Earthquake Cycle Deformation in the Tibetan Plateau with a Weak Mid-Crustal Layer

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Earthquake cycle deformation in the Tibetan plateau with a weak mid-crustal layer

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[1] Geodetic observations of interseismic deformation across the Tibetan plateau contain information about both tectonic and earthquake cycle processes. Time-variations in surface velocities between large earthquakes are sensitive to the rheological structure of the subseismogenic crust, and, in particular, the viscosity of the middle and lower crust. Here we develop a semianalytic solution for time-dependent interseismic velocities resulting from viscoelastic stress relaxation in a localized midcrustal layer in response to forcing by a sequence of periodic earthquakes. Earthquake cycle models with a weak midcrustal layer exhibit substantially more near-fault preseismic strain localization than do classic two-layer models at short (<100 yr) Maxwell times. We apply both this three-layer model and the classic two-layer model to geodetic observations before and after the 1997 MW = 7.6 Manyi and 2001 MW = 7.8 Kokoxili strike-slip earthquakes in Tibet to estimate the viscosity of the crust below a 20 km thick seismogenic layer. For these events, interseismic stress relaxation in a weak (viscosity \( \leq 10^{18.5} \text{ Pa-s} \)) and thin (height \( \leq 20 \text{ km} \)) midcrustal layer explains observations of both preseismic near-fault strain localization and rapid (>50 mm/yr) postseismic velocities in the years following the coseismic ruptures. We suggest that earthquake cycle models with a localized midcrustal layer can simultaneously explain both preseismic and postseismic geodetic observations with a single Maxwell viscosity, while the classic two-layer model requires a rheology with multiple relaxation time scales.


1. Introduction

[2] Geodetic observations of surface velocities from both early and late in the earthquake cycle may provide constraints on the rheology of the subseismogenic crust and mantle. Within the Tibetan plateau, transient postseismic deformation rates up to ~100 mm/yr have been observed following the 1997 MW = 7.6 Manyi [Ryder et al., 2007] and 2001 MW = 7.8 Kokoxili earthquakes (Figure 1) [ChaoJun et al., 2009; Diao et al., 2011; Ryder et al., 2011]. These observations of time-dependent postseismic surface deformation have been explained with earthquake cycle models that relate transient surface velocities to the viscous relaxation of stresses at depth [Ryder et al., 2007, 2011]. In these viscoelastic models, stresses generated during the coseismic stage of the earthquake cycle are relaxed through viscoelastic processes at depth to produce time-dependent surface velocities throughout the interseismic period of the earthquake cycle.

Rapid postseismic deformation observed in the months following the 1997 Manyi rupture can be explained by a two-layer earthquake cycle model consisting of an elastic upper crust overlying a semi-infinite standard linear solid layer with a relatively low viscosity (~4 \( \times 10^{18} \text{ Pa-s} \)) subseismogenic layer beneath the Tibetan upper crust [Ryder et al., 2007]. The same postseismic deformation can also be explained by an elastic upper crust overlying a Maxwell rheology layer with viscosity decreasing exponentially with depth [Yamasaki and Houseman, 2012].

[3] In contrast, GPS observations from late in the earthquake cycle (preseismic) on the western Kunlun Fault, ~500 km east of the Manyi earthquake (Figure 1), have been interpreted as consistent with relatively high Maxwell viscosities [Hilley et al., 2005]. Bayesian inferences of the Maxwell relaxation times suggest that higher viscosities, ~10^{20} \text{ Pa-s}, most probably explain pre-earthquake velocity gradients near the Kunlun fault [Hilley et al., 2005]. The inference of a relatively high viscosity is based on the observation of a large interseismic GPS velocity gradient (~12 mm/yr) within ~700 km of the Kunlun fault just prior to the 2001 MW = 7.8 Kokoxili earthquake [Zhang et al., 2004]. This preseismic differential velocity is comparable to the geologically constrained long-term fault slip rate, 11.7 ± 1.5 mm/yr [Van der Woerd et al., 2002]. However, the two-layer Maxwell earthquake cycle model [Savage and Prescott, 1978] with a low viscosity of ~10^{18} \text{ Pa-s} and an earthquake recurrence interval of 300 years [Haibing et al.,

Additional supporting information may be found in the online version of this article.

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2005] predicts a differential velocity of only 1–5 mm/yr late in the earthquake cycle. This discrepancy in subseismogenic viscosity estimates is notable because similar behavior was observed before and after the Manyi and Kokoxili earthquakes. The black box across the Manyi fault shows the approximate location of interferograms before and after the earthquake [Ryder et al., 2007; Bell et al., 2011]. The black box across the Kunlun fault shows the location of the fault-parallel velocity profile (Figure 3b). Yellow circles show the locations of the four Chinese Seismological Bureau GPS stations deployed one month after the Kokoxili earthquake [ChaoJun et al., 2009].

