Noise-Driven Stem Cell and Progenitor Population Dynamics

The Harvard community has made this article openly available. Please share how this access benefits you. Your story matters

<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Published Version</td>
<td><a href="http://dx.doi.org/10.1371/journal.pone.0002922">http://dx.doi.org/10.1371/journal.pone.0002922</a></td>
</tr>
<tr>
<td>Citable link</td>
<td><a href="http://nrs.harvard.edu/urn-3:HUL.InstRepos:11987421">http://nrs.harvard.edu/urn-3:HUL.InstRepos:11987421</a></td>
</tr>
<tr>
<td>Terms of Use</td>
<td>This article was downloaded from Harvard University’s DASH repository, and is made available under the terms and conditions applicable to Other Posted Material, as set forth at <a href="http://nrs.harvard.edu/urn-3:HUL.InstRepos:dash.current.terms-of-use#LAA">http://nrs.harvard.edu/urn-3:HUL.InstRepos:dash.current.terms-of-use#LAA</a></td>
</tr>
</tbody>
</table>
Noise-Driven Stem Cell and Progenitor Population Dynamics

Martin Hoffmann¹*, Hannah H. Chang²,³,⁴, Sui Huang⁵, Donald E. Ingber², Markus Loeffler⁶, Joerg Galle¹

¹ Interdisciplinary Centre for Bioinformatics, University of Leipzig, Leipzig, Germany, ² Vascular Biology Program, Department of Pathology and Surgery, Children’s Hospital and Harvard Medical School, Boston, Massachusetts, United States of America, ³ Program in Biophysics, Harvard University, Boston, Massachusetts, United States of America, ⁴ MD-PhD Program, Harvard Medical School, Boston, Massachusetts, United States of America, ⁵ Institute for Biocomplexity and Informatics, University of Calgary, Calgary, Canada, ⁶ Institute for Medical Informatics, Statistics, and Epidemiology, University of Leipzig, Leipzig, Germany

Abstract

Background: The balance between maintenance of the stem cell state and terminal differentiation is influenced by the cellular environment. The switching between these states has long been understood as a transition between attractor states of a molecular network. Herein, stochastic fluctuations are either suppressed or can trigger the transition, but they do not actually determine the attractor states.

Methodology/Principal Findings: We present a novel mathematical concept in which stem cell and progenitor population dynamics are described as a probabilistic process that arises from cell proliferation and small fluctuations in the state of differentiation. These state fluctuations reflect random transitions between different activation patterns of the underlying regulatory network. Importantly, the associated noise amplitudes are state-dependent and set by the environment. Their variability determines the attractor states, and thus actually governs population dynamics. This model quantitatively reproduces the observed dynamics of differentiation and dedifferentiation in promyelocytic precursor cells.

Conclusions/Significance: Consequently, state-specific noise modulation by external signals can be instrumental in controlling stem cell and progenitor population dynamics. We propose follow-up experiments for quantifying the imprinting influence of the environment on cellular noise regulation.

Introduction

A growing body of evidence indicates that noise is not generally detrimental to biological systems but can be employed to generate genotypic, phenotypic, and behavioral diversity [1–5]. In particular, noise-driven solutions are expected to prevail in cellular adaptation to variable environments [6]. It has been proposed that biological systems have built-in molecular devices for noise control [7–12]. These mechanisms are of specific importance in developing organisms [11,13]. This view is supported by experimental findings demonstrating that noise is down-regulated in embryonic stem cells [14,15] and that fluctuations of the transcription factor Nanog predispose these cells towards differentiation [16]. The results of the present study suggest that noise regulation can be an effective strategy in stem cell differentiation.

Stem cells are characterized by their ability to self-maintain and generate differentiated cell types and functional tissues. Moreover, they show flexibility and reversibility in their use of these options [17,18]. Populations derived from these cells, subsequently denoted as ‘stem cell populations’, comprise stem cells, progenitors, and differentiated cells. Their population structure is strongly influenced by environmental factors such as specific cell-cell interactions [19], growth factor and oxygen supply [20], as well as the geometry and mechanical properties of the local environment [21–23]. Changing these factors results in either cell death or adaptation within days [24–28]. Recently, progress has been made in the modeling and understanding of these processes on different levels of complexity [3,29–36].

Our previous studies on stem cell population dynamics focused on the reversibility and stochasticity of cellular fate decisions [37,38]. In the model of Roeder et al. [35,36,38] individual cells gain and lose stem cell properties depending on whether they localize inside or outside a specific niche environment, respectively. Thus, the environment directs the cellular fate and the reversibility of cell fate decisions is enabled by probabilistic switches between different micro-environments. The model well described several experimental data sets on the in vivo organization of normal and malignant hematopoietic stem cell populations [35,36,39]. However, even within homogeneous in vivo environments stem cells are capable of expanding and maintaining the aforementioned stem cell populations. For modeling these systems the present study expanded the ideas of Roeder et al. [35,36] by...
assuming that cells gain and loose stem cell properties according to a probabilistic process whose state-specific amplitudes are set by the environment. Within this approach cell fate decisions are basically reversible. The assumed cell state fluctuations can be hypothesized to be generated by intra- and extracellular noise triggering random transitions between different regulatory network activation patterns. This concept is in agreement with experimental findings demonstrating that epigenetic gene silencing, known to be instrumental in cell differentiation and fate control, has a strong stochastic component [40,41].

