The glaciations of the Neoproterozoic Era (1,000 to 542 MyBP) were preceded by dramatically light C isotopic excursions preserved in preglacial deposits. Standard explanations of these excursions involve remineralization of isotopically light organic matter and imply strong enhancement of atmospheric CO$_2$ greenhouse gas concentration, apparently inconsistent with the glaciations that followed. We examine a scenario in which the isotopic signal, as well as the global glaciation, result from enhanced export of organic matter from the upper ocean into anoxic subsurface waters and sediments. The organic matter undergoes anoxic remineralization at depth via either sulfate- or iron-reducing bacteria. In both cases, this can lead to changes in carbonate alkalinity and dissolved inorganic pool that efficiently lower the atmospheric CO$_2$ concentration, possibly plunging Earth into an ice age. This scenario predicts enhanced deposition of calcium carbonate, the formation of siderite, and an increase in ocean pH, all of which are consistent with recent observations. Late Neoproterozoic diversification of marine eukaryotes may have facilitated the episodic enhancement of export of organic matter from the upper ocean, by causing a greater proportion of organic matter to be partitioned as particulate aggregates that can sink more efficiently, via increased cell size, biominerization or increased C:N of eukaryotic phytoplankton. The scenario explains isotopic excursions that are correlated or uncorrelated with snowball initiation, and suggests that increasing atmospheric oxygen concentrations and a progressive oxygenation of the subsurface ocean helped to prevent snowball glaciation on the Phanerozoic Earth.

Biologically induced initiation of Neoproterozoic snowball-Earth events

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The glaciations of the Neoproterozoic Era (1,000 to 542 MyBP) were preceded by dramatically light C isotopic excursions preserved in preglacial deposits. Standard explanations of these excursions involve remineralization of isotopically light organic matter and imply strong enhancement of atmospheric CO$_2$ greenhouse gas concentration, apparently inconsistent with the glaciations that followed. We examine a scenario in which the isotopic signal, as well as the global glaciation, result from enhanced export of organic matter from the upper ocean into anoxic subsurface waters and sediments. The organic matter undergoes anoxic remineralization at depth via either sulfate- or iron-reducing bacteria. In both cases, this can lead to changes in carbonate alkalinity and dissolved inorganic pool that efficiently lower the atmospheric CO$_2$ concentration, possibly plunging Earth into an ice age. This scenario predicts enhanced deposition of calcium carbonate, the formation of siderite, and an increase in ocean pH, all of which are consistent with recent observations. Late Neoproterozoic diversification of marine eukaryotes may have facilitated the episodic enhancement of export of organic matter from the upper ocean, by causing a greater proportion of organic matter to be partitioned as particulate aggregates that can sink more efficiently, via increased cell size, biominerization or increased C:N of eukaryotic phytoplankton. The scenario explains isotopic excursions that are correlated or uncorrelated with snowball initiation, and suggests that increasing atmospheric oxygen concentrations and a progressive oxygenation of the subsurface ocean helped to prevent snowball glaciation on the Phanerozoic Earth.
isotropic excursion and vice versa. The mechanism, although necessarily speculative, may explain why snowball events occurred in the Neoproterozoic but not thereafter, addresses the time scale between events, seems consistent with snowball-related geochemical observations, and makes several testable predictions.

An Overview of the Snowball Initiation Scenario
First, we consider attempts to explain preglacial isotopic excursions by a net aerobic remineralization of isotopically light organic matter. Fig. 1 shows such a scenario (using the model described in Materials and Methods and the SI Appendix). The scenario assumes a temporary drop in oxygenic primary production while aerobic remineralization proceeds unchanged (Fig. 1A). The pool of dissolved organic carbon (DOC) consequently shrinks while the dissolved inorganic carbon (DIC) pool grows (Fig. 1B), and the isotopic composition of both becomes significantly lighter (Fig. 1B). However, as a result of the increased DIC pool, atmospheric pCO₂ rises dramatically (Fig. 1C), preventing glaciation and, therefore, seemingly inconsistent with the observed record.

There are many indications that the oxygen minimum zone of Neoproterozoic oceans tended toward anoxia (20, 21). With this in mind, we consider a steady state of ocean biogeochemistry, with oxygenic upper ocean primary production by cyanobacteria and algae balanced largely by aerobic remineralization within the surface ocean mixed layer. A (small) net export production flux would maintain subsurface water-column anoxia by consuming dissolved oxygen mixed into the subsurface ocean from oxygenated surface water. Most of the organic matter would be contained within the upper oxygenated ocean in both dissolved form and suspended particulate form (e.g., cyanobacteria cells) that tends to remain in the upper ocean because of its relative buoyancy; both forms are referred to together below as DOC. Further consider the possibility that at some point an increase in this export rate sends an enhanced flux of organic matter into anoxic subsurface waters and sediments, where it could be remineralized to dissolved inorganic carbon via anaerobic respiration by either sulfate reducing bacteria or iron-reducing bacteria, or buried.

Enhanced export production causes partially oxygenated subsurface ocean layers to be stripped of oxygen by the enhanced aerobic remineralization of sinking organic matter. This extends the depth range through which anoxic conditions dominate and may, therefore, reduce both oxygenic production and aerobic remineralization. As we will see shortly, this combination can lead to a reduction of atmospheric pCO₂ as well as a carbon isotopic signal consistent with the observed presnowball excursions. To appreciate this, examine now how these processes affect the marine carbonate system. Production and remineralization in the upper ocean may be represented by

\[
2\text{CO}_2 + 2\text{H}_2\text{O} = 2\text{CH}_2\text{O} + 2\text{O}_2. \tag{1}
\]

Next, the anoxic remineralization of organic matter via sulfate (SO₄²⁻) reduction leads to the formation of sulfide (H₂S, or in its dissociated form, HS⁻). Sulfide can either diffuse toward the oxygenated upper ocean and be oxidized back into sulfate, or react with Fe³⁺ to form pyrite. These three processes may be represented by

\[
2\text{CH}_2\text{O} + \text{SO}_4^{2-} \rightarrow \text{HS}^- + \text{H}_2\text{O} +\text{CO}_2 + \text{HCO}_3^-; \\
\text{HS}^- + 2\text{O}_2 \rightarrow \text{SO}_4^{2-} + \text{H}^+. \\
\text{Fe}^{2+} + 2\text{HS}^- \rightarrow \text{FeS}_2 + \text{H}_2. \tag{2}
\]

Sulfate reduction can take place in anoxic subsurface water, although the sediments are a more likely site because of the higher organic matter concentrations and longer exposure time there (22). Next, examine the effect of sulfate reduction on the carbonate system and therefore on atmospheric pCO₂ (schematically shown on the right side of Fig. 2). If the induced reduction in aerobic remineralization is exactly balanced by anoxic remineralization via sulfate reduction, there is no net change in remineralization, and the scenario is effectively described by reaction 2a minus reaction 1.

\[
\text{SO}_4^{2-} + \text{CO}_2 + \text{H}_2\text{O} \rightarrow \text{HS}^- + \text{HCO}_3^- + 2\text{O}_2.
\]

Fig. 1. Time-dependent results of scenario #1, a net aerobic remineralization of organic matter leading to a negative δ¹³C isotopic excursion. Time advances from left to right. (A) Prescribed carbon fluxes; the only flux prescribed to change in this scenario is the decreasing oxygenic production \( P_{\text{ox}} \) forcing the isotopic signal. (*) Anaerobic remineralization fluxes are plotted shifted and are identically zero in this scenario. (B) Dissolved organic and inorganic carbon masses (solid lines) and δ¹³C isotopic compositions (dashed). (C) Atmospheric pCO₂ (ppm) showing a large increase, due to the increase in dissolved inorganic carbon concentration, and a decrease in ocean pH.

Fig. 2. Schematic of the biologically induced snowball initiation scenarios. The right side represents the sulfate reduction plus pyrite formation pathway, which increases alkalinity and therefore reduces pCO₂; the left side represents the iron reduction path, which leads to the deposition of siderite and reduction in the size of the DIC pool, and therefore, again, to the reduction of pCO₂. Note the shoaling of the (dashed blue) interface between the anoxic and oxic ocean depth ranges, in response to the enhanced export production, potentially leading to a reduction of both oxygenic production and aerobic remineralization. These scenarios are demonstrated using a single box model described in the text.
Thus, the net reaction involves no change to the organic (CH₂O) or inorganic (CO₂, HCO₃⁻) carbon pools, but leads to a significant addition of carbonate alkalinity via the addition of HCO₃⁻. Alkalinity may be defined as net charge due to ions of weak acids involved in the carbonate system; a useful approximation for the purpose of this section is Alk = [HCO₃⁻] + 2[CO₃²⁻] + [OH⁻] − [H⁺]; see Materials and Methods for details. An interesting consequence of the above scenario is that the added alkalinity leads to a reduction of the atmospheric pCO₂, which may provide a biological mechanism for snowball initiation.

In order for a negative isotopic excursion to develop as well, a net remineralization of isotopically light organic matter is required, due to either increased remineralization rates or a drop in oxygenic production. This is a fine balance, as the net remineralization adds to the DIC pool and therefore tends to increase the pCO₂. For a reduction in atmospheric pCO₂ to accompany an isotopic signal, the increase in alkalinity due to anaerobic remineralization must exceed the increase in the size of the DIC pool. This is demonstrated using specific time-dependent model scenarios in the next section.

If the sulfide (H₂S) formed by sulfate reduction within the sediments diffuses upward into the oxygenated ocean water, and is oxidized via reaction 2b, the carbonate alkalinity gained by sulfate reduction is lost and there is no reduction in atmospheric CO₂. However, if the sulfide reacts with Fe³⁺ to form pyrite via reaction 2c within the sediments or within anoxic subsurface water masses, the alkalinity is retained. Below, we assume that 50% of the sulfide generated by bacterial sulfate reduction is removed by pyrite formation and that the rest is oxidized. Note that pyrite formation is a complex multistage process that is not completely understood. Arguments have been raised for (24–26) and against (27, 28) the reaction 2c used above, which is the net reaction of a complex multistage process. The SI Appendix, section SI-3, cites literature suggesting that this net reaction is a viable path in the presence of biological catalysts. Alternative pyrite formation scenarios to 2c may lead to the removal of alkalinity added during sulfate reduction and eliminate the pCO₂ reduction (SI Appendix, section SI-3).

Next, consider a similar scenario involving anoxic remineralization of exported organic matter into DIC by iron-respiring bacteria reducing Fe³⁺ to Fe²⁺. This reaction may again be followed by either mixing of Fe²⁺ toward the upper ocean and its oxidation back to Fe³⁺, or by siderite (FeCO₃) formation and burial. These three reactions are represented by

\[
\begin{align*}
2\text{CH}_2\text{O} + 8\text{Fe(OH)}_3 & \rightarrow 8\text{Fe}^{2+} + 2\text{HCO}_3^- + 14\text{OH}^- + 6\text{H}_2\text{O}, \\
8\text{Fe}^{2+} + 2\text{O}_2 + 20\text{H}_2\text{O} & \rightarrow 8\text{Fe(OH)}_3 + 16\text{H}^+ , \\
8\text{Fe}^{2+} + 8\text{CO}_3^{2-} & \rightarrow 8\text{FeCO}_3.
\end{align*}
\]

Dissimilatory iron reduction of organic matter [3a] leads to a large injection of sixteen carbonate alkalinity units (via the 14OH⁻ and 2HCO₃⁻ terms) per two units of remineralized organic matter—while increasing the DIC by only two (via 2HCO₃⁻). This would lead to a reduction of pCO₂, except that once the Fe⁺ is oxidized to Fe³⁺ via [3b] or reacts with the carbonate ion to form siderite via [3c], the entire alkalinity addition is lost. In the latter case, some DIC is deposited as siderite, which does lead to a reduction of pCO₂.