[4] The development of models that simultaneously explain preseismic and postseismic deformation is a step toward understanding the temporal evolution of deformation and stress transfer throughout the entire earthquake cycle. Several previous earthquake cycle models in Tibet have been based on the analysis of two-layer models (Figure 2b) with an elastic upper crust (schizosphere) above a homogeneous semi-infinite Maxwell rheology viscoelastic layer (plastosphere) [Hilley et al., 2005, 2009; Ryder et al., 2007; Yamasaki and Houseman, 2012]. Here, we consider a three-layer model with a Maxwell rheology midcrustal layer embedded between an elastic upper crust and an elastic lower crust/upper mantle (Figure 2a). This three-layer model has been proposed before [Hearn, 2003; Matsura et al., 1981; Ryder et al., 2007; Segall, 2010], but has never been used to explain both postseismic and preseismic observations simultaneously.

[5] This three-layer model (Figure 2a), although simple in both geometry and rheology, is motivated by three observational arguments for the presence of a relatively weak, and perhaps low viscosity, middle or lower crustal layer in the Tibetan plateau. First, quartz textures from Bhutan suggest that the Greater Himalayan Sequence is part of an extruded, and possibly low-viscosity, channel underneath the plateau [Grujic et al., 1996, 2002]. Second, both magnetotelluric and wide-angle seismic reflection data are consistent with the presence of potentially weakening fluids at 13–18 km depth beneath the Yadong-Gulu rift in southern Tibet.

Figure 1. Interseismic GPS velocities [Zhang et al., 2004] and shaded relief map of Tibet. Velocities are shown in a nominally Asian reference frame and are color coded by magnitude with warmer colors indicating faster velocities. The yellow stars show the locations of the 1997 $M_w=7.6$ Manyi and 2001 $M_w=7.8$ Kokoxili earthquakes. The black box across the Manyi fault shows the approximate location of interferograms before and after the earthquake [Ryder et al., 2007; Bell et al., 2011]. The black box across the Kunlun fault shows the location of the fault-parallel velocity profile (Figure 3b). Yellow circles show the locations of the four Chinese Seismological Bureau GPS stations deployed one month after the Kokoxili earthquake [ChaoJun et al., 2009].

![Schematic diagrams of the (a) three-layer and (b) two-layer model geometries.](image)

Figure 2. Schematic diagrams of the (a) three-layer and (b) two-layer model geometries. The thicknesses of the elastic upper crust and viscoelastic midcrustal layer given by $H$ and $h$, respectively.
2. Geodetic Observations of Preseismic and Postseismic Deformation in Tibet

Interferometric synthetic aperture radar (InSAR) techniques have been used to measure near-fault velocities prior to [Bell et al., 2011] and following [Ryder et al., 2007] the 1997 $M_W = 7.6$ Manyi earthquake. Preseismic InSAR data across the Manyi fault [Bell et al., 2011] reveal a differential fault-parallel velocity of $\sim 3$ mm/yr within $\sim 400$ km of the fault trace in the 5 years leading up to the coseismic rupture. Here we consider the running mean of InSAR line-of-sight estimates (Figure 3a), converting range change estimates to fault parallel displacements using the reported satellite look angle of 23°, corresponding to 1 mm/yr of horizontal motion [Bell et al., 2011]. Postseismic deformation following the Manyi earthquake measured using InSAR techniques suggests an annual average velocity of $75 \pm 19$ mm/yr at a distance of $\sim 20$ km from the fault trace (supporting information) [Ryder et al., 2007].

Interseismic GPS velocities in Tibet acquired prior to the 2001 $M_W = 7.8$ Kokoxili earthquake (Figure 1) include an array of GPS stations along the Qinghai-Tibet Highway, with a simple three-layer viscoelastic earthquake cycle model to constrain the viscosity and thickness of the midcrust beneath the Kunlun fault in Tibet. To do this, we develop a two-dimensional semianalytic solution for the time-dependent evolution of interseismic deformation in response to an infinite sequence of periodic earthquakes with viscoelastic stress relaxation confined to a midcrustal layer. We quantify the trade-offs between viscoelastic layer thickness and viscosity and assess whether or not both preseismic and postseismic deformation can be adequately explained with a single-viscosity model, or if polyviscous rheologies are required. The model developed here, and viscosities estimated, are most directly comparable to two-dimensional models of the entire earthquake cycle [e.g., Savage and Prescott, 1978; Hetland and Hager, 2005; Segall, 2002; Hilley et al., 2005; Savage, 1990, 2000; Dixon et al., 2002, 2003], rather than three-dimensional models of rapid postseismic deformation alone [e.g., Ryder et al., 2007, 2011; Hearn et al., 2009; Pollitz, 2005].
which crosses the central Kunlun Fault ~200 km east of the epicenter of the 2001 Manyi event [Zhang et al., 2004]. These measurements reveal an apparently smooth preseismic velocity gradient, with a differential velocity of ~12 mm/yr within 600 km of the fault trace (Figure 3b). In the weeks following the coseismic rupture, four continuous GPS stations were deployed across the Qinghai-Tibet highway to record postseismic deformation [ChaoJun et al., 2009] including station BDGD at a distance of ~30 km from the fault trace (Figure 4). At station BDGD, the average postseismic velocity from 18 to 351 days after the earthquake was 62 ± 4 mm/yr (Figure 4) [ChaoJun et al., 2009; Diao et al., 2011]. The average annual postseismic velocity is an idealization of a set of complex observations including somewhat asymmetric deformation across the Kunlun fault, which has been hypothesized to result from lateral changes in material properties in the Qaidam basin to the north [Ryder et al., 2011]. Three-dimensional variations in fault geometry could also be responsible for this asymmetric deformation, such as the changes in dip angle that have been proposed along the Manyi fault [Funning et al., 2007].

