. Each box represents the corresponding transistor node shown in Fig. 1B. The blue color represents $V_c < 2$ V, which are capable of output gain or I/O matching; and the gray color represents $V_c \geq 2$ V, which will yield reduced output.

**Fig. 3. nanoFSM output.** (A, B) The logic flow of the output state $A_1$ (blue) $A_0$ (red) with respect to the control input $C_{in}$ (green) and clock signal CLK (gray) as indicated in Fig. 1B.

**Fig. 4. 2-bit full adder.** (A) Schematic of a n-bit full adder constructed from serial 1-bit full adders. (B) The 2-tile circuit design for the 2-bit full adder. (C) Experimental truth table for the 2-bit full adder. The table consists of 32 sets of input combinations ($A_1A_0$, $B_1B_0$, $C_0$) with the corresponding outputs $S_1$, $S_0$, $C_2$, and $/C_2$. The voltage output values are shown in brackets. The input values for 1 and 0 are 2.3 and 0 V, respectively.
Supporting Information for:

Nanowire finite-state machine nanocomputer

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This file includes:
Figures Legends S1-S9
Supporting references
Fig. S1. Circuit fabrication. (A) Schematics of the deterministic fabrication flow. Steps 1-2: nanowire assembly is carried out using the deterministic nanocombing technique (S1), with the details described in the Materials and Methods section. The dashed black line indicates the interface between the anchoring sites (blue stripes) and combing surface (yellow, PMMA). Step 3: The PMMA layer was subsequently removed by acetone vapor without disturbing the nanowire positions. The dashed black line indicates the position of the original interface between the anchoring sites. Steps 4-6: Trimming process to yield deterministic nanowire array. First, a sacrificial mask (400 nm PMMA-C2) was defined and aligned to the anchoring-combing interface (step-4). Second, the unprotected portions of the nanowires were removed by reactive ion etching (step-5). Third, the PMMA mask was then removed in acetone (step-6). Step 7: The subsequent fabrication of the device arrays. First, source/drain contacts (Cr/Ni 1/40 nm) were defined by mapping sets of contact patterns to the initial anchoring stripe positions without registration to nanowires. This approach contrasts the typical bottom-up electronic circuit fabrication methodology where each nanowire must be individually identified and a contact registered to its position. Second, Al2O3-ZrO2-Al2O3 (2-5-5 nm) dielectric layers were deposited by atomic-layer deposition. Third, arrays of gate lines (Cr/Au, 4/65 nm) were defined by electron beam lithography. (B) SEM image of a typical nanocombed Ge/Si nanowire array, corresponding to the fabricated device array in Fig. 1D. (C) SEM image of the trimmed Ge/Si nanowire array. (D) SEM image of the Ge/Si nanowire array with defined source and drain contacts. Scale bars, 1 µm in (B-D).

Fig. S2. Deterministic nanocombing. (A) SEM image of Ge/Si nanowire arrays assembled by deterministic nanocombing on a Si/SiO2 surface covering an area of ~ 0.5 × 0.6 mm2. Scale bar, 100 µm. (B), Zoomed-in SEM image of the assembled Ge/Si nanowire arrays indicated by the orange dashed region in (A). Scale bar, 10 µm. (C), Nanowire-occupancy statistics. For 496 anchoring sites equally distributed in (A), 293 (~59%) were single-nanowire sites, 122 (~25%) were double-nanowire sites, 45 (~ 9%) were vacant sites. The statistics are based on nanowires with a combing length > 2 µm.

Fig. S3. Fabricated Chip. (A) SEM image of the final chip having 204 contact pads on the outer periphery of the chip. The pads match the pins of a probe card that is connected to the test system. Scale bar, 500 µm. The metal pads and fan-in interconnect lines appear bright in the image. (B) SEM image of the inner layout of the fabricated chip as indicated in the dashed box in (A). The red dashed box region corresponds to the 3-tile circuit shown in Fig. 1E. Scale bar, 100 µm.

Fig. S4. Logic tile and programmable transistor node. (A) Schematic of the logic tile that corresponds to the tiles in Fig. 1B in the main paper. The logic input, \( V_{\text{in}} \), is fed to the first array (upper left) and its output, \( V_{\text{out}} \), serves as the input to the second array (lower right) for the final output of the tile, \( V'_{\text{out}} \). Here \( V_{\text{DD}}, V_{\text{SS}}, \) and \( R_S \) represent the drain, source voltages and load resistors, respectively. The dashed area delineates the testing unit for a single transistor node (red dot). (B) Cross-section schematic of each transistor node, which consists of a Ge/Si nanowire covered by a tri-layer Al2O3-ZrO2-Al2O3 dielectric and a top Au electrode. The tri-layer dielectric layer serves similarly as a float gate (S2, S3), such that electron-rich or electron-
depleted configuration can be resulted to modulate the threshold voltage of the transistor to be inactive or active state. (C) The equivalent circuit (a programmable inverter) to single transistor node (red dot) in (A). This circuit also corresponds to the $V_{\text{in}} - V_{\text{out}}$ relationship ($V_{\text{DD}} = 2$ V, $V_{\text{SS}} = 0$ V) shown in Fig. 2A in the main paper.