Next, we consider specific model calculations based on the above scenarios. Although clearly not quantitative because of the many uncertainties regarding Neoproterozoic conditions, the results below are nonetheless useful in allowing us to visualize the above scenarios and examine their consequences.

Results of a Time-Dependent Scenario

The model is described in Materials and Methods and the SI Appendix. The results of the main scenario, involving both sulfate and iron reduction, are summarized in Fig. 3. Fig. 3A shows the prescribed fluxes that drive the isotopic signal and atmospheric CO₂ drawdown. Export production is specified to increase over a time period of about 0.5 My, and then recover. In response, for the reasons explained above, both oxygenic primary production and aerobic remineralization are prescribed to decrease (dashed black and red curves). In parallel, exported organic matter is remineralized by sulfate reduction and iron reduction (dashed cyan and green).

The changes in productivity and remineralization fluxes correspond to a net remineralization, which leads to a decrease of the organic matter pool, which is converted to DIC (Fig. 3C). We find that we need to postulate a large initial organic matter pool (13), about 400 times larger than that of present day, to allow for a net remineralization event large enough to explain the observed isotopic signal. The net remineralization leads to a large isotopic excursion of DIC, 15‰ (Fig. 3C), and the isotopic compositions of the DIC covary with DIC as the latter is incorporated into newly produced DOC. This covariance is consistent with recent measurements of Neoproterozoic samples (14). Ref. 13 also assumed the DOC pool to be large, to prevent it from covarying with the DIC. This was motivated by earlier measurements indicating no such covariation (12). The carbonate system (Fig. 3B) responds to the changes in DIC, alkalinity fluxes, and enhanced DIC burial (below), leading to a significant CO₂ drawdown (Fig. 3F).

A major issue for the scenario considered here is the availability of sufficient sulfate and iron (see also ref. 29). Fig. 3D indicates that some 6 millimol per liter (mM) sulfate are needed, or, equivalently, that the maximum required sulfate flux into the ocean at the peak of the event be about four times the present-day flux. The Neoproterozoic ocean was most likely sulfate poor (30), with probably no more than about 10% of the present-day concentration of 28 mM. Recent arguments suggest higher sulfate concentrations can be maintained during ferruginous conditions (21), and are supported by sulfate evaporate deposition (31). A level of approximately 3 mM before the beginning of the event, supplemented by riverine continental flux about twice that of present day, could provide sufficient sulfate. Enhanced continental weathering due to continental collision and building of a supercontinent could provide the additional flux. Providing the implied Fe²⁺ flux for pyrite formation (solid blue curve in Fig. 3E) peaks at approximately 10 × 10⁻¹² mol/sy) seems more of a challenge. Estimates of Fe²⁺ released today by midoceanic ridges vary between 2 × 10⁻¹² mol/sy (32) and 9 × 10⁻¹² mol/sy (33). However, given the lower sulfate concentration in the Neoproterozoic, the hydrothermal Fe²⁺ concentration is expected to have been much higher (34). In addition, a somewhat higher-than-present Neoproterozoic heat flux could have lead to a higher hydrothermal water flow, consistent with trace element measurements (35) that suggest a high ratio of hydrothermal to riverine input to the ocean in the late Proterozoic. The higher heat flux also implies higher temperatures in hydrothermal systems, which could lead to a hundredfold increase in the Fe²⁺ flux (36), bringing the required Fe²⁺ flux for pyrite formation within reach. The mechanisms suggested here for an increased Fe²⁺ supply to the ocean, although speculative, are consistent with iron speciation chemistry, which suggests that beginning about 800 My ago, anoxic surface waters were commonly ferruginous (20, 21). Finally, the required Fe²⁺ flux for iron reduction (solid red in Fig. 3E) peaks at (about) 3 times present-day flux into the ocean (dashed red) and may result again from tectonically enhanced weathering associated with continental collision and building of a supercontinent (37). In addition, Fe³⁺ can accumulate in sediments before the beginning of the event and be used there by iron-reducing bacteria (38) during the event, so that the required amount of Fe³⁺ again does not seem to contradict existing information about iron availability.
The low-latitude Neoproterozoic land mass distribution (39) could make the tropical oceans especially rich in iron and phosphate carried from the continents. Much of the biological production, anoxic remineralization, and exchange of CO₂ with the atmosphere may have therefore been concentrated in low-latitude seas. In this case, the relevant ocean volume participating in setting the atmospheric CO₂ could have been much smaller. The fluxes of iron and sulfate required to affect the carbonate system of this smaller ocean volume could be significantly reduced, making the scenario more realizable.

In aerobic scenarios of DOC remineralization, ocean pH decreases because of an increase in the size of the marine DIC pool, leading to enhanced dissolution of marine carbonates. The current scenario (Fig. 3G) predicts instead an increased rate of carbonate deposition during the isotopic excursion, due to increased alkalinity and pH. Intensified DIC burial, which disperses of the newly produced DIC and allows the drawdown of atmospheric CO₂, is divided between deposition of calcium carbonate (with a corresponding decrease in Ca²⁺ concentration, Fig. 3F) and siderite.

The large isotopic signal found here is possible because of a deviation from steady-state dynamics (see a related discussion in ref. 13). If the DOC pool is not as large as assumed in ref. 13, it is likely in an isotopic quasi-equilibrium (δorg/dt ≈ 0) because of its short residence time. The isotopic compositions are then governed by (Materials and Methods) δorg = δinorg + ε and

\[ M_{\text{inorg}} \frac{d\delta_{\text{inorg}}}{dt} = M_{\text{in}} (\delta_{\text{in}} - \delta_{\text{inorg}}) - (F_{\text{prod}} - F_{\text{remin}}) \epsilon, \]

where ε = −28‰ is the fractionation between organic and inorganic matter, \( M_{\text{inorg}} \) is the DIC pool, \( F_{\text{prod}} \) is the organic matter production rate, \( F_{\text{remin}} \) is the total remineralization rate, \( F_{\text{in}} \) is the carbon flux from volcanoes and carbonate weathering, and \( \delta_{\text{in}} \) is its isotopic composition. At the minimum point of an inorganic isotopic excursion, where \( \frac{d\delta_{\text{inorg}}}{dt} = 0 \), we therefore have

\[ \delta_{\text{inorg}} = \delta_{\text{in}} - f^B \epsilon, \]

with \( f^B = (F_{\text{prod}} - F_{\text{remin}})/F_{\text{in}} \). In a steady state, \( F_{\text{prod}} - F_{\text{remin}} \) is the organic burial rate and \( f^B \) is then the organic burial fraction, \( f \). But in a non-steady-state of the DIC pool, remineralization could significantly outpace primary production, making \( f^B \) negative and large (Fig. 3H), leading to a large negative isotopic excursion (Fig. 3C) not possible in a steady state, when \( f^B = f > 0 \).

Fig. 3F shows the ocean pH increasing during the event, and the pCO₂ decreasing. Recent model estimates for the threshold CO₂ leading to a snowball vary from below present-day values to four times present-day values (40). We demonstrate that a pCO₂ reduction in conjunction with an appropriate isotopic signal is indeed possible under the specified scenario, and a much larger pCO₂ reduction is easily obtained by retuning the model. Given the enormous increase in pCO₂ in the standard aerobic remineralization scenario for explaining the isotopic signal (Fig. 1), it is remarkable that a self-consistent scenario invoking anaerobic remineralization can produce an isotopic excursion of as much as 15‰ as well as a significant decrease in pCO₂ (Fig. 3C and I). This provides a counterview to organic matter oxidation acting as a negative feedback preventing a full glaciation (41).

Carbon fluxes due to production and remineralization are prescribed rather than calculated from first principles here, because of uncertainties regarding Neoproterozoic biogeochemistry. We therefore consider in the SI Appendix, section SI-4, a fairly thorough set of sensitivity tests of our results to changes in prescribed fluxes, demonstrating the robustness of the model results to prescribed parameters.

**Discussion and Comparison to Available Observations**

This paper is motivated by a 200-My period of time, characterized by several major glacial events and isotope anomalies of distinct character. Given the simplicity of the model used here, it is best...
not to attempt to model specific glaciations and isotopic anomalies found in the geologic record. Still, the scenario considered here may explain observed large negative presnowball δ¹³C excursions, while accounting for a reduction in atmospheric pCO₂ that could lead to global glaciations. It also makes additional predictions that can be tested against the geologic record. Both the sulfate and iron reduction paths lead to an increased ocean pH (Fig. 3f). This modest pH increase represents an ocean-wide average, and could have been larger in some specific environments. Evidence of increased pH may be found in unusual centimeter-scale talc nodules formed during early diagenesis of carbonate sediments, observed to date only in mid-Proterozoic marine successions and requiring pore water pH > 8.6 (42). The increased pH also leads to a prediction of enhanced calcium carbonate deposition (Fig. 3g), consistent with the observation of widespread stromatolite formation in immediately preglacial successions (43). The model uncertainty does not allow us to determine whether the DIC deposition via siderite or carbonate precipitation may have dominated during the preglacial Proterozoic (Fig. 3g), yet both rates may be expected to be significant, in particular on anoxic continental shelves and slopes where organic carbon accumulates. Indeed shales deposited in anoxic shell environments suggest that all deposited carbonates are siderite (a few percent of total deposits) (21), although it is difficult to estimate global budgets. We do not have a record of still deeper environments, and although preserved shallow-water environments show abundance of carbonate, they show little to no siderite, perhaps because they were oxygenated. Overall, geochemical observations of later Neoproterozoic sedimentary rocks seem consistent with the requirements and predictions of the scenario considered here.

Some recent observations show the large negative isotopic δ¹³C excursions returning to positive values prior to the regional onset of glacial deposits (11, 18, 19). Moreover, the late Ediacaran Shuram anomaly is the largest in the geologic record and appears to postdate the Neoproterozoic glaciations. This raises the interesting possibility that the δ¹³C excursions and snowball events are not mechanistically linked. By changing the balance between iron reduction and sulfate reduction on one hand, and oxygenic production and export on the other, the above scenario may be modified to result in a CO₂ reduction without a δ¹³C signal, as well as an isotopic signal without CO₂ change (scenarios #5 and #6 in the SI Appendix, section SI-4; Figs. SI-5 and SI-6).

The oxygenic fixation of organic matter, followed by anaerobic remineralization, amounts to an oxygen source. The sulfide and iron oxidation act as oxygen sinks. The net oxygen source predicted here thus needs to be regulated by appropriate sinks so that the deep ocean remains anoxic for the above scenario to be valid. The implied O₂ source is significant, of the same order as present-day pyrite weathering and volcanogenic (via SO₂ gas) sink of O₂ (SI Appendix, section SI-5), seemingly allowing for the possibility of such regulation, except that weathering flux before the advent of land plants may have been as much as one order of magnitude weaker. All we can currently do is point out this significant difficulty with the scenario examined here.

Conclusions
We examined whether an enhanced export production scenario followed by anaerobic remineralization of the sinking organic matter may lead to isotopic excursions as observed before the two largest Neoproterozoic glaciations. Specifically, sulfate reduction followed by pyrite formation increases alkalinity and therefore enhances calcium carbonate precipitation. Alkalinity gained during iron reduction is lost during the siderite formation that follows, but siderite formation itself leads to DIC burial. In both cases, and unlike the explanation of the isotopic signal via aerobic remineralization, the net effect can lead to a drawdown rather than a large increase of atmospheric pCO₂, possibly explaining both the isotopic signal and snowball initiation. Previously proposed mechanisms for ice age initiation (see the Introduction) may all supplement the scenario discussed here and are not inconsistent with it.