The regularity of biological development in spite of the ubiquitous presence of noise has raised the concept of a 'potential energy landscape' or 'attractor landscape' explaining cell differentiation and phenotypic diversification in terms of non-linear systems theory and non-equilibrium thermodynamics [22,42–44]. In this concept, cells visit their accessible states driven by differences in potential energy and non-state-specific, so-called additive noise. Potential minima constitute attractor states corresponding to population density maxima in steady state. The alternative concept put forward in the present study assumes that noise is predominant in most cellular states. Its essence is that the population density is determined by state-specific, so-called multiplicative noise forming a 'noise landscape', with low noise states representing the attractor states. Cells subjected to an environment not matching their internal state are assumed to be destabilized by a high noise amplitude. They subsequently adapt to this environment by traveling towards low noise states [34].

Recently, we have studied biochemically induced differentiation and dedifferentiation in promyelocytic precursor cells by measuring the inducer dose-dependent dynamics of cell differentiation as observed by the expression of a specific cell surface marker [27]. Results from our model agreed well with the experimental data, thus demonstrating the utility of our alternative description. This suggests that stem cell and progenitor population dynamics can be effectively driven by state-specific noise, thereby providing a new vista onto phenomena like stem cell maintenance, plasticity, and environmental adaptation. We propose follow-up experiments for quantifying environmental influence on cellular noise regulation.

Results

In the following paragraphs we describe our model and illustrate its general behavior for different parameter settings. Subsequently, the model is applied to a set of experimental data.

Model

The present study focuses on the degree of differentiation as the basic cellular attribute of interest. It is defined as the loss of stem cell properties and goes along with but is not identical to lineage commitment. Cell differentiation is quantified by a variable \( \alpha \) taking values between zero (full stem cell potential) and one (complete cell differentiation). Each value of \( \alpha \) may stand for a set of regulatory network activation patterns. The overabundance of these patterns as seen in gene expression profiles [30] suggests the use of a continuous variable for the degree of differentiation. Physically, \( \alpha \) depends on the abundance and sub-cellular localization of proteins and RNAs, as well as other types of signaling and metabolic molecules [45]. The \( \alpha \)-dynamics of a single cell can be modeled according to a one-dimensional Langevin equation:

\[
\frac{d\alpha}{dt} = f(\alpha) + g(\alpha)\xi(t),
\]

with \( f(\alpha) \) representing the deterministic part of the dynamics and \( g(\alpha)\xi(t) \) denoting the usual Gaussian white noise term \( \langle \xi(t) \rangle = 0, \langle \xi(t)\xi(t') \rangle = \delta(t-t') \). In applying Equation (1) one may focus on deterministically dominated \( \langle |f(\alpha)| \rangle \geq g(\alpha) \) or noise modulation-dominated \( \langle |f(\alpha)| \rangle \leq g(\alpha) \) dynamics, both of which can give the same equilibrium distribution of \( \alpha \)-values when sampled over time. In the following, we concentrate on noise modulation-dominated dynamics. Carrying the predominance of noise to an extreme we completely neglect any deterministic dynamics in our model \( f(\alpha) = 0 \), corresponding to globally equivalent deterministic potential energy states and simulate stem cell differentiation as a result of noise modulation alone.

In order to simulate population dynamics in terms of the number of cells in state \( \alpha \) we transfer the general ideas of the Langevin approach Equation (1) to a classical population dynamics model which is similar in structure to a master equation for a composite Markov process [46,47]. The model assumes each cell’s \( \alpha \)-value to randomly fluctuate according to a state-specific noise amplitude \( \sigma(\alpha) \). Starting from an initial value \( \alpha \) a cell assumes a new value \( \alpha' \) drawn from a Gaussian distribution \( p(\alpha') \) that is centered around \( \alpha \) and has standard deviation \( \sigma(\alpha) \) (see Methods). The frequency of this random transfer is determined by the randomization rate \( R(\alpha) \) defining the number of random events per time. We assume \( R(\alpha) \) to increase linearly with the cell proliferation rate \( r(\alpha) \) accounting for cell division as a major source of randomization [48]. Finally, the dynamics of the average number of cells \( N(\alpha) \) in state \( \alpha \) is governed by the random transfer towards and away from \( \alpha \), and by cell proliferation:

\[
\frac{dN(\alpha)}{dt} = \int_0^1 p(\alpha|\beta) R(\beta) N(\beta) d\beta - R(\alpha) N(\alpha) + r(\alpha) N(\alpha)
\]

with

\[
p(\alpha|\beta) \propto \exp \left( -\frac{(\alpha - \beta)^2}{2\sigma^2(\beta)} \right)
\]

and

\[
R(\alpha) = R_0 + R_1 r(\alpha).
\]

As a consequence of experimental findings [49] we replaced the proliferation term in Equation (2) by the cell cycle model of León et al. [50] assuming cell cycle progression to be a multi-step process [see Methods, Supporting Text S1, and Supporting Figures S1 and S2; five cell cycle steps were used in all simulations]. Figure 1 illustrates the general principle of state-specific (multiplicative) noise-driven dynamics. Each cell can gain or loose stem cell properties in a random event. This makes cell differentiation a reversible process in general. A stable stem cell state or terminal differentiation can be introduced by assigning zero noise levels to \( \alpha = 0 \) or \( \alpha = 1 \), respectively. Each cell will then finally end up in the respective absorbing state. However, cell proliferation is capable of sustaining a broad population distribution irrespective of individual cell fates.