Fig. S5. Control of threshold voltage. (A) The circuit threshold voltage $V_c$ (at $V_d = 1$ V) for the active Ge/Si transistor nodes from different control tests. The charge-trapping transistor devices all adopt the same structure as described in the main paper, with the gate line (Cr/Au, 4/65 nm) width 200 nm. First, a trend of reduction in the $V_c$ was observed with the decrease of growth temperature for the Ge core (blue dots). Second, for nanowires with the Ge core grown at a fixed temperature of 255 ºC (the ones used for the construction of nanoFSM), the nanocombing and trimming processes involved in device-array fabrication (Materials and Methods) had little effect on $V_c$ (0.46 ± 0.52 V, red star), compared to the value (0.33 ± 0.64 V) obtained from analysis of single nanowire devices prepared by solution-dispersion on a substrate (without nanocombing and trimming steps). However, resist removal (Fig. S1A-3) by UV-ozone (120 ºC, 15 s) does result in an increase in the $V_c$ (0.75 ± 0.56 V, green diamond), which is unfavorable to I/O matching. Therefore, the resist, which serves as the combing layer, was removed in acetone vapor; this method did not perturb the combed nanowires and did not adversely affect $V_c$. In addition, $V_c$ can be reduced further by using Al gate lines (-0.74 ± 0.55 V, gray circle). (B) Schematic of the resist removal by acetone vapor (Fig. S1A-3).

Fig. S6. Statistics of $V_c$. It features the $V_c$ from both active (red) and inactive (blue) states (at $V_d = 2$ V) from the 190 transistor nodes shown in Fig. 2B in the main paper.

Fig.S7. Programming scheme for the logic tiles. The programming scheme is illustrated in a simplified tile structure, with 3 × 3 transistor nodes in block-1 and 2 × 3 in block-2. This scheme is expandable to tiles with arbitrary size and number of transistor nodes as in our work. (A) Consecutive steps for programming the selected transistor nodes to be active in both blocks in the tile. The square box at each transistor node indicates voltage difference between the gate line and nanowire during the programming, with dark, green and magenta indicating the difference of $-V$, $V$ and $V/2$, respectively. For the actual programming voltage used ($V = -9$ V for 5 s), a $-V$ and $V$ difference can program the node to be inactive and active, respectively, while a $V/2$ difference does not alter the state. The dashed white box indicates that the programmed state in the block-1 is presently not relevant to the final state. (B) The intermediate programmed state of block-2, with the circled green dot indicating the programmed active state in the node. (C) The final programmed state of the tile (target programming state).

The programming process starts from block-2. First, all the nanowires (source and drain) in block-1 are applied $-V$ with all the nanowires in block-2 grounded, which maps the entire block-2 to be inactive (A, step-I). Then for the selected node, the nanowire in Block-1 connecting to the gate line of this node is applied $V$ with the corresponding nanowire in Block-2 grounded; the rest nanowires in Block-1 and Block-2 are all applied $V/2$ (A, step-II). In this manner, a voltage difference $V$ is produced at the selected node in Block-2, with the rest nodes having voltage difference of either $V/2$ or 0. Therefore, only the selected node is programmed to be active (as shown in B). Similarly, for the subsequent programming of block-1, all the gate lines in block-1
are applied \(-V\) with all the nanowires in the tile grounded to map the entire block-1 inactive (\(A\), step-\(III\)). Then for the selected node, the corresponding gate line and nanowire are applied \(V\) and 0, respectively; the rest gate lines and nanowires in block-1 are applied \(V/2\) with the nanowires in block-2 grounded (\(A\), step-\(IV\)). In this way, the selected node is applied a voltage difference of \(V\), with the rest nodes in the entire tile having voltage difference no larger than \(V/2\). Therefore, the selected node in block-1 is programmed to be active, without altering the previously programmed states in block-2 (as shown in \(C\)). Note that for multiple nodes to be programmed, the programming can be done sequentially for each gate line, and the multiple nodes sharing the same gate line in the same block can be programmed simultaneously.

**Fig. S8. Logic outputs of the half adder.** The half adder constitutes the 1st tile in the FSM circuit in Fig. 1B. (\(A\)) Schematic of the programmed circuit, with \(A_1A_0\), \(C_{\text{in}}\) and \(A'_1A'_0\) representing the 2-bit input, 1-bit input, and 2-bit output, respectively. The green dots at cross-points highlight nodes programmed to the active state. (\(B\)) The complete logic outputs with respect to different inputs (\(C_{\text{in}}, A_1A_0\)). The logic inputs 0 and 1 had values of 0 and 2.4 V, respectively, and \(V_{\text{dd}} = 2.6\) V. (\(C\)) The corresponding truth table of the half adder. The logic outputs of 0 and 1 show an experimental range of 0-0.1 V and 2.4-2.5 V, respectively, thus demonstrating strict I/O matching.

**Fig. S9. DFF circuit and logic output.** (\(A\)) Schematic of the logic (upper) and physical tile circuit design (lower) of the DFF that serves as the register elements in the FSM circuit. The green dots indicate the active transistor nodes. (\(B\)) Measurement of \(Q\) (V) with respect to D and CLK signals demonstrates that \(Q\) is consistently changed to new values of D with the rising edge of CLK, while the circuit holds or locks its state at other times and that the output \(Q\) (2.55 V) matches closely the input D (2.50 V) and CLK (2.60 V). (\(C\)) Stability of the programmed DFF circuit. Logic output from the same circuit after 10 h in ambient environment without re-programming. The output exhibits no obvious degradation during this time period. Degradation of the output was observed beyond 15 h, which is largely due to changes in individual transistor nodes (e.g., by moisture). We expect that hermetic sealing/passivation of the circuit, which is standard for conventional top-down fabricated circuits, will resolve this issue and substantially improve the long-term stability of our programmable nanowire circuits.

**Supporting References**