The factors that could lead to enhanced export production, and thus initiate the above scenario, remain conjectural. It is interesting to note, however, that although eukaryotes originated early in the Proterozoic Eon, if not earlier, both fossils (44) and molecular biomarkers (45) show evidence of dramatic increase in the abundance, diversity, and environmental distribution of marine eukaryotes beginning about 800 My ago. Biogeochemical consequences potentially include higher sinking rates on continental shelves, associated with larger mean cell size and propensity to form particulate aggregates (46); higher sinking rates associated with mineralized tests and scales (45, 47); and increased biomass associated with high (relative to cyanobacteria) C:N in eukaryotic phytoplankton (48). Thus, mid-Neoproterozoic increase in the importance of marine eukaryotes could have provided marine ecosystems with an unprecedented capacity for episodic increases in export flux. Therefore, given the increased vulnerability of the Earth system to glaciation introduced by tectonic factors, epistemically enhanced increase in the export of organic matter into anoxic subsurface water masses and sediments could have pushed climate beyond the threshold for glaciations, and done so repeatedly. If later Ediacaran oceans were more broadly oxygenated (49), the biological mechanism introduced here for glacial initiation would no longer apply. The anaerobic remineralization mechanism considered here may be relevant to other carbon isotopic excursions in Earth history that did not necessarily involve the large pCO₂ increases expected from large-scale aerobic remineralization events. Although hypothetical and speculative, many aspects of the mechanisms considered here are testable, and it should be interesting to examine the geologic record in view of these ideas.

Materials and Methods
The model considers the ocean as a single volume, yet treats separately anoxic andoxic remineralization processes. The organic carbon mass (partitioned and dissolved) is affected by primary production, total remineralization and burial, \( \text{dM}_{\text{org}}/\text{dt} = \text{prod} - \text{remin} - \text{wthr} \), whereas the inorganic carbon mass is affected in addition by volcanic input, \( \text{dM}_{\text{org}}/\text{dt} = \text{F}_0 + \text{F}_{\text{remin}} - \text{F}_{\text{prod}} - \text{F}_{\text{wthr}} \). The organic and inorganic isotopic compositions are governed by \( \text{M}_{\text{org}}/\text{dt} = \text{F}_{\text{prod}}/\text{w} - \text{F}_{\text{remin}}/\text{w} \); and \( \text{M}_{\text{org}}/\text{dt} = \text{F}_{\text{prod}}/\text{w} - \text{F}_{\text{remin}}/\text{w} \), where \( \text{w} \) represents the fractionation during biological production. The model includes an expanded carbonate system with the carbonate species, \( \text{Co}_2 = \text{H}_2\text{CO}_3 \), \( \text{H}_2\text{O} = \text{H} + \text{OH}^- \), \( \text{H}_2\text{CO}_3 = \text{H} + \text{H}_2\text{CO}_3 \), \( \text{H}_2\text{CO}_3 = \text{H} + \text{CO}_3^- \); boron, \( \text{B} + \text{OH}^- = \text{H} + \text{B(OH)}_2^- \); sulfate and sulfide, \( \text{HSO}_3^- = \text{H} + \text{SO}_3^- \), \( \text{S} = \text{H} + \text{S} \); all these are solved for at every time step to round-off accuracy using Jacobian-assisted optimization (SI Appendix, section SI-2.10), and given the values of total dissolved \( \text{CO}_2 \), boron, sulfide, and sulfate and a generalized alkalinity (charge balance), all defined as follows, \( \text{C}_2 = [\text{H}_2\text{CO}_3] + [\text{H}_2\text{CO}_3] + [\text{CO}_3^-] \); \( \text{B} = [\text{B(OH)}_2^-] + [\text{OH}^-] \); \( \text{Sr} = [\text{SO}_3^-] + [\text{SO}_4^{2-}] \); \( \text{H}_2\text{S} = [\text{H}_2\text{S}] + [\text{HS}^-] + [\text{S}^-] \); \( \text{Alk}_{\text{G}} = [\text{H}_2\text{CO}_3] + 2[\text{CO}_3^-] + 2[\text{B(OH)}_2^-] + 2[\text{OH}^-] \); \( \text{CO}_2 = 2[\text{CO}_3^-] + [\text{H}^+] + [\text{OH}^-] - [\text{H}^+] \). The total CO₂ is given by the inorganic mass \( \text{M}_{\text{org}} \) per liter; total boron is specified at 400 µmol/L; total sulfide and sulfate concentrations are affected by sulfate remineralization flux, by the mixing of sulfate toward upper oxic ocean and its eventual oxidation back to sulfite, and by pyrite formation, \( \text{d}(\text{H}_2\text{S}_4)/\text{dt} = + \text{F}_{\text{remin}}/\text{SO}_2 - \text{FS}_{\text{min}} - \text{FS}_{\text{py}} \); \( \text{dS}/\text{dt} = -0.5\text{F}_{\text{remin}}/\text{SO}_2 - \text{FS}_{\text{min}} \). Generalized alkalinity sources and sinks include the input weathering flux of calcium carbonate, inorganic burial, pyrite formation, iron remineralization, and mixing followed by oxidation of iron and siderite formation, \( \text{dM}_{\text{L}}/\text{dt} = 2 \times \text{F}_{\text{remin}}/\text{Fe} - 2 \times \text{F}_{\text{prod}}/\text{Fe} - \text{prod} - \text{py}_{\text{remin}}/\text{Fe} - \text{F}_{\text{wthr}}/\text{Fe} \). The effect of the weathering flux on alkalinity input, \( \text{F}_{\text{wthr}} \), follows ref. 50. The calcium ion concentration is affected by input weathering flux and sedimentation/dissolution of CaCO₂, \( \text{dCa}^+/\text{dt} = \text{F}_{\text{wthr}}/\text{Ca} - \text{F}_{\text{wthr}}/\text{Fe} \). Iron(III) is consumed by iron remineralization and produced by mixing and oxidation of iron(II), \( \text{Fe}^{3+}/\text{dt} = -4\text{F}_{\text{remin}}/\text{Fe} + \text{FS}_{\text{min}} \). Iron(II) budget is additionally affected by siderite formation, \( \text{dFe}^{2+}/\text{dt} = 4\text{F}_{\text{remin}}/\text{Fe} - \text{Fe}_{\text{siderite}} \).
\( F_{\text{amplitude}} \). The prescribed fluxes have a Gaussian structure in time (SI Appendix, section S1-2.2). The response to step-forcing is examined in the SI Appendix, where the model is also fully described, and the response amplitude is found to be remarkably robust, although its temporal structure does depend on that of the forcing. The model code is written in Matlab and is available with the SI Appendix or at www.seas.harvard.edu/climate/el/Downloads.


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Supplementary Information for: Biologically induced snowball initiation

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SI-1. Overview
The supplementary information is divided into the model formulation (SI-2), a discussion of pyrite formation (SI-3), some additional scenarios supplementing those discussed in the main text and extensive sensitivity tests (SI-4), a calculation of the implications on the oxygen cycle (SI-5) and some back of the envelope calculations verifying model results (SI-6).

SI-2. Model formulation
We start the model description with a discussion of the carbon mass balance and isotopic mass balance equations (section SI-2.1), and then describe the specific scenario modeled here, specifying the changes to the export production, oxygenic production rate, aerobic remineralization rate and anaerobic remineralization rates (SI-2.2). The equations (dissociation reactions) for the expanded carbonate system are then described, including the carbonate system, boron, sulfate and sulfide (SI-2.3). Because the remineralization of organic matter leads to pH changes, it is essential to include the buffering effect via pH changes, it is essential to include the buffering effect via the dissolution of bottom sediments (SI-2.4). This, in turn, requires that we include the chemical weathering feedback as the dissolution of bottom sediments (SI-2.4). This, in turn, requires that we include the chemical weathering feedback as well for consistency (SI-2.5). The Ca^{2+} ion concentration may change significantly due to dissolution and deposition, and is therefore also added as a prognostic variable (SI-2.6). Next, sulfate reduction is discussed, including the pyrite formation sink for the sulfide formed by sulfate reduction (SI-2.7), and followed by iron reduction and siderite formation (SI-2.8). Several of the processes listed above contribute to carbonate alkalinity changes, which in turn plays a critical role in setting the atmospheric CO_{2} concentration, and the corresponding charge budget is presented (SI-2.9). The solution method of the expanded carbonate system is described in (SI-2.10), including both an exact numerical solution and an approximate solution which provides some intuition into the effects of the alkalinity changes due to sulfate reduction.

The model parameters that are kept constant across model scenario runs are given in Table SI-2. Model parameters that vary among the scenarios are given in Table SI-3.

SI-2.1 Mass and δ^{13}C conservation equations. The mass balances for organic (particulate and dissolved) and inorganic carbon are

\[
\begin{align*}
d\frac{\Delta M_{\text{org}}}{dt} & = F_{\text{prod}} - F_{\text{remin}} - F_{b,\text{org}} \\
d\frac{\Delta M_{\text{inorg}}}{dt} & = F_{\text{in}} + F_{\text{remin}} - F_{\text{prod}} - F_{b,\text{inorg}}
\end{align*}
\]

[SI-1]

Where \(F_{\text{prod}}\) is the rate of production of organic matter by oxyogenic photosynthesis (in units of 10^{15} kg carbon per year), while \(F_{\text{remin}}\) is the remineralization by aerobic processes, and by sulfate reduction and iron reduction. \(F_{\text{in}}\) is the flux from volcanoes and weathering, and \(F_{b,\text{org}}, F_{b,\text{inorg}}\) are the organic and inorganic burial rates. The mass balance equations for the fractions of organic and inorganic carbon that is of \(^{13}\)C isotopic composition are,

\[
\begin{align*}
\frac{d(\delta_{\text{org}} \Delta M_{\text{org}})}{dt} & = F_{\text{prod}}(\delta_{\text{inorg}} + \varepsilon) - F_{\text{remin}}\delta_{\text{org}} - F_{b,\text{org}}\delta_{\text{org}}, \\
\frac{d(\delta_{\text{inorg}} \Delta M_{\text{inorg}})}{dt} & = F_{\text{in}}\delta_{\text{in}} + F_{\text{remin}}\delta_{\text{org}} - F_{\text{prod}}(\delta_{\text{inorg}} + \varepsilon) - F_{b,\text{inorg}}\delta_{\text{inorg}}. \quad [SI-2]
\end{align*}
\]

The isotopic composition of new organic material is \(\delta_{\text{inorg}} + \varepsilon\), with \(\varepsilon < 0\). Using the above mass balance equations, the last two equations may be written as

\[
\begin{align*}
\frac{dM_{\text{org}}}{dt} & = F_{\text{prod}}(\delta_{\text{inorg}} + \varepsilon - \delta_{\text{org}}), \\
\frac{dM_{\text{inorg}}}{dt} & = F_{\text{in}}(\delta_{\text{in}} - \delta_{\text{inorg}}) - (F_{\text{prod}} - F_{\text{remin}})\varepsilon - F_{\text{remin}}(\delta_{\text{inorg}} + \varepsilon - \delta_{\text{org}}). \quad [SI-3]
\end{align*}
\]

These are the equations used to obtain the model results discussed within the paper itself. Before proceeding with the model description, consider some further simplifications that are useful in order to get some intuition into the model results. Because of the large production and remineralization fluxes, the isotopic composition of organic matter, \(\delta_{\text{org}}\), tends to be in a quasi-steady state (\(\frac{d\delta_{\text{org}}}{dt} = 0\)), while the equations for the total organic and inorganic mass and the inorganic isotopic are not necessarily in a steady state. If the inorganic isotopic composition \(\delta_{\text{inorg}}\) undergoes an excursion, then at its minimum point, where \(\frac{d\delta_{\text{inorg}}}{dt} = 0\) we have

\[
\begin{align*}
\delta_{\text{org}} & = \delta_{\text{inorg}} + \varepsilon, \\
\delta_{\text{inorg}} & = \delta_{\text{in}} - f^{\delta}\varepsilon. \quad [SI-4]
\end{align*}
\]

where

\[
\begin{align*}
f^{\delta} & = \frac{F_{\text{prod}} - F_{\text{remin}}}{F_{\text{in}}} \quad [SI-5]
\end{align*}
\]

Note that because a steady state is not assumed for the mass balance equations, \(f^{\delta}\) is not necessarily equal to the organic burial fraction. The consequences of these relations are discussed in the accompanying paper.