Basic assumptions

Figure 2 shows simplified noise amplitudes \( \sigma(\alpha) \) and prolifera- tion rates \( r(\alpha) \). The functional form of the noise amplitudes \( \sigma(\alpha) \) is assumed to be determined by the environment. The stem cell maintaining environments S1 and S2 stabilize stem cell-like states with low \( \alpha \)-values whereas the differentiation promoting environments D1 and D2 stabilize committed states with large values of \( \alpha \) by the assignment of low noise levels. The noise amplitudes are assumed to be linear functions of \( \alpha \) for simplicity. Stem cells and
differentiated cells are generally believed to be mostly quiescent whereas progenitors are proliferative. This is reflected by the bell-shaped proliferation rates \( r(a) \) being zero at the interval boundaries and assuming their maximum value \( r_{\text{max}} > 0 \) halfway in between. However, stem cells and differentiated cells can also be assumed to proliferate in our model. As long as all proliferative states have a positive noise amplitude an initial distribution of \( a \)-values evolves towards a non-degenerate stationary distribution (see Discussion).

In the following, stem cell populations are caracterized in terms of their numerically calculated relative frequencies \( P(z_i) = N(z_i) / \sum N(x_j) \) with \( N(z_i) \) denoting the number of cells in the respective differentiation state interval centered at \( z_i \) (see Methods).

Environmental adaptation

Figure 3 shows the adaptation dynamics for two cell populations being transferred from a stem cell maintaining environment S to a differentiation promoting environment D. The timescale of the equilibration processes is of the order of days, consistent with experimental data (see below, [24–28]). In both cases, the S and D environments fully stabilize pure stem cells \( (a=0) \) and differentiated cells \( (a=1) \), respectively. However, in the S2 and D2 environments these states can hardly be accessed dynamically because the associated cumulative sum of directed steps is too small on average. This dynamical hindrance together with the stronger stabilization of proliferative progenitor states results in equilibrium distributions that are peaked at intermediate \( a \)-values. Generally, extensive low noise domains can hardly be accessed from outside these domains.

Randomization rate

The influence of the noise parameter \( R_1 \) on the frequency distribution of \( a \)-states is illustrated in the left panel of Figure 4 for the S2 environment. A high value of \( R_1 \) disperses the cells away from the most proliferating states around the mid-interval towards the noise-reduced states at low \( a \)-values. The effect of the background noise parameter \( R_0 \) is similar but without the state-specific modulation by the proliferation rate \( r(a) \). It drives the cells into the low-noise attractors when proliferation is down-regulated. This is demonstrated in the right panel of Figure 4 for different values of \( r_{\text{max}} \). The equilibrium distribution of non-proliferating cells \( (r_{\text{max}} = 0) \) would be a delta peak at \( a = 0 \). Conversely, in the absence of noise the population would converge to a delta peak at \( a = 0.5 \) when starting from an equal distribution. In summary, randomization and proliferation act as antagonists in modulating the cell state distribution, with proliferation enabling the maintenance of subpopulations in environmentally unfavored states.

Cell differentiation

Recently, we studied the transition of HL60 promyelocytic precursor cells to the neutrophil lineage after stimulation with the inducer dimethyl sulfoxide (DMSO) by monitoring the differentiation marker CD11b (Mac-1) using flow cytometry [27]. The model was applied to two experimental series. In the first series, cells were exposed to 0.75% DMSO for 7 days and monitored for CD11b expression at day 1, 3, 5, and 7 of treatment (Figure 5). In the second series, cells were exposed to DMSO concentrations of 0.0, 0.5, 0.7, 0.9, and 1.1%, respectively, with CD11b expression being measured after 7 days of treatment (Figure 6). For modeling, we mapped the logarithmic fluorescence intensities to the unit interval and identified them with the differentiation state \( a \). The functional form of the noise amplitudes as depicted in the lower

---

**Figure 1.** Multiplicative noise-driven dynamics. Upper panel: state-specific noise amplitude (standard deviation) \( \sigma(a) \) of the Gaussian conditional probability density function (cpdf) \( p(z|x) \) assumed to be a linear decreasing function of \( z \). The pictogram shows a cell with \( z = 0.4 \) being scattered towards \( z = 0.2 \) and 0.6, respectively (upper row). The subsequent scatter starting at \( z = 0.6 \) has a smaller range (lower row). This results in an average rightward drift of the peak position of the probability distribution of \( z \)-values. Lower panel: Gaussian cpdf \( p(z|x) \) as a function of \( z \) for \( \sigma = 0.4 \) (left) and \( \sigma = 0.6 \) (right). The corresponding standard deviations are \( \sigma(0.4) = 0.15 \) and \( \sigma(0.6) = 0.10 \).

**Figure 2.** Noise amplitude \( \sigma(a) \) (left) and proliferation rate \( r(a) \) (right) as a function of cell differentiation \( a \). The noise amplitude is shown for four idealized environments: i) two stem cell maintaining environments \( (S1 \text{ and } S2) \) stabilizing stem cell states and ii) two differentiation promoting environments \( (D1 \text{ and } D2) \) stabilizing differentiated states. The proliferation rate is zero (quiescence) at the interval boundaries for pure stem cells and differentiated cells, respectively, and assumes its highest values at intermediate \( a \). The maximum proliferation rates \( r_{\text{max}} = 0.1, 0.2, \text{ and } 1.0 \cdot \ln 2/d \) correspond to minimum cell cycle times of \( r_{\text{min}} = 10, 5, \text{ and } 1 \) days, respectively. Note that for exponential growth \( N(t) = N(0) e^{r_{\text{min}} t} = 2^a = 2^{rt} \).

**Figure 3.** Environmental adaptation of the population between two cell populations being transferred from a stem cell maintaining environment S to a differentiation promoting environment D. The timescale of the equilibration processes is of the order of days, consistent with experimental data (see below, [24–28]). In both cases, the S and D environments fully stabilize pure stem cells \( (a=0) \) and differentiated cells \( (a=1) \), respectively. However, in the S2 and D2 environments these states can hardly be accessed dynamically because the associated cumulative sum of directed steps is too small on average. This dynamical hindrance together with the stronger stabilization of proliferative progenitor states results in equilibrium distributions that are peaked at intermediate \( a \)-values. Generally, extensive low noise domains can hardly be accessed from outside these domains.

**Figure 4.** Randomization rate. The influence of the noise parameter \( R_1 \) on the frequency distribution of \( a \)-states is illustrated in the left panel of Figure 4 for the S2 environment. A high value of \( R_1 \) disperses the cells away from the most proliferating states around the mid-interval towards the noise-reduced states at low \( a \)-values. The effect of the background noise parameter \( R_0 \) is similar but without the state-specific modulation by the proliferation rate \( r(a) \). It drives the cells into the low-noise attractors when proliferation is down-regulated. This is demonstrated in the right panel of Figure 4 for different values of \( r_{\text{max}} \). The equilibrium distribution of non-proliferating cells \( (r_{\text{max}} = 0) \) would be a delta peak at \( a = 0 \). Conversely, in the absence of noise the population would converge to a delta peak at \( a = 0.5 \) when starting from an equal distribution. In summary, randomization and proliferation act as antagonists in modulating the cell state distribution, with proliferation enabling the maintenance of subpopulations in environmentally unfavored states.

**Figure 5.** Environmental adaptation of the population between two cell populations being transferred from a stem cell maintaining environment S to a differentiation promoting environment D. The timescale of the equilibration processes is of the order of days, consistent with experimental data (see below, [24–28]). In both cases, the S and D environments fully stabilize pure stem cells \( (a=0) \) and differentiated cells \( (a=1) \), respectively. However, in the S2 and D2 environments these states can hardly be accessed dynamically because the associated cumulative sum of directed steps is too small on average. This dynamical hindrance together with the stronger stabilization of proliferative progenitor states results in equilibrium distributions that are peaked at intermediate \( a \)-values. Generally, extensive low noise domains can hardly be accessed from outside these domains.

**Figure 6.** Randomization rate. The influence of the noise parameter \( R_1 \) on the frequency distribution of \( a \)-states is illustrated in the left panel of Figure 4 for the S2 environment. A high value of \( R_1 \) disperses the cells away from the most proliferating states around the mid-interval towards the noise-reduced states at low \( a \)-values. The effect of the background noise parameter \( R_0 \) is similar but without the state-specific modulation by the proliferation rate \( r(a) \). It drives the cells into the low-noise attractors when proliferation is down-regulated. This is demonstrated in the right panel of Figure 4 for different values of \( r_{\text{max}} \). The equilibrium distribution of non-proliferating cells \( (r_{\text{max}} = 0) \) would be a delta peak at \( a = 0 \). Conversely, in the absence of noise the population would converge to a delta peak at \( a = 0.5 \) when starting from an equal distribution. In summary, randomization and proliferation act as antagonists in modulating the cell state distribution, with proliferation enabling the maintenance of subpopulations in environmentally unfavored states.
panel of Figures 5 and 6, respectively, was designed to match the experimental data and provide a proof of principle for our approach (see Methods). The noise amplitude minima constitute attractor states corresponding to the CD11b-low-expressing, rather undifferentiated state ($\alpha = 0.4$) and the CD11b-high-expressing, rather differentiated state ($\alpha = 0.6$), respectively. The assumption of everywhere non-zero noise amplitudes implies reversible (ergodic) $\alpha$-dynamics in agreement with our experimental results (Figure 7) and the finding that certain HL60 sublines have lost the irreversibility of terminal differentiation [25]. The proliferation rate as shown in the lower panel of Figure 5 was chosen to be a hat-like function of $\alpha$ implementing a proliferation double-switch (off-on-off). Its width ensures that both the CD11b-low and CD11b-high-expressing cells divide. This is consistent with HL60 cells generally being very proliferative. Moreover, the above assumptions results in the cell population peak positions being largely independent of proliferation, in accordance with the observation that proliferation does not substantially influence HL60 cell differentiation [24,26,28]. Lowering of the proliferation rate towards the interval boundaries is required in order to reduce population density tails. This suggests that HL60 cells are almost quiescent for low and high values of $\alpha$. In addition to the above $\alpha$-dependent proliferation rate, we introduced an $\alpha$-independent apoptosis rate increasing linearly with time to account for the experimentally observed decrease in population doubling rates from 1.0 to 0.5/d for 0.0, 0.5, and 0.7% DMSO and from 1.0 to 0.2/d for 0.9 and 1.1% DMSO, respectively (unpublished data, see also Methods). Alternatively, this decrease in proliferation could result from an asymmetric proliferation rate showing a pronounced proliferation maximum for undifferentiated cells ($\alpha = 0.4$). This assumption did, however, not lead to a satisfactory model fit. Nevertheless, a minor asymmetry cannot be completely excluded since small alterations in the proliferation rate can be partly compensated by adjusting the model parameters and the fluorescence data mapping to the unit interval. This weak sensitivity with respect to the proliferation profile is a general feature of our model. The model is most sensitive to the shape of the noise profile at low noise amplitudes. The randomization rates are important for setting the time scale of the differentiation process.