Reserved for Publication Footnotes
SI-2.2 Increased export production and sulfate remineralization scenario. Following standard model formulation, we specify the background (that is, steady state values before the applied perturbation to the export production) remineralization and export production as fraction of the oxygenic production flux,

\[
F_{\text{remin,0}} = \alpha_{\text{remin}} F_{\text{prod,0}}, \\
F_{\text{ep,0}} = (1 - \alpha_{\text{remin}}) F_{\text{prod,0}}, \\
F_{\text{remin}} = F_{\text{remin,0}} + F_{\text{remin,SO}_4} + F_{\text{remin,Fe}}, \\
F_{b,\text{org}} = F_{\text{ep,0}}. \tag{SI-6}
\]

Next, we specify the changes to the export production and remineralization fluxes during the expanded export production scenario. With \( U \) the amplitude of the increase to the export production, we prescribe the changes to the oxygenic production and remineralization as well as to the anoxic remineralization by sulfate reduction and iron reduction, as fractions of \( U \),

\[
F_{\text{ep}} = F_{\text{ep,0}} + UF_{\text{ep,0}} \mathcal{H}(t), \\
F_{\text{prod}} = F_{\text{prod,0}} - \gamma UF_{\text{ep,0}} \mathcal{H}(t), \\
F_{\text{remin,0}_2} = F_{\text{remin,0}} - \beta UF_{\text{ep,0}} \mathcal{H}(t), \\
F_{\text{remin,SO}_4} = \alpha UF_{\text{ep,0}} \mathcal{H}(t), \\
F_{\text{remin,Fe}} = \eta UF_{\text{ep,0}} \mathcal{H}(t). \tag{SI-7}
\]

The scaling factors \( \alpha, \beta, \gamma \) and \( \eta \) are given in tables SI-2 and SI-3. The specified transient perturbation to the different carbon fluxes first increases and then decreases. The time dependence is a Gaussian in time, chosen for simplicity and represented by \( \mathcal{H}(t) = \exp \left( -(t - t_0)^2 / \tau_{\text{ep}}^2 \right) \). Model experiments 7, 8 and 9 use instead a step-function like forcing having the same area under the curve,

\[
\mathcal{H}(t) = \begin{cases} \sqrt{\pi} / 2 & |t - t_0| < \tau_{\text{ep}} \\ 0 & \text{elsewhere} \end{cases} \tag{SI-8}
\]

which allows us to examine the model response time scale, please see discussion in section below. As seen in the accompanying paper, the perturbation to the fluxes leads to a CO2 drawdown. One expects the ensuing glacial conditions to lead to a sever perturbation to the marine biology, so that the specified dependence of the fluxes beyond that point (i.e., the decaying part of the Gaussian perturbation) is not expected to be meaningful.

SI-2.3 The expanded carbonate system. The relevant set of dissociation and dissolution reactions is,

\[
\begin{align*}
\text{CO}_2(g) &\rightleftharpoons \text{H}_2\text{CO}_3^+ \\
\text{H}_2\text{O} &\rightleftharpoons \text{H}^+ + \text{OH}^- \\
\text{H}_2\text{CO}_3^- &\rightleftharpoons \text{H}^+ + \text{HCO}_3^- \\
\text{HCO}_3^- &\rightleftharpoons \text{H}^+ + \text{CO}_3^{2-} \\
\text{B(OH)}_3 + \text{H}_2 &\rightleftharpoons \text{H}^+ + \text{B(OH)}_4^- \\
\text{HSO}_4^- &\rightleftharpoons \text{H}^+ + \text{SO}_4^{2-} \\
\text{H}_2\text{S(aq)} &\rightleftharpoons \text{HS}^- + \text{H}^+ 
\end{align*} \tag{SI-9}
\]

where \( \text{H}_2\text{CO}_3 \equiv \text{CO}_2\equiv\text{CO}_2(aq) + \text{H}_2\text{CO}_3 \), and it is assumed that the first dissociation of the sulfuric acid, \( \text{H}_2\text{SO}_4 \), is complete because it is a strong acid. The 12 unknowns are, \( \text{H}^+, \text{OH}^-, \text{CO}_2(g), \text{H}_2\text{CO}_3^+, \text{HCO}_3^-, \text{CO}_3^{2-}, \text{B(OH)}_3, \text{B(OH)}_4^-, \text{HSO}_4^- \), \( \text{SO}_4^{2-} \), \( \text{H}_2\text{S(aq)}, \text{HS}^- \). \tag{SI-10}

These are solved for using the above 7 equations of the expanded carbonate system, plus 5 constraints on the total carbon, total boron, total sulfate, total sulfide and a generalized alkalinity \( \text{Alk}_{G} \) (all of which to be calculated later via prognostic equations),

\[
\begin{align*}
\text{CT} &= [\text{H}_2\text{CO}_3^+] + [\text{HCO}_3^-] + [\text{CO}_3^{2-}], \\
\text{BT} &= [\text{B(OH)}_3] + [\text{B(OH)}_4^-], \\
\text{ST} &= [\text{HSO}_4^-] + [\text{SO}_4^{2-}], \\
(\text{HS}_2)_{\text{T}} &= [\text{H}_2\text{S(aq)}] + [\text{HS}^-], \\
\text{Alk}_{G} &= [\text{CO}_3^{2-}] + 2[\text{CO}_3^{2-}] + [\text{B(OH)}_3] + [\text{HSO}_4^-] + 2[\text{SO}_4^{2-}] + [\text{HS}^-] + [\text{OH}^-] - [\text{H}^+]. \tag{SI-11}
\end{align*}
\]

We include \( \text{SO}_4^{2-} \) and \( \text{HSO}_4^- \) in the charge balance, although the second dissociation of sulfuric acid is sufficiently complete that it could be assumed to occur completely. The contribution of variations in these terms to the variations in the charge balance turns out to be small, of the order of that due to the hydrogen ion.

SI-2.4 Dissolution and precipitation of bottom sediments. The changes in DIC concentration lead to corresponding changes to the carbonate (\( \text{CO}_3^{2-} \)) ion concentration, which may bring \( \text{CaCO}_3 \), to under or over saturation and lead to dissolution or deposition of \( \text{CaCO}_3 \) sediments. This, in turn, would affect both the total DIC and the alkalinity and as a result regulate the pH. The inorganic burial also includes siderite formation and may be formulated as follows \cite{[1]}

\[
F_{\text{b,\text{org},f}} = \frac{\text{Alk}_{G}}{\text{CaCO}_3} \text{sign}(\Delta \Omega)(\Delta \Omega)^{4.5} + F_{\text{siderite}}, \tag{SI-12}
\]

\[
\Delta \Omega \equiv \frac{[\text{CO}_3^{2-}]}{[\text{CO}_3^{2-}]_{\text{sat}}} - 1. \tag{SI-12}
\]

The subscript \( f \) in \( F_{\text{flux},f} \) is the flux \( F_{\text{flux}} \) measured in units of \( \mu \) mole carbon per liter per year instead of Peta (\( 10^{15} \)) kg carbon per year,

\[
F_{\text{flux},f} = F_{\text{flux}} \times \frac{10^{15} \text{kg C}}{\text{year}} \times \frac{1}{\text{g C} \text{liter}^{-1}} \times 83.3 \times 10^6 \mu \text{ mole C} \text{liter}^{-1} \times 60.8. \tag{SI-13}
\]

SI-2.5 Weathering. Assume that a fraction \( 0 \leq \alpha_{\text{wthr}} \leq 1 \) of the \( \text{CO}_2 \) from volcanic activity finds its way to the ocean via silicate weathering, while the rest, \( 1 - \alpha_{\text{wthr}} \), is absorbed by the ocean directly, without the accompanying \( \text{CaCO}_3 \). The weathering fraction \( \alpha_{\text{wthr}} \) is a function of the temperature, as a higher temperature leads to enhanced chemical weathering.

We parameterize the dependence of \( \alpha_{\text{wthr}} \) on temperature following Berner’s GEOCARB II model (eqn 31 in \cite{[2]})

\[
f_{B}(T) = \exp[0.090(T - T_0)] \times \left[ 1 + 0.038(T - T_0) \right]^{0.65} \tag{SI-10}
\]

where \( T_0 \) is the present-day global mean temperature. Prescribing a relation between temperature and atmospheric \( \text{CO}_2 \) we can write the above weathering feedback as function of \( \text{CO}_2 \) \cite{[2] eqn 33, neglecting fertilization effects for land plants
which did not exist yet during the Neoproterozoic, as well as solar variations),
\[ f_B(RCO_2) = (RCO_2)^{0.007 \times [1 + 0.038 \Gamma \ln(RCO_2)]^{0.65}} \]
where \( RCO_2 \) is the ratio between the pCO_2 concentration and that of present day. The sensitivity of temperature to CO_2 is given by \( \Gamma \) which is defined via,
\[ T(t) - T(0) \equiv \Gamma \ln(RCO_2), \]
so that a value of \( \Gamma = 6^\circ \)C corresponds to a 4°C warming for a doubling of CO_2. The parameterization \( f_B(RCO_2) \) is monotonically increasing as function of the pCO_2 and we set the weathering fraction to be,
\[ \alpha_{\text{wthr}}(RCO_2) = \alpha_{\text{wthr,0}} \times f_B(RCO_2). \quad [SI-14] \]
This parameter is, of course, allowed to vary only between zero and one.

**SI-2.6 Calcium ion budget.** The concentration of Ca^{2+} depends on both the sedimentation rate and the input from weathering,
\[ \frac{d}{dt}\text{Ca}^{2+} = F_{\text{in,Ca}} + \frac{2}{\tau} - F_{\text{in,org}}, \quad [SI-15] \]
Where \( F_{\text{in,Ca}} \) is a prescribed input flux (calculated using the weathering parameterization), and the second term represents the effect of sedimentation/dissolution on CaCO_3.

The calcium carbonate precipitation reaction may be written in several equivalent ways, all involving the loss of two alkali unit and one DIC unit. This has the net effect of increasing pCO_2 and, by itself, could function as a negative feedback on the scenario analyzed here. But this reaction needs to be considered together with the rest of the picture and in particular the burial of DIC via siderite formation and the addition of alkalinity via sulfat reduction followed by pyrite formation. With these processes included, the net effect presented in the scenario here is a reduction of atmospheric pCO_2.

**SI-2.7 Remineralization via sulfate reduction.** The anoxic remineralization of organic matter via sulfate (SO_4^{2-}) reduction, most likely occurring in the upper sediment layers, leads to the formation of sulfide (H_2S, or in dissociated form, HS^-) which can then either diffuse toward the oxygenated upper ocean and be oxidized there back into sulfate, or react with iron to form pyrite. These three processes may be represented by,
\[ 2\text{CH}_2\text{O} + \text{SO}_4^{2-} \rightarrow \text{HS}^- + \text{H}_2\text{O} + \text{CO}_2 + \text{HCO}_3^- , \]
\[ \text{HS}^- + 2\text{O}_2 \rightarrow \text{SO}_4^{2-} + \text{H}^+ , \]
\[ \text{Fe}^{2+} + 2\text{HS}^- \rightarrow \text{FeS}_2 + \text{H}_2. \quad [SI-16] \]
The oxidation of organic matter via sulfate reduction leads to a change in the sulfate and sulfide concentrations (as well as contributes to the mass and isotopic balances, see section SI-2.1) as follows,
\[ \frac{d}{dt}(\text{H}_2\text{S})_T = \frac{1}{2} F_{\text{rem,SO}_4^{2-}} - F_{\text{H}_2\text{S,mixing}} - F_{\text{pyrite}}, \]
\[ \frac{d}{dt} S_T = -\frac{1}{2} F_{\text{rem,SO}_4^{2-}} + F_{\text{H}_2\text{S,mixing}}. \quad [SI-17] \]
The factor of one half is needed because the oxidation of two mole of carbon involves turning one mole of sulfate into H_2S.

The mixing and pyrite formation fluxes are parameterized as,
\[ F_{\text{H}_2\text{S,mixing}} = (\text{H}_2\text{S})_T \frac{\tau_{\text{mixing}}}{\tau_{\text{pyrite}}}, \]
\[ F_{\text{pyrite}} = (\text{H}_2\text{S})_T \frac{\tau_{\text{pyrite}}}{\tau_{\text{mixing}}}. \quad [SI-18] \]
where \( \tau_{\text{mixing}} \) and \( \tau_{\text{pyrite}} \) are specified time scales for both processes, and these fluxes are in units of moles of S per unit time. In the present-day ocean nearly all (about 90%) of the sulfide formed in the sediments by sulfate reduction escapes into the ocean and is oxidized there back to sulfate. In the anoxic Neoproterozoic ocean, one expects that even some of the sulfide escaping into the water column will still form pyrite there before getting to the oxygenated upper ocean. We therefore choose the pyrite formation time scale to be equal to the mixing time scale. As a result, half of the sulfide forms pyrite and half is oxidized. Changing this ratio does not have a significant effect on the results. If more of the sulfide is oxidized into sulfate, one needs to postulate more export production of organic matter to remineralized and contribute to the alkalinity budget and CO_2 reduction. The scenario is not significantly affected otherwise and, in particular, the total required sulfate or iron, the limiting factors in this scenario as explained in the paper, do not change. Finally, note that the pyrite formation into the aerobic ocean and be oxidized there back into sulfate, or react with iron to form pyrite.

**SI-2.8 Remineralization via iron reduction.** Next, consider the anoxic remineralization of the exported organic matter by iron reducing bacteria which reduce Fe^{3+} into Fe^{2+} while remineralizing the organic matter into DIC. This reaction may again be followed by either the mixing of Fe^{2+} to the upper ocean and its oxidation back into Fe^{3+}, or by siderite (FeCO_3) formation. These three reactions are represented by,
\[ 2\text{CH}_2\text{O} + 8\text{Fe(OH)}_3 \rightarrow 8\text{Fe}^{2+} + 2\text{H}_2\text{O} + 2\text{HCO}_3^- + 14\text{OH}^- + 6\text{H}_2\text{O}, \]
\[ 8\text{Fe}^{2+} + 2\text{O}_2 + 20\text{H}_2\text{O} \rightarrow 8\text{Fe(OH)}_3 + 16\text{H}^+, \]
\[ 8\text{Fe}^{2+} + 2\text{CO}_3^{2-} \rightarrow 8\text{FeCO}_3. \quad [SI-19] \]
Fe^{2+} is soluble, and given the above stoichiometry we write an equation for its concentration, including the production by iron reduction, the loss to siderite formation and the gain from the oxidation of Fe^{3+} as follows,
\[ \frac{d}{dt}\text{Fe}^{2+} = 4F_{\text{rem,Fe}}/\tau_{\text{rem}} - F_{\text{siderite}} - F_{\text{Fe,mixing}}. \quad [SI-20] \]
Fe^{3+} is practically insoluble, it accumulates in the sediments where it can be used by iron reducing bacteria [3,4]. We need to estimate the Fe^{3+} flux required to sustain the iron remineralization. The rate of consumption of Fe^{3+} (calculated initially for convenience in units of micromole per liter per year) is given by,
\[ \frac{d}{dt}\text{Fe}^{3+} = -4F_{\text{rem,Fe}}/\tau_{\text{rem}} + F_{\text{Fe,mixing}}. \quad [SI-21] \]
and the implied needed iron flux into the ocean in moles iron per year is then obtained by multiplying the left hand side by the ocean volume in liters and converting from micromoles to moles,
\[ \text{Flux(Fe}^{3+}) = 10^{-6}V_{\text{ocean}} \frac{d}{dt}\text{Fe}^{3+}. \quad [SI-22] \]
We parameterize the rate of siderite deposition in the sediments, as well as the rate of mixing of Fe^{3+} into the aerobic upper ocean zone, where it is oxidized back to Fe^{3+}, similarly.
to the formulation of pyrite formation and sulfide oxidation in the previous subsection, in moles Fe per unit time, as,

\[ F_{\text{siderite}} = \frac{F_{\text{Fe}^{2+}}}{\tau_{\text{siderite}}} \]

\[ F_{\text{Fe,mixing}} = \frac{F_{\text{Fe}^{2+}}}{\tau_{\text{mixing}}} \] \[ \text{[SI-23]} \]

It is worth noting that the siderite formation reaction appears in the literature in different forms. Some of these, including the one used here, are,

\[ \text{Fe}^{2+} + CO_3^{2-} \rightarrow \text{FeCO}_3 \]

\[ \text{Fe}^{2+} + \text{HCO}_3^- + \text{OH}^- \rightarrow \text{FeCO}_3 + \text{H}_2\text{O} \]

\[ \text{Fe}^{2+} + 2\text{HCO}_3^- \rightarrow \text{FeCO}_3 + \text{CO}_2 + \text{H}_2\text{O} \]

While these are different reactions, it is important to note that they are completely equivalent from our perspective here. All involve the loss of two units of alkalinity (either as \( CO_3^{2-} \), \( 2\text{HCO}_3^- \), or a combination of \( \text{HCO}_3^- \) and \( \text{OH}^- \)). All three also involve the net loss of one unit of DIC (in the third reaction two units are lost on the left hand side, but one is gained back on the rhs).

\( \text{CO}_2 \), \( \text{HCO}_3^- \) and \( \text{OH}^- \) are all in equilibrium within the ocean carbonate system. Because the above three siderite formation reactions have the same effects on DIC and alkalinity, and because we equilibrate the carbonate system at every time step of the model, the three are completely equivalent and would lead to the same changes to the pH and pCO_2.

### SI-2.9 Alkalinity budget.

The weathering flux of each mole of carbon in the form of \( \text{CaCO}_3 \) is accompanied by a two mole change in alkalinity due to the double charge of \( CO_3^{2-} \). In addition, the alkalinity budget is affected by the inorganic burial of calcium carbonate which removes carbonate ions, pyrite formation eliminates sulfide ions, siderite formation eliminates carbonate ions again, and iron reduction and oxidation also affect the alkalinity as discussed above. The corresponding alkalinity budget equation is therefore,

\[
\frac{d}{dt}\text{Alk}_G = 2 \times F_{\text{weather}} \times F_{\text{in},t} - 2 \times F_{\text{inorg},t} - F_{\text{pyrite}} + 8F_{\text{rem},\text{Fe}} - 2F_{\text{mixing}} - 2F_{\text{siderite}}.
\]

[SI-24]

Note that two moles of alkalinity are lost per mole of iron deposited as siderite [SI-19]c, two moles of alkalinity are lost per mole of \( \text{Fe}^{3+} \) diffusing toward the aerobic zone and being oxidized to \( \text{Fe}^{2+} \), while 8 moles of alkalinity are gained per mole of carbon remineralized by iron reduction [SI-19]a. Also remember that \( F_{\text{pyrite}} \) is in units of moles of \( S \) per unit time rather than moles of pyrite buried per unit time.

### SI-2.10 Solving the expanded carbonate system.

In the first subsection below (SI-2.10.1) we describe the numerical algorithm for solving the full expanded carbonate system, as used in the model solutions presented above. The standard method of forming a polynomial equation and solving it iteratively is not appropriate in this case given the larger number of equations which leads to a high order polynomial. We therefore use a gradient based optimization method and provide the gradient analytically. The second subsection (SI-2.10.2) describes the solution of an approximate carbonate system which includes sulfide, yet is sufficiently simple to provide some intuition into the full solution.

#### SI-2.10.1 Numerical solution of the full expanded carbonate system.

In order to solve the carbonate system using an optimization approach, write the equations for the dissociation reactions [SI-9] as,

\[ K_w = [H^+][OH^-] \]

\[ K_0(T, S, P) = [H_2\text{CO}_3]/[\text{CO}_2(aq)] \]

\[ K_1(T, S, P) = [H^+][\text{HCO}_3^-]/[\text{H}_2\text{CO}_3] \]

\[ K_2(T, S, P) = [H^+][\text{CO}_3^{2-}]/[\text{H}_2\text{CO}_3] \]

\[ K_{\text{HSO}_4} = [H^+][\text{SO}_4^{2-}]/[\text{HSO}_4] \]

\[ K_B = [H^+][\text{B(OH)}_3]/[\text{B(OH)}_3(aq)] \]

\[ K_{H_2S,1} = [H^+][\text{HS}^-]/[\text{H}_2\text{S(aq)}] \] \[ \text{[SI-25]} \]

Where the carbonate dissociation constants are taken from [5]. Sulfate and sulfide dissociation constants are from “AquaEna” [6]. We take \( \text{pH} = -\log_{10}[\text{H}^+] \). Differences from other scales should be minor. Together with the definitions of total carbon, sulfate, sulfide, boron and alkalinity [SI-11], we write the complete set of equations in the following form,

\[
0 = F_1 = K_w - [H^+][OH^-] = F_2 = K_0(T, S, P) [\text{CO}_2(aq)] - [H_2\text{CO}_3] = F_3 = K_1(T, S, P) [H_2\text{CO}_3] - [H^+][\text{HCO}_3^-] = F_4 = K_2(T, S, P) [HCO_3^-] - [H^+][\text{CO}_3^{2-}] = F_5 = K_{\text{HSO}_4} [\text{HSO}_4] - [H^+][\text{SO}_4^{2-}] = F_6 = K_B [\text{B(OH)}_3] - [H^+][\text{B(OH)}_3] = F_7 = K_{H_2S,1} [\text{H}_2\text{S(aq)}] - [H^+][\text{HS}^-] = F_8 = [H_2\text{CO}_3] + [\text{HCO}_3^-] + [\text{CO}_3^{2-}] - C_T = F_9 = [\text{B(OH)}_3] + [\text{B(OH)}_3] - B_T = F_{10} = [\text{HSO}_4] + [\text{SO}_4^{2-}] - S_T = F_{11} = [\text{HS}^-] + [\text{H}_2\text{S(aq)}] - (H_2S)_T = F_{12} = [\text{H}_2\text{CO}_3] + 2[\text{CO}_3^{2-}] + [\text{B(OH)}_3] + [\text{HSO}_4] + 2[\text{SO}_4^{2-}] + [\text{HS}^-] + [\text{OH}^-] - [H^+] - Alk_G
\]

Ordering the vector of unknowns as shown in Table SI-1, the Jacobian (needed for the optimization solver) is,

\[
\frac{\partial F_i}{\partial X_j} = \begin{pmatrix}
\frac{\partial F_1}{\partial X_1} & \cdots & \frac{\partial F_1}{\partial X_n} \\
\vdots & \ddots & \vdots \\
\frac{\partial F_n}{\partial X_1} & \cdots & \frac{\partial F_n}{\partial X_n}
\end{pmatrix}
\]

[SI-26]

which, for the above system is again shown in Table SI-1.