The presented results demonstrate that our model is capable of quantitatively reproducing both the dynamics of the induced differentiation process (Figure 5) and the inducer dose dependence of the respective equilibrated $\alpha$-distributions (Figure 6) using consistent parameter settings. The experimental data agree with the notion of DMSO inducing an attractor state associated with cell differentiation ($\alpha = 0.6$) in a switch-like manner when raising its concentration from 0.5 to 0.7% (Figure 6). An increase in DMSO dosage beyond this point eliminates the original precursor cell attractor ($\alpha = 0.4$) in a more graduated fashion. The position of

Figure 3. Adaptation dynamics of a stem cell population after instantaneous switching from a stem cell maintaining environment S to a differentiation promoting environment D. Left panel: S1 to D1. Right panel: S2 to D2. Snapshots are taken at the time of switching and 1, 3, and 20 days, respectively, after switching. $R_0 = 0.3/d$, $R_1 = 0.9$, $r_{\text{max}} = 1.0\cdot\ln2/d$.

doi:10.1371/journal.pone.0002922.g003

Figure 4. Impact of the noise parameter $R_1$ (left panel) and the maximum proliferation rate $r_{\text{max}}$ (right panel) on the stationary distributions for the S2 environment. A high value of $R_1$ disperses the cells away from the central proliferation zone towards the more noise-reduced states. A small cellular growth as expressed by low values of $r_{\text{max}}$ lets noise dominate over proliferation even in the presence of a dynamic hindrance in approaching the noise-reduced states (see text). The parameters are identical to those of Figure 3, except for $R_1$ in the left panel and $r_{\text{max}}$ in the right panel. The equilibration period was generally 20 days. Systems with small noise amplitudes or low randomization rates may show slow dynamics. For this reason, the equilibration period was set to 60 and 120 days for $r_{\text{max}} = 0.2$ and $0.1\cdot\ln2/d$, respectively. The displayed distributions were checked to be well equilibrated by solving the equilibration condition $\partial N(\alpha)/\partial t = 0$ for $N(\alpha)$ using Broyden’s method [65].

doi:10.1371/journal.pone.0002922.g004
both attractors neither depends on time nor on DMSO dosage suggesting that DMSO activates a single noise reduction mechanism.

Differentiation-dedifferentiation hysteresis

The experimental system exhibits hysteresis in that the final distribution arrived at after 7 days of culture depends on the distribution of the initial cell population. In Figure 7 the final distribution at various DMSO doses is characterized by the fraction of cells that show a high CD11b expression. This high fraction is lower for the culture being initiated by untreated HL60 cells (forward direction) compared to HL60 cells previously treated with a high DMSO dosage for 7 days (backward direction). Stochastic systems, like the one presented here, generally evolve towards unique equilibrium distributions but may exhibit a kinetic hysteresis [47]. Figure 7 (right panel) shows the experimental and simulated high fractions (α > 0.55) demonstrating that for the same parameter settings as in Figure 6 the kinetic hysteresis displayed by our model is consistent with the experimental observations.

Population regeneration

In addition to the cell differentiation assays of the previous paragraphs we performed population regeneration (restimulation) experiments [27]. In a first experimental step cells were stimulated with 0.8% DMSO for 7 days and FACS-sorted for cells with a low CD11b expression. Subsequently, these CD11b-low-expressing cells were restimulated with the same DMSO dosage for another 7 days. We simulated FACS-sorting by retaining the fraction of cells with α ≤ 0.45 in the distributions obtained after 7 days of 0.75% DMSO treatment corresponding to the results of Figure 5. The system was then further evolved for 7 days using the same DMSO dosage conditions (Figure 8, left panel). The right panel of Figure 8 displays the fraction of CD11b-high-expressing cells (high fraction, α > 0.45) during stimulation and restimulation. While the experimental data of the primary stimulation agree quite well with the model results the cellular response to restimulation is much faster than predicted by our present one-dimensional model (priming effect, see Discussion).

Discussion

Noise is ubiquitous in biological systems and must be controlled to ensure reliable cell functioning, at least in higher multicellular organisms that feature noise-sensitive processes like alternative splicing and epigenetic regulation of gene expression. Noise regulation is most economic if applied only to those cellular states that are relevant under the prevailing environmental conditions. Noise regulation is thus expected to depend on the match between the internal state of a cell and its environment. In the present study we introduced a simple few-parameter model of stem cell and progenitor population dynamics that is explicitly based on noise regulation. Applying this model to a recent unique data set measuring various aspects of the dynamics and inducer dose dependence of stimulated differentiation in promyelocytic precursor cells [27] we demonstrate that our approach provides a
consistent description of these data including differentiation-
differentiation hysteresis as well as population regeneration.
Our results suggest that stem cell and progenitor population
dynamics can be effectively driven by state-specific noise. These
findings provide new insights into phenomena like stem cell
maintenance, plasticity, and environmental adaptation.