For the optimization routine to work efficiently, we scale the variables and Jacobian to make all variables order one,

\[
X_i' = X_i/\text{scale}_i,
\frac{\partial F_i}{\partial X_j'} = \text{scale}_i \frac{\partial F_i}{\partial X_j}
\]

We use Matlab’s fsolve routine and the resulting solution of the expanded carbonate system is accurate to round-off error.
SI-2.10.2 Approximate solution of the expanded carbonate system

Consider an approximate solution to the carbonate+sulfide system. The approximation used here for DIC is valid only at pH values around 8, and for small perturbations to the DIC and H$_2$S. It is not used in the model calculations and is only shown in order to provide intuition into the expanded carbonate system.

Let the unknowns be the concentrations of CO$_2$(g), CO$_2$(aq), HCO$_3^-$, CO$_3^{2-}$, H$_2$S(aq), HS$^-$, H$^+$. With a total of seven unknown, we need seven equations,

\[
K_H = \frac{[CO_2(aq)]}{[CO_2(g)]},
\]

\[
K_1 = \frac{[HCO_3^-][H^+]}{[CO_2(aq)]},
\]

\[
K_2 = \frac{[CO_3^{2-}][H^+]}{[HCO_3^-]},
\]

\[
K_{SI-3} = \frac{[HS^-][H^+]}{[H_2S(aq)]},
\]

\[
C_T = [HCO_3^-] + [CO_2(g)],
\]

\[
(H_2S)_T = [HS^-] + [H_2S(aq)] \approx [HS^-],
\]

\[
Alk = [HCO_3^-] + 2[CO_3^{2-}] + [HS^-].
\]  

[SI-27]

The last three equations give,

\[
[CO_3^{2-}] = 2C_T - [Alk - (H_2S)_T] = 2C_T - AlkC,
\]

\[
[CO_2(g)] = [Alk - (H_2S)_T] - C_T = AlkC - C_T,
\]

\[
[HS^-] = (H_2S)_T,
\]

where the carbonate alkalinity is given by

\[
AlkC \equiv [HCO_3^-] + 2[CO_3^{2-}] = Alk - HS^- \approx Alk - (H_2S)_T.
\]

Using the $K_2$ equation,

\[
[H^+] = K_2 \frac{2C_T - AlkC}{AlkC - C_T},
\]

next, using the $K_1$ equation,

\[
[CO_2(aq)] = \frac{K_2 (2C_T - AlkC)^2}{K_1 AlkC - C_T},
\]

which, using Henry’s law, gives

\[
[CO_2(g)] = \frac{K_2}{K_1 K_H} \frac{(2C_T - AlkC)^2}{AlkC - C_T}. 
\]  

[SI-28]

Given that $AlkC > C_T$, the last equation makes it clear that if the carbonate alkalinity increases, the atmospheric CO$_2$ decreases.

SI-3. Pyrite formation

Pyrite, FeS$_2$, is believed to commonly form in anoxic marine sediments via a reaction of Fe$^{2+}$ with sulfide H$_2$S resulting from sulfate reduction of organic matter. The formation proceeds in two stages. The first phase [7] is the formation of brownish black amorphous Fe$^{2+}$ monosulfide, FeS,

\[
Fe^{2+} + HS^- \rightarrow FeS(s) + H^+, \quad [SI-29]
\]

which, according to [7], is actually a shorthand for,

\[
[Fe(H_2O)_6]^{2+} + HS^- \rightarrow FeS(s) + H^+ + 6H_2O.
\]

The iron monosulphide can take several forms and have different stoichiometric relations around Fe$_3$S$_2$. When it forms crystals it is exactly represented by FeS with a small (nano scale) crystal size, and is then referred to as Mackinawite [7], although this name is used for non-crystalline amorphous iron monosulfide by some authors.

The literature contains several possible scenarios and some strong disagreements regarding the second phase of pyrite formation. Some [8–10] suggest that this occurs via oxidation by elemental sulfur,

\[
FeS + S^0 \rightarrow FeS_2 \quad [SI-30]
\]

This requires a reaction for the formation of S$^0$ from H$_2$S, probably via some bacterial path [9,10]. However, [7] point out that S$^0$ is in fact S$_8$, making the above reaction an impossible multi-molecular reaction step mechanism, although the stoichiometry of the reaction may still be correct.

Alternatively, the second step may occur via an oxidation by H$_2$S,

\[
FeS + H_2S \rightarrow FeS_2 + H_2(\text{aq}) \quad [SI-31]
\]

In this case the combined pyrite formation reaction of [SI-29] and [SI-31] is

\[
Fe^{2+} + HS^- + H_2S \rightarrow FeS_2 + H_2(\text{aq}) + H^+ 
\]

which is stoichiometrically equivalent to

\[
Fe^{2+} + 2HS^- \rightarrow FeS_2 + H_2(\text{aq}). \quad [SI-32]
\]

This is the reaction used in the paper itself and it is further justified below.

Interestingly, [8] states that reaction [SI-32] “has never been observed . . . during several years of experimentation”. [11] do observe the reaction [SI-32] at 100$^\circ$C, yet [12] reject the scenario of [SI-31] and [SI-32], present experimental data showing that as long as the iron monosulfide is kept in a reducing atmosphere, devoid of any reactant other than H$_2$S, Mackinawite is the stable phase and the formation of pyrite is inhibited. They state,

Numerous experimental studies have demonstrated that at temperatures below 100$^\circ$C the conversion of unoxidized Mackinawite to pyrite is a very slow process. It was shown that this is not an important process in low temperature pyrite formation . . .

and

These new experiments have shown that in reducing H$_2$S and HS$^-$ solutions, pyrite forms at a negligible to very slow rate.

The very extensive review by [7] suggests how to resolve these contradicting results. They, and [13], first explain that the conversion of monosulfide (Mackinawite or otherwise) to pyrite is not a solid phase reaction. The oxidation of FeS to pyrite involves the dissolution of FeS to form an aqueous FeS complex, FeS(aq), which is oxidized to form FeS$_2$, which is then recrystallized as pyrite. During this process, the S(-II) is oxidized to S(II) and the Fe$^{2+}$ remains unoxidized. As an evidence that this cannot be a solid phase reaction they show that the formed crystals of pyrite are orders of magnitude larger than the original ones of Mackinawite. In this sense solid Mackinawite is not strictly a necessary precursor for pyrite formation. According to [7], pyrite formation involves two distinct physical processes, nucleation and crystal growth. Pyrite crystal growth is quite fast, but nucleation of pyrite crystals is slow and can be the rate-limiting phase in the conversion of
monosulfide to pyrite. The critical point is that the nucleation is sensitive to trace element catalysis and inhibitors. As an example of such catalytic effects on the formation of iron sulfides, [13] demonstrate the catalytic effect of aldehydic carbonyl groups (\(-\text{CHO}\)) in the formation of greigite, FeS\(_2\), from amorphous FeS via the H\(_2\)S path.

In a related paper, [14] demonstrate the sulfide path [SI-29], [SI-31] and [SI-32] under strictly anoxic conditions. They also explain that,

The metastable persistence of FeS with H\(_2\)S is well known [12, 15]. The pyrite nucleation barrier must be overcome for bulk formation of FeS\(_2\), since pyrite formation on a suitable substrate with only FeS and H\(_2\)S is fast [16]. Such substrates are reaction initiators and may include partially oxidized FeS [12], greigite, sulfur grains, bacterial cell walls [17] or pyrite [16].

The role of bacterial cell walls was demonstrated by [17] who write “In vitro enrichment cultures of dissimilatory sulfate-reducing bacteria precipitated FeS and catalyzed its transformation into FeS\(_2\) at ambient temperature and pressure under anaerobic conditions. When compared to purely abiotic processes, the bacterially mediated transformation was shown to be more efficient in transforming FeS into FeS\(_2\).”

It is important to realize that some alternative pyrite formation scenarios such as SI-30 and some others considered in the literature lead to the elimination of alkalinity added during sulfate reduction, and eliminate the pCO\(_2\) reduction predicted here. While pyrite formation is not sufficiently well understood to rule out the path used here, we do note that this issue adds uncertainty to our proposed scenario of pCO\(_2\) reduction via sulfate remineralization.

The bottom line is that in the presence of appropriate catalysts, especially organic materials of which there should be no shortage in anoxic sediments where pyrite forms, the H\(_2\)S path [SI-32] seems an appropriate representation of pyrite formation. The reason this path was not seen in many experiments is most likely that they were conducted under inorganic conditions and without the needed catalysts to accelerate the rate-limiting nucleation phase of pyrite formation. Even if one does not accept the catalyst scenario, the debate in the literature indicates that [SI-32] is considered at least by some a possible path for pyrite formation, and one is justified in considering its consequences as we do here.

**SI-3.1 The fate of hydrogen from pyrite formation.** The hydrogen produced by the pyrite formation in the anoxic sediments [SI-32] may be used by methanogens,

\[
4\text{H}_2 + \text{CO}_2 \rightarrow \text{CH}_4 + 2\text{H}_2\text{O}. \quad [\text{SI-33}]
\]

Some of the methane may accumulate in the deep ocean as methane clathrates and this reaction can therefore contribute to the reduction of the total DIC. Alternatively, some of the methane could diffuse up to the oxic upper ocean to be oxidized back to CO\(_2\),

\[
\text{CH}_4 + 2\text{O}_2 \rightarrow \text{CO}_2 + 2\text{H}_2\text{O}. \quad [\text{SI-34}]
\]

The net reaction is therefore simply

\[
4\text{H}_2 + 2\text{O}_2 \rightarrow 2\text{H}_2\text{O}, \quad [\text{SI-35}]
\]

and may be ignored as far as the effect on alkalinity or total CO\(_2\).

It is interesting to note that the above path leading to the accumulation of methane clathrates could be linked to the snowball initiation scenario of [18] if these clathrates are released to the atmosphere at some later time.

**SI-4. Additional scenarios and sensitivity study**

The parameters for the different scenarios shown here and in the main paper are all given in Tables SI-2 and SI-3. Fig. SI-1 shows fuller details of scenario #1 from the main paper, were aerobic remineralization is used to produce an isotopic signal of 15 permil and results in a very large pCO\(_2\) increase.

**SI-4.1. Additional scenarios.** Figs. SI-3 and SI-4 show scenarios #3 and #4 in which the same isotopic signal and pCO\(_2\) decrease presented in our main scenario (#2, Fig. 3 in paper) are obtain by sulfate reduction only and by iron reduction only, correspondingly. Note the larger requirements of sulfate and Fe\(^{3+}\) in these two scenarios, correspondingly.

Scenario #5 (Fig. SI-5) shows the same isotopic signal, but effectively no change in atmospheric CO\(_2\). Finally, Fig. SI-6 shows the results of scenario #6 in which the same CO\(_2\) drawdown is obtained as in our main scenario (#2, Fig. 3 in paper), but with no isotopic signal. Note that hardly any net remineralization is needed in this case.

While also being interesting on their own, taken together, these scenarios compose a set of sensitivity experiments. These experiments, together with the corresponding model parameter values in Table SI-3, demonstrate that the scenarios leading to an isotopic signal as well as a CO\(_2\) reduction are not overly sensitive to the model assumptions and occur over a robust regime of the model parameter space. However, we also perform an explicit sensitivity study of specific major parameters, as described in the following subsection.

**SI-4.2. Sensitivity study.** The set of sensitivity model experiments is summarized in Table SI-3. Scenarios 7, 8 and 9 (Figs. SI-7, SI-8, SI-9) repeat the sequence of 2, 3 and 4 (both sulfate and iron reduction, sulfate only and iron only, correspondingly), but with no isotopic signal. Note that hardly any net remineralization is needed in this case.

Scenarios 10 and 11 perturb the climate sensitivity \(\Gamma\) from its value used in the original Berner model of 4 degree C per doubling of CO\(_2\) to 5 and 3 degrees, correspondingly. The results are shown in Figs. SI-10 and SI-11, and are not overly sensitive to this parameter. Overall, silicate weathering provides a negative climate feedback: a reduction of atmospheric CO\(_2\) leads to cooling, slowing of silicate weathering reactions and therefore the delivery of alkalinity to the ocean, and thus a decrease in the rate of CO\(_2\) removal via carbonate precipitation. Larger climate sensitivity \(\Gamma\) (scenario 10) leads to stronger reduction of the minimum weathering fraction value,
to $\alpha_{wthr} = 0.53$ at the peak of the event, to a smaller alkalinity flux and therefore to a smaller corresponding CO$_2$ reduction, to 174 ppm. A smaller climate sensitivity (scenario 11) leads to a smaller reduction of the weathering fraction of $\alpha_{wthr} = 0.55$, to a larger alkalinity flux, and a corresponding CO$_2$ reduction to 134 ppm.

The parameters $\alpha$, $\beta$ and $\gamma$ control the amplitude of perturbations to the sulfate reduction remineralization, aerobic remineralization and oxygenic production, correspondingly (SI-7). These parameters are selected in the above scenarios to obtain results which seem interesting, yet their values are clearly somewhat arbitrary in our scenarios and therefore it is important to study their sensitivity, as is done in scenarios 12-17. The runs are summarized in Table SI-3 and shown in Figs. SI-12, SI-13, SI-14, SI-15, SI-16 and SI-17.

The change in the specified reduction in oxygenic production, controlled by $\gamma$, between experiments 16 and 17 is quite significant, about 25%. In response, the corresponding CO$_2$ reduction is to 100ppm in one case and to 200ppm in the other (compare scenarios 16 and 17, Figs. SI-16i and SI-17i). So while this parameter affects the results, they are clearly not overly sensitive to its value.

A change of about 30% in the sulfate remineralization rate factor $\alpha$, from 0.7 to 0.9, leads from a CO$_2$ decrease of some 200ppm, to an increase of about 100ppm (compare scenarios 12 and 13, Figs. SI-12i and SI-13i). This seems a sizable change, but is negligible relative to the CO$_2$ increase to 60,000ppm when no anaerobic remineralization is used (scenario 1). The model is also not overly sensitive to the aerobic remineralization rate factor, $\beta$ (compare scenarios 12 and 13, Figs. SI-14i and SI-15i).

SI-5. Consequences to oxygen cycle

The oxygenic fixing of organic matter, balanced by anaerobic remineralization, leads to the accumulation of oxygen in the ocean and atmosphere. On the other hand, the consumption of oxygen via sulfide oxidation and iron oxidation leads to the loss of oxygen. Consider an estimate of the magnitude of these effects and their consequences.

Begin with the oxygen production rate. The net perturbation to the aerobic remineralization and oxygenic production rates is given by (in gr C/year) $F_{net,C}(t) = \Delta F_{prod}(t) - \Delta F_{rem}(t)$, where $\Delta F_{prod}(t) = F_{prod}(t) - F_{prod}(0)$. These carbon fluxes involved in the production of oxygen are shown in Fig. SI-18a. Each net mole of fixed organic carbon leads to the production of one mole of O$_2$, so that the implied oxygen flux into the ocean and atmosphere, in moles O$_2$ per year, is $F_{O2}(t) = F_{net,C}(t)/12$, shown by the green line in Fig. SI-18b.

Next, let us address the consumption of oxygen in the scenario examined here. The two relevant reactions are those representing sulfide and iron oxidation,

$$\text{HS}^- + 2\text{O}_2 \rightarrow \text{SO}_4^{2-} + \text{H}^+,$$

$$8 \text{Fe}^{2+} + 2\text{O}_2 + 20\text{H}_2\text{O} \rightarrow 8\text{Fe(OH)}_3 + 16\text{H}^+.$$

Thus oxidizing of one mole of sulfide ion involves the loss of two moles of O$_2$, while the oxidation of eight moles of Fe$^{2+}$ also leads to the loss of two moles of O$_2$.

Combining the above oxygen sources and sinks, we can write the rate of change of oxygen (moles per liter per unit time) as follows,

$$\frac{dO_2}{dt} = \frac{1}{12} F_{net,C}(t) - \frac{2}{8} F_{Fe,\text{mixing}} - 2F_{H_2S,\text{mixing}} \quad [SI-36]$$

Note that $F_{Fe,\text{mixing}}$ is in units of moles Fe$^{2+}$ per unit time, while $F_{H_2S,\text{mixing}}$ is in units of moles S per unit time. The sources and sinks for oxygen are shown in Fig. SI-18b.

Combining these effects together, Fig. SI-18c shows the net oxygen production rate (source minus sinks) during the scenario. To maintain the oxygen concentration unperturbed, this flux would need to be balanced by sinks such as the O$_2$ sink due to weathering flux, estimated at present at about $15 \times 10^{12}$ moles O$_2$ per year [19] and shown as the green dashed line in Fig. SI-18c. The implied net oxygen source $F_{O2}(t)$ and the weathering flux seem to be of similar magnitudes, suggesting that the weathering flux and other sinks may have been able to regulate the oxygen level during the scenario. However, we need to remember that the weathering flux before the advent of land plants could have been as much as one order of magnitude weaker.

The implied oxygen source is therefore a non negligible addition to the ocean-atmosphere oxygen pool. If this leads to a significant rise in the atmospheric oxygen level, then the ocean anoxia may be reduced, affecting the assumptions behind the scenario considered here. The mechanisms maintaining the atmospheric oxygen concentration are not completely understood [19], and it is difficult to estimate therefore how efficient they would be in keeping the oxygen level down during such an injection of oxygen into the ocean and atmosphere. All we can currently do is point out this significant potential difficulty with the scenario examined here.

The ideas discussed here may be relevant to the suggestion of [20] that a pre-snowball drawdown of atmospheric oxygen into the ocean, leading to DOM oxidation and therefore to atmospheric pCO$_2$ increase, may help stabilize a slushball and prevent a hard snowball. We note that if the remineralization occurs via anaerobic processes as discussed here, followed by pyrite and siderite formation, this may lead to a drawdown of atmospheric pCO$_2$ instead.

SI-6. Sanity checks

The following order-of-magnitude checks on the results of the model help obtain some additional insight into the quantitative calculations and workings of the model, and serve as an additional check on the model results. Unless noted otherwise, we base these calculation on scenario #7 with step-like forcing, for which it is simpler to estimate the total perturbation to the forcing and the amplitude of the response, and compare to the shown results of the time dependent model calculations. All values used for the calculations below can be obtained from the shown Figures.

- **Is the change in DOC consistent with the prescribed fluxes?** The perturbations in aerobic remineralization, oxygenic production, sulfate reduction and iron reduction sum to a net remineralization rate of $1.6e-4-6.38e-4+1.1e-4=2.7e-4$ peta kg/yr for 0.604e6yr, and should lead to a 2.7e-4×1e15 kg C/yr×0.604e6yr=160e+15 kg C change in DOC, consistent with Fig. SI-7c.

- **Is the isotopic signal consistent with the amount of DOC remineralized?** Given the initial $(\delta_0)$ and final $(\delta_1)$ isotopic concentrations, we can write the isotopic mass balance for $^{13}$C as,

$$200(DOC)\times \delta_0 + 50(DIC)\times (\delta_0 + 28) = 50(DOC)\times \delta_1 + 200(DIC)\times (\delta_1 + 28)$$

which gives a change in the isotopic composition of $\delta_0 - \delta_1 = 16$, again consistent with Fig. SI-7c.

- **Charge balance/ alkalinity:** turning off the weathering feedback, dissolution and precipitation of calcium carbonate, and pyrite and siderite deposition, we verify that the
charge added via sulfate reduction is exactly balanced by changes to the carbonate, boron and sulfide charge concentration changes (Figure not shown, see scenario 18 in code files distributed with SI).

- DIC units: panel (b) of Fig 3 in the paper shows an increase in DIC concentration to be 0.208 mmole/liter (from 2.213 mmole/liter before the perturbation to 2.421 after the perturbation; the increase in the new equilibrium is due to the elimination of some of the Calcium). Panel (c) shows the increase in the total DIC to be 3.42 peta kg (from 36.38 peta kg to 39.80 peta kg). Multiplying the concentration by the ocean volume 13.7e20 liter and then by 12e-6 kg C/m mole, we see that the two diagnostics represent the same increase.

- How much oxygen is produced?

In scenario 7, oxygenic production of organic matter decreases during the event by (0.0036-0.00344)=1.6e-4 peta kg/yr; aerobic remin decreased by a larger amount of (0.003564-0.002926)=6.38e-4 peta kg/yr. Net addition to oxygenic production is therefore 4.78e-4 peta kg/yr. The perturbation lasts (1.801-1.197)=0.604 Myr, so the implied accumulated carbon is (4.78e-4 peta kg/yr)×(0.604e6 yr)=2.887e17 kg C, which is equal to (2.887×10^2 g C)/(12 g C/mole)=2.4e19 mole C. Each mole of produced organic carbon leads to the production of one mole of O_2, so we have a net O_2 production: 2.4e19 mole O_2, or a production rate of 4e13 mole O_2/year.

However, as discussed in section below, oxygen is also consumed by Fe^{2+} and H_2S oxidation. Consider these fluxes next. The time scales for pyrite formation and sulfide oxidation are the same, so that half of the sulfide formed via sulfate reduction is oxidized (see Table SI-2). Similarly, the time scales for siderite formation and Fe^{2+} oxidation are the same, so that half of the Fe^{2+} produced by iron reduction is oxidized (see Table SI-2).

First, calculate the oxygen sink due to iron mineralization. The perturbation to iron remineralization via reduction is 0.0003046-0.0002926=1.1e-4 peta kg/yr, which amounts to (1.1e-4 peta g C/yr)/(12 g C/mole)=9.17e12 mole C/year. Now, 4 moles of Fe^{2+} are produced per one mole of remineralized organic carbon (SI-19), so the above amount of 36.68e12 mole Fe(II)/year. Half of this is oxidized, and each oxidized mole of Fe(II) consumes 0.25 mole of O_2 (SI-19), so we expect the O_2 consumption rate to be 36.68e12×0.5×0.25=4.585e12 moles O_2/year, and over the perturbation period, this results in an Fe sink of (4.585e12 moles O_2/year)×(0.604e6 yr)=2.77e18 mole O_2.