The model assumes that cell population dynamics result from
random fluctuations of the state of differentiation $a$. In the present
study we simply identified $a$ with the logarithmic CD11b marker
expression. More generally, measuring a number of stem cell,
differentiation or lineage markers, like promyelocytic or granu-
locyte markers in hematopoiesis, would enable a definition of the
state of differentiation as a multivariate function of the measured
markers. Clearly, changes in $a$ correspond to changes in the
combined marker expression, and thus to transitions between
complex regulatory network activation patterns. In our present
model these transitions are understood as random fluctuations
caused by molecular level noise inherent in biological systems.
Biological noise was proposed to arise from chromatin remodeling,
promoter activation, and transcription [11,31,51–55]. Moreover,
the spatial variation of molecular concentrations as well as
asymmetric partitioning of proteins during cell division can be
considered further sources of noise [45,48,56]. It has been
proposed that biological systems have built-in molecular devices
for noise control [7–12]. These control mechanisms are of specific
importance in developing organisms with the Wnt signaling
pathway as a prominent example [11,13]. Further support comes
from recent experimental findings demonstrating that noise is
down-regulated in embryonic stem cells [14,15]. The present
modeling concept assumes that state-specific noise regulation in
response to environmental signals serves as a selector of certain
differentiation states representing specific functional cellular
programs. This noise-driven selection scheme appears to be an
economic general purpose mechanism for environmental adapta-
tion and diversification since only the selected cell states need to be
noise-reduced. Stem cell differentiation in higher organisms is
controlled by epigenetic phenomena. Prominent mediators of
epigenetic reprogramming are Polycomb Group proteins [57].
Their expression level has been shown to be modulated by
environmental inputs, thus linking extracellular cues to repro-
gramming of the epigenome [58]. Together with the fact that
epigenetic gene silencing has a strong stochastic component
[40,41] this suggests environmentally regulated epigenetic pro-
cesses as effectors of noise regulation during differentiation.

The results of the present study demonstrate the capability of
our model to explain the dynamics of differentiation marker
expression in response to variable doses of soluble inducing factors
as well as the regeneration of cell populations from subpopula-
tions. Population structure and dynamics were most sensitive to
the shape of the noise profile at low noise amplitudes. Measured
proliferation rates were consistently described. Chang et al. [27]
observed that the regeneration from subpopulations under DMSO
treatment was faster for pre-stimulated cells compared to native
Our present one-dimensional model cannot describe these priming effects, thus calling for model extensions that account for multi-stable and multi-step differentiation processes in a multidimensional system as suggested in [27]. Recent results suggest that lineage choice in hematopoietic progenitor cells is indeed a multi-step process that is noise controlled [59]. The same work also demonstrates regeneration of whole populations from various subpopulations in hematopoietic systems. This supports the assumption of reversible cell differentiation underlying the present study. Simulating cell differentiation as a result of noise modulation alone is another abstraction specific to our model. In general, the deterministic part of the dynamics \( f(a) \) in the Langevin equation (1) will be different from zero. As a consequence, deterministic system behavior, as commonly modeled by chemical rate equations, will prevail in low noise states enabling more reliable cell functioning. This implication was already noted for models with constant noise amplitude [43].

The present model has been developed in particular for simulating the dynamics of stem cell and progenitor adaptation to different environments. Stem cell niches are assumed to reduce state fluctuations of stem cell-like states. Thus, the progeny of stem cells remains stem cell-like. This mimics symmetric cell division maintaining or expanding the stem cell pool. Transfer of stem cell populations into environments that promote differentiation leads to destabilization of stem cell-like states. This process can be understood as stem cell activation. In direct analogy to the destabilizing effect of noise assumed in the present study, fluctuations of Nanog, a potent stem cell regulator, were recently suggested to open temporal windows for the initiation of differentiation processes [16]. The progeny of cells in high-fluctuation states quickly diverges. This mimics asymmetric cell division. Such destabilized cells adapt to their environment by traveling towards low-fluctuation states. For near zero noise amplitudes the cells become trapped in these states for their life time rendering this adaptation process effectively irreversible.

According to our model high-fluctuation states can be kept populated by cell proliferation. Vice versa, a population-wide proliferation stop would accumulate a maximum number of cells in low-noise states. Due to the prevalence of deterministic dynamics over noise in these states, the accumulated cells should function more predictably. However, the resulting homogeneous cell population of highly specialized individuals will in general be less flexible for adaptation to unexpected environmental changes [2]. Repeated exposure to the same environmental changes could have resulted in the evolution of efficient deterministic adaptation mechanisms that do not rely on noise regulation. Such mechanisms are most likely found in simple organisms like the...
lactose and tryptophan utilization networks in E.coli and other bacteria [60–62]. However, Kashiwagi et al. [34] showed that E.coli cells equipped with a synthetic bistable gene switch actively select the attractor state that allows survival in one of two alternative nutritional environments. Through promoter swap experiments they demonstrated that this selection mechanism is not hard-wired in the E.coli genome, and thus must be non-deterministic and driven by gene expression noise.

The transfer of cells from a stem cell niche to an in vitro culture constitutes a drastic change in environmental conditions leading to a complete reorganization of the stem cell population. Similar effects are expected for the recruitment of in vivo stem cells to implanted biomedical scaffolds. A better understanding of such adaptation processes will be essential for the optimization of stem cell culture protocols and the design of injectable biomaterials [22,63,64].

Subsequent to the present studies, follow-up experiments addressing the imprinting influence of the environment on cellular noise regulation and the reversibility of stem cell development must effectively quantify noise during cellular differentiation and dedifferentiation. Future projects should thus analyze the fluctuations of stem cell marker expression in single cells while resuspended at 8–10^6 cells/ml and growing at a basal rate of 1.3–1.7 day^-1 were treated with variable concentrations of DMSO (Sigma) ranging from 0.3% to 1.25% (v/v) to induce differentiation. At each time point, cells were harvested from the suspension culture, pelleted, and processed for flow cytometry analysis.

Flow cytometry and Fluorescence Activated Cell Sorting (FACS). For the Guava-PCA system (see below) 200,000 cells were pelleted and incubated in 7 μl of CD11b/MAC-1 R-PE conjugated fluorescence antibody (BD Pharmingen) on ice for 30 min, washed with ice-cold 1% fetal calf serum/PBS/0.01% NaN₃ (NaN₃ is left out in sorting experiments), and resuspended in the same buffer at 10^6 cells/ml density for analysis. For fluorescence-activated cell sorting, staining was scaled up 10-fold to 50 μl of CD11b/MAC-1 R-PE conjugated fluorescence antibody (BD Pharmingen) per 10^6 cells and cells were resuspended at 8–10^6 cells/ml. Flow cytometry was performed on a Guava-PCA microfluidic-based flow cytometer (GuavaTechnologies, Inc). Fluorescence activated cell sorting was performed with either a Becton Dickinson FACS Vantage (Becton Dickinson) or a Becton Dickinson FACS Aria (Becton Dickinson) flow cytometer. Data analysis was done with either Cytosoft™ 2.1.1. (GuavaTechnologies, Inc) or WinMDI software. For cell sorting, starting cell number ranged between 40–90×10^6 cells, and cells were sorted into ice-cold medium for a maximum of 3 hours. Gates for sorting the CD11b-low-expressing subpopulation in the 0.8% DMSO-treated samples were set relative to an untreated, native population. The latter was also mock sorted and processed in exactly the same way as the former to control for the effects of FACS sorting on cellular expression of CD11b. To remove the staining antibody before reculturing, pelleted cells were suspended in pH 2.25 MES (morpholinoethane sulfonic acid)/Tris buffer for 30 s. A 10-fold volume of pH 7.4 PBS was immediately added for neutralization and the cells were pelleted and resuspended in culture medium. After antibody removal the cells had fluorescence signal intensities on par with unstained HL60 cells and exhibited normal viability for future immunofluorescence staining. For detailed Methods see [27].

Population Dynamics

The present modeling approach is based on the dynamics of stem cell populations stratified with respect to cell differentiation. Cell differentiation is defined through the variable $\alpha \in [0,1]$ with $\alpha = 0$ for pure stem cells and $\alpha = 1$ for fully differentiated cells. The model assumes cell differentiation to be subject to random changes defined by the conditional probability density function (cpdf) $p(\alpha|x)$ for $\alpha$ given $x$ and the randomization rate $R(x)$ quantifying the number of random events per time (Equations (2) and (3)). The cpdf $p(\alpha|x)$ is assumed to be Gaussian centered at $\alpha$ with standard deviation (noise amplitude) $\sigma(x)$. It is renormalized to unity for each $x$ to account for the truncation to the interval $[0,1]$. The noise amplitude $\sigma(x) = \sum_i q_i(x)B_i(x)$ is specified as a sum of piecewise linear or quadratic functions $q_i(x) = q_{i0} + q_{i1}(x - z_{i0}) + q_{i2}(x - z_{i0})^2$ localized by tanh-type radial basis functions $B_i(x) = b_i(x)/\sum_j b_j(x)$ with $b_i(x) = 1/2 \tanh([x-z_{i0}]/\gamma_i)^2 + 1/2 \tanh([x-z_{i0}]/\gamma_i)^2$, in which $\gamma_i$ and $\gamma_i$ denote the offset of the polynomial and the radial basis, respectively, whereas $\gamma_i$ specifies the characteristic radius, and $\gamma_i$ the transfer width of the base. The cells are assumed to proliferate according to the growth rate $r(x)$ and the time-dependent apoptosis rate $a(x)\equiv a_t (t)$ irrespective of generation. The two-dimensional rate equation for the average number of cells is numerically solved by the explicit Euler Forward Method on a 2D-grid of discrete differentiation values $x_i$, $i=1,\ldots,\rho_n$, and generation-specific cell cycle phases $k=1,\ldots,\rho_l$. According to

$$\frac{\Delta M(x_t,k)}{\Delta t} = \sum_j \rho_j(z_j|x_t) R(z_t) M(z_t,k) - R(z_t) M(z_t,k)$$

$$+ \tau(z_t) \eta_k[p(k)M(z_t,k) - \rho(k)M(z_t,k)] - a_t(k) M(z_t,k)$$ (4)

in which $\eta_k$ denotes the number of cell cycle phases per generation, $\rho(k)=2$ if $k=1$ (mod $\rho_n$) to account for cell doubling and $\rho(k)=1$ otherwise. Furthermore, $\rho(k)=0$ if $k=\rho_n$ and $\rho(k)=1$ otherwise. It is understood that $M(0,0,k-1)=0$ for $k=1$. The cell cycle terms in the second row of Equation (4) implement the continuous cell cycle model of León et al. [50] without $G_0$ phase arrest. The number of cells in generation $i$ is calculated by summing over its cell cycle phases $N(a_t,l) = \sum_{k=1}^{\rho_n} M(a_t,k)$. The dynamics of the marginal relative frequencies associated with cell differentiation can easily be derived from $P(x_t) = \rho_l \sum_{a_t} N(a_t,l)$

$\sum_{a_t} N(a_t,l)$

Truncation of the cpdf $p(\xi|x)$ to the unit interval generally results in non-symmetric scattering and thus in a non-vanishing

Theoretical Methods

In conclusion, we suggest that noise regulation can be effective in cellular development and environmental adaptation. It is expected to be relevant especially in higher multicellular organisms that comprise exposed noise-sensitive phenomena. Decoding the ‘noise landscape’ will be essential for the understanding of cell fate control and development.