Next, calculate the oxygen sink due to sulfide oxidation. The perturbation to remineralization via sulfate reduction is 0.003564-0.002926=6.38e-4 peta kg/yr, which amounts to (6.38e-4 peta g C/yr)/(12 g C/mole)=5.32e+13 mole C/year. Now, half a mole of sulfide ion HS^{-} is produced per mole of remineralized carbon (SI-16) so the above sulfate reduction rate amounts to the production of 2.66e13 mole HS^{-}/year. Half of this is oxidized, and each oxidized mole of HS^{-} requires two moles of O_2, so we expect the O_2 consumption rate to be 2.66e13 mole HS^{-}/year)×0.5×2=5.32e+13 mole O_2/year. Over the time of the perturbation, this should lead to an O_2 sink: S_{18}=2.66e13 mole O_2/year)×(0.604e6 yr)=1.61e+19 mole O_2.

The total net production of O_2 is therefore Source−S_{18}=2.4e19−2.77e18=1.61e19=5.13e18 mole O_2 over a period of 0.604 Myr, or a rate of 8.5e12 mole O_2/year. These need to be compared with the present-day atmospheric content of oxygen, about 3e19 moles, and with the present-day sink of O_2 due to weathering and volcanoes of 1.5e13 mole O_2/year. The similarity of the flux of produced oxygen and of the oxygen sink makes it not implausible that this source flux could be regulated by the sink to keep oxygen concentration at a low value.


Table SI-1. Order of variables of the expanded carbonate system, and the Jacobian [SI-26] for solving it.

\[ X = \begin{bmatrix}
H^+ & OH^- & CO_2(g) & H_2CO_3 & HCO_3^- & CO_3^{2-} & B(OH)_3 & B(OH)_4^-
\end{bmatrix} \]

\[ \left\{ \frac{\partial F_i}{\partial X_j} \right\} = \begin{bmatrix}
-\text{OH}^- & -H^+ & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0
0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0
-1 & 1 & 0 & 0 & 1 & 2 & 0 & 1 & 1 & 2 & 0 & 1
\end{bmatrix} \]

Table SI-2. Model parameters that remain constant across different runs presented in this paper.

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>( F_{in} )</td>
<td>0.15e-3 Gt C/yr</td>
<td>volcanic CO(_2) flux</td>
</tr>
<tr>
<td>( \delta_{in} )</td>
<td>-6 permil</td>
<td>volcanic ( \delta^{13} )C</td>
</tr>
<tr>
<td>( \varepsilon )</td>
<td>-28 permil</td>
<td>organic matter fractionation</td>
</tr>
<tr>
<td>( F_{prod,0} )</td>
<td>3.6e-3 Gt C/yr</td>
<td>background production rate</td>
</tr>
<tr>
<td>( \alpha_{remin} )</td>
<td>0.99</td>
<td>background remineralization fraction</td>
</tr>
<tr>
<td>( Alk_0 )</td>
<td>2300 ( \mu )mol/lit</td>
<td>scale in CaCO(_3) dissolution</td>
</tr>
<tr>
<td>( \tau_{CaCO_3} )</td>
<td>5e3 yr</td>
<td>time scale in CaCO(_3) dissolution</td>
</tr>
<tr>
<td>( \tau_{mixing} )</td>
<td>3e3 yr</td>
<td>ocean mixing time scale</td>
</tr>
<tr>
<td>( \tau_{pyrite} )</td>
<td>3e3 yr</td>
<td>pyrite formation time scale</td>
</tr>
<tr>
<td>( \tau_{siderite} )</td>
<td>3e3 yr</td>
<td>siderite formation time scale</td>
</tr>
<tr>
<td>( V_{ocean} )</td>
<td>1.37e21 liter</td>
<td>ocean volume</td>
</tr>
<tr>
<td>( \Gamma )</td>
<td>6°C</td>
<td>weathering parameter</td>
</tr>
<tr>
<td>( \tau_{ep} )</td>
<td>0.3e6 yr</td>
<td>time scale for imposed perturbation</td>
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</table>
Table SI-3. Model experiments, specifying parameters which vary among model scenarios presented in the paper and supplementary information. All values correspond to nondimensional amplitudes as follows (equations [SI-7]): $U$ is the nondimensional amplitude of the export production perturbation; $\alpha$ of the increase in sulfate reduction; $\beta$ of the drop in aerobic remineralization; $\gamma$ of the drop in oxygenic production; $\eta$ of the increase in iron remineralization.

<table>
<thead>
<tr>
<th>description</th>
<th>Fig</th>
<th>$U$</th>
<th>$\alpha$</th>
<th>$\beta$</th>
<th>$\gamma$</th>
<th>$\eta$</th>
</tr>
</thead>
<tbody>
<tr>
<td>run 1 aerobic remineralization</td>
<td>SI-1</td>
<td>13</td>
<td>0</td>
<td>0</td>
<td>1</td>
<td>0</td>
</tr>
<tr>
<td>run 2 sulfate and iron</td>
<td>SI-2</td>
<td>25</td>
<td>0.8</td>
<td>0.8</td>
<td>0.2</td>
<td>0.138</td>
</tr>
<tr>
<td>run 3 sulfate only</td>
<td>SI-3</td>
<td>73</td>
<td>1</td>
<td>1</td>
<td>0.12</td>
<td>0</td>
</tr>
<tr>
<td>run 4 iron only</td>
<td>SI-4</td>
<td>4.7</td>
<td>0</td>
<td>0</td>
<td>0.77</td>
<td>1</td>
</tr>
<tr>
<td>run 5 $\delta^{13}C$ w/o CO$_2$ signal</td>
<td>SI-5</td>
<td>25</td>
<td>0.45</td>
<td>0.8</td>
<td>0.55</td>
<td>0.138</td>
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<tr>
<td>run 6 CO$_2$ w/o $\delta^{13}C$ signal</td>
<td>SI-6</td>
<td>4.8</td>
<td>0.6</td>
<td>0.8</td>
<td>0.12</td>
<td>0.1</td>
</tr>
<tr>
<td>run 7 like 02 with step forcing</td>
<td>SI-7</td>
<td>25</td>
<td>0.8</td>
<td>0.8</td>
<td>0.2</td>
<td>0.138</td>
</tr>
<tr>
<td>run 8 like 03 with step forcing</td>
<td>SI-8</td>
<td>73</td>
<td>1</td>
<td>1</td>
<td>0.12</td>
<td>0</td>
</tr>
<tr>
<td>run 9 like 04 with step forcing</td>
<td>SI-9</td>
<td>4.7</td>
<td>0</td>
<td>0</td>
<td>0.77</td>
<td>1</td>
</tr>
<tr>
<td>run 10 $\Gamma = 5^\circ / \log(2)$</td>
<td>SI-10</td>
<td>25</td>
<td>0.8</td>
<td>0.8</td>
<td>0.2</td>
<td>0.138</td>
</tr>
<tr>
<td>run 11 $\Gamma = 3^\circ / \log(2)$</td>
<td>SI-11</td>
<td>25</td>
<td>0.8</td>
<td>0.8</td>
<td>0.2</td>
<td>0.138</td>
</tr>
<tr>
<td>run 12 sensitivity to $\alpha$</td>
<td>SI-12</td>
<td>25</td>
<td>0.7</td>
<td>0.8</td>
<td>0.2</td>
<td>0.138</td>
</tr>
<tr>
<td>run 13 sensitivity to $\alpha$</td>
<td>SI-13</td>
<td>25</td>
<td>0.9</td>
<td>0.8</td>
<td>0.2</td>
<td>0.138</td>
</tr>
<tr>
<td>run 14 sensitivity to $\beta$</td>
<td>SI-14</td>
<td>25</td>
<td>0.8</td>
<td>0.9</td>
<td>0.2</td>
<td>0.138</td>
</tr>
<tr>
<td>run 15 sensitivity to $\beta$</td>
<td>SI-15</td>
<td>25</td>
<td>0.8</td>
<td>0.7</td>
<td>0.2</td>
<td>0.138</td>
</tr>
<tr>
<td>run 16 sensitivity to $\gamma$</td>
<td>SI-16</td>
<td>25</td>
<td>0.8</td>
<td>0.8</td>
<td>0.18</td>
<td>0.138</td>
</tr>
<tr>
<td>run 17 sensitivity to $\gamma$</td>
<td>SI-17</td>
<td>25</td>
<td>0.8</td>
<td>0.8</td>
<td>0.22</td>
<td>0.138</td>
</tr>
</tbody>
</table>
Fig. SI-1. Fuller details of scenario #1 shown in Fig. 1 in the paper, with no iron or sulfate reduction, leading to an isotopic excursion of 15 permil, as well as to a dramatic increase in pCO₂. The green curve in panel (f) shows the fraction of volcanic CO₂ entering the ocean via weathering. The fraction is physically limited to the range (0,1), and in this case reached saturation as calculated following [2]. Please see caption of Fig. 3 in the paper for details.

Fig. SI-2. Scenario #2 also shown in Fig. 3 in the paper, with both iron and sulfate reduction, leading to an isotopic excursion of 15 permil, as well as to a decrease in pCO₂.
Fig. SI-3. Scenario #3, leading to the same isotopic signal and CO$_2$ drawdown as scenario #2 of Fig. 3 in the paper, but using only sulfate reduction, and no iron reduction.

Fig. SI-4. Scenario #4, leading to the same isotopic signal and CO$_2$ drawdown as scenario #2 of Fig. 3 in the paper, but using only iron reduction, and no sulfate reduction.
Fig. SI-6. Scenario #6, leading to the same pCO$_2$ drawdown as scenario #2 of Fig. 3 in the paper, but with practically no isotopic signal.

Fig. SI-5. Scenario #5, leading to the same isotopic signal as scenario #2 of Fig. 3 in the paper, but with basically no change to the atmospheric pCO$_2$. 
Fig. SI-7. Scenario #7, same as 2, but with step function forcing.

Fig. SI-8. Scenario #8, same as 3, but with step function forcing.
Fig. SI-9. Scenario #9, same as 4, but with step function forcing.
Fig. SI-10. Scenario #10, as in 2, except that climate sensitivity is set to 5 degree C per doubling of CO₂ instead of 4.

Fig. SI-11. Scenario #11, as in 2, except that climate sensitivity is set to 3 degree C per doubling of CO₂ instead of 4.
Fig. SI-12. Scenario #12, as in 2, except that sulfate remineralization rate factor is set to $\alpha = 0.7$ instead of 0.8.

Fig. SI-13. Scenario #13, as in 2, except that sulfate remineralization rate factor is set to $\alpha = 0.9$ instead of 0.8.
Fig. SI-14. Scenario #14, as in 2, except that the aerobic remineralization rate factor is set to $\beta = 0.9$ instead of 0.8.

Fig. SI-15. Scenario #15, as in 2, except that the aerobic remineralization rate factor is set to $\beta = 0.7$ instead of 0.8.
Fig. SI-16. Scenario #16, as in 2, except that the oxygenic production rate factor is set to $\gamma = 0.18$ instead of 0.2.

Fig. SI-17. Scenario #17, as in 2, except that the oxygenic production rate factor is set to $\gamma = 0.22$ instead of 0.2.
**Fig. SI-18.** Oxygen consequences of scenario #2. (a) Oxygenic production and remineralization carbon fluxes, and implied net anomalous carbon flux (anomaly in production minus anomaly in remineralization, (section SI-5). (b) Sources and sinks of oxygen due to net oxygenic organic carbon production (red), Fe$_2$ oxidation (green) and sulfide oxidation (blue). (c) Total O$_2$ source (solid green), present-day weathering sink of O$_2$ (dashed green), and the total accumulating O$_2$ due to the net carbon flux, in the absence of any sinks (solid blue).