Methods

Experimental Methods

Cell Culture and Differentiation. HL-60 cells (ATCC) were cultured in IMDM medium (ATCC) supplemented with 10% fetal bovine serum and 1% glutamine plus penicillin and streptomycin. Cells of passage 7 (after receipt from ATCC) at a density of 1.0×10^6 cells/ml and growing at a basal rate of 1.3–1.7 day^-1 were treated with variable concentrations of DMSO (Sigma) ranging from 0.3% to 1.25% (v/v) to induce differentiation. At each time point, cells were harvested from the suspension culture, pelleted, and processed for flow cytometry analysis.

Flow cytometry and Fluorescence Activated Cell Sorting (FACS). For the Guava-PCA system (see below) 200,000 cells were pelleted and incubated in 7 μl of CD11b/MAC-1 R-PE conjugated fluorescence antibody (BD Pharmingen) on ice for 30 min, washed with ice-cold 1% fetal calf serum/PBS/0.01% NaN₃ (NaN₃ is left out in sorting experiments), and resuspended in the same buffer at 10^6 cells/ml density for analysis. For fluorescence-activated cell sorting, staining was scaled up 10-fold to 50 μl of CD11b/MAC-1 R-PE conjugated fluorescence antibody (BD Pharmingen) per 10^6 cells and cells were resuspended at 8–10^6 cells/ml. Flow cytometry was performed on a Guava-PCA microfluidic-based flow cytometer (GuavaTechnologies, Inc). Fluorescence activated cell sorting was performed with either a Becton Dickinson FACS Vantage (Becton Dickinson) or a Becton Dickinson FACS Aria (Becton Dickinson) flow cytometer. Data analysis was done with either Cytosoft™ 2.1.1. (GuavaTechnologies, Inc) or WinMDI software. For cell sorting, starting cell number ranged between 40–90×10^6 cells, and cells were sorted into ice-cold medium for a maximum of 3 hours. Gates for sorting the CD11b-low-expressing subpopulation in the 0.8% DMSO-treated samples were set relative to an untreated, native population. The latter was also mock sorted and processed in exactly the same way as the former to control for the effects of FACS sorting on cellular expression of CD11b. To remove the staining antibody before reculturing, pelleted cells were suspended in pH 2.25 MES (morpholinoethane sulfonic acid)/Tris buffer for 30 s. A 10-fold volume of pH 7.4 PBS was immediately added for neutralization and the cells were pelleted and resuspended in culture medium. After antibody removal the cells had fluorescence signal intensities on par with unstained HL60 cells and exhibited normal viability for future immunofluorescence staining. For detailed Methods see [27].
drift term $A(x)$ as defined for the Fokker-Planck equation [47]. This term mimics a deterministic dynamic component corresponding to $f(x)$ in the Langevin equation (1). The results of the present study were checked against either using the numerically determined non-zero $A(x)$ or setting $A(x)=0$ in the equilibrated distributions. We found no notable difference except for the $S_0$ D1 transition shown in Figure 3, for which, however, also the Fokker-Planck approximation to the master equation breaks down.

Supporting Information

Text S1

Found at: doi:10.1371/journal.pone.0002922.s001 (0.03 MB DOC)

Figure S1

Cell generation distribution. Experimental data (large open circles) as adapted from Holtz et al. [1] and model results obtained by assuming a number of $n_c=1$ (filled squares) and 5 (filled circles) cell cycle steps in the proliferation model of León et al. [2]. Assuming only one cell cycle step corresponding to Equation (2) of the MM is not in agreement with the experimental data. Model parameters as in Figure 3, left panel, of the MM except for $r_{max}=1.1 \times h n_2/d$. CD34+/CD38- FACS-sorting was simulated by retaining cells with $z=0.17$ resulting in a percentage of 23% primitive progenitors. The distribution obtained by retaining all cells in the simulation (open circles) illustrates that the primitive progenitor fraction is initially depleted for fast proliferating cells.

Found at: doi:10.1371/journal.pone.0002922.s002 (0.37 MB TIF)

Figure S2

Number of cell cycle steps. Equilibrium distributions of $z$-values corresponding to Figure 4, right panel, of the MM for a number of cell cycle steps $n_c=1$, 2, 5, and 20. The larger the number of cell cycle steps $n_c$ the smaller the effective proliferation rate (compare also Figure S1) driving the cells into the most attractive state at $z=0$. The effect of $n_c$ on the $z$-dynamics saturates for high values of $n_c$ and is smaller for higher proliferation rates.

Found at: doi:10.1371/journal.pone.0002922.s003 (0.29 MB TIF)

Acknowledgments

The authors would like to thank Ingo Roeder and Ingmar Glauche for critical discussion.

Author Contributions

Conceived and designed the experiments: MH HH SH DEI ML JG. Performed the experiments: MH HH SH JG. Analyzed the data: MH HH SH JG. Wrote the paper: MH JG.

References