Both of these earthquakes share preseismic velocity gradients that are localized within several hundred kilometers of the active fault trace. However, at distances less than 100 km away from the fault trace, preseismic differential velocities appear to be less than the geologically estimated long-term fault slip rate of ~11±2 mm/yr [Van der Woerd et al., 1998, 2000, 2002] in the vicinity of the Kokoxili rupture. Also common to both events is evidence for rapid near-field (<50 km from fault trace) postseismic deformation at rates exceeding five times the long-term fault slip rate.

3. Time-Dependent Viscoelastic Earthquake Cycle Models

These geodetic observations demonstrate that deformation rates between large earthquakes are not steady in time, although deformation outside of the decadal postseismic regime is often effectively approximated as such in Tibet [e.g., Bilham et al., 1997; Wallace et al., 2004; Chen et al., 2004; Meade, 2007; Burchfield et al., 2008; Loveless and Meade, 2011]. Time-dependent deformation is typically modeled as resulting from either localized deformation on a deep shear zone extending beneath the seismogenic fault and governed either by viscous or frictional behavior [e.g., Montesi, 2004] or distributed deformation in a viscoelastic layer beneath the upper crust [e.g., Hilley et al., 2005]. Here we consider only the second of these two possibilities as it bears directly on the weak layer or channel hypothesis frequently proposed for the Tibetan plateau.

![Figure 5](image.png)  
**Figure 5.** Fault parallel velocities (red) as a function of the number of past earthquakes $N$. As $N$ becomes large the solution approaches a spun-up or cycle invariant state. The viscosity here is assumed to be $10^{19}$ Pa·s with midcrustal layer thickness $h$ = 20 km and the velocity profiles are shown immediately after the most recent earthquake ($t = 0^+$).

![Figure 6](image.png)  
**Figure 6.** (a) Time-variable fault-parallel velocity profile for the three-layer model with an $H$ = 20 km thick upper crust and an $h$ = 20 km viscoelastic lower crust with a viscosity of $10^{19}$ Pa·s. (b) Time-variable fault-parallel velocity profiles for the two-layer model with a 20 km thick upper crust and a viscosity of $10^{19}$ Pa·s in the viscoelastic plastosphere. Time-independent interseismic velocity profiles from the steady elastic half-space model [Savage and Burford, 1973] are shown in blue for reference.
Figure 7. Best-fitting models and observations from before and after the Manyi earthquake for the three-layer model (red) and the two-layer model (blue). The first row shows the results for three-layer models with middle crust thickness of $h = 10$ km, and the second row shows the results of the two-layer model. The first column shows the data from before the earthquake (grey circles) [Bell et al., 2011], and the best-fitting late-in-the-earthquake cycle velocity profile from each model. Gray curves show the predicted velocity profiles for viscosities of $(10^{17}, 10^{18}, 10^{19}, 10^{20}, 10^{21})$ Pa·s. The second column shows the observed postseismic velocity (grey circle) [Ryder et al., 2007] and the best-fitting postseismic velocity profile from each model; again, grey curves show the predicted velocity profiles for the same range of viscosities as above. The third column shows the model residuals for the data before the Manyi earthquake (solid lines) as a function of viscosity, and the model residuals for the postseismic data (dotted lines). Minima of the two residuals curves are close together, $|\Delta \log \eta| = 0.3$, for the three-layer models, demonstrating that the three-layer model can explain the entire earthquake cycle with a single viscosity. By contrast, the minima of the two curves for the two-layer model are much farther apart, $|\Delta \log \eta| = 0.7$.

[11] To calculate the time-dependent velocities throughout the earthquake cycle for the three-layer model (Figure 2a), we extend previous work on representative models of vertical, infinitely long, two-dimensional, strike-slip faults. We restrict our study to two-dimensional models to facilitate comparison with these previous studies [e.g., Savage and Prescott, 1978; Hetland and Hager, 2005; Segall, 2002; Hilley et al., 2005; Savage, 1990, 2000; Dixon et al., 2002, 2003].

[12] In classic two-layer models (Figure 2b), the upper crust (schizosphere) is assumed to behave elastically and the lower crust and upper mantle beneath are modeled as a homogeneous half-space with a Maxwell viscoelastic rheology (plastosphere) [Nur and Mavko, 1974; Savage and Prescott, 1978]. The time-dependent solution for surface velocities in response to a single earthquake in a two-layer elastic model can either be obtained analytically using the method of images [e.g., Savage and Prescott, 1978; Savage, 2000] or semianalytically with propagator matrices [Ward, 1985]. With both methods, the correspondence principle is applied to transform the quasi-static viscoelastic problem into an equivalent elastic problem with a time-dependent shear modulus in the Laplace domain [e.g., Nur and Mavko, 1974; Savage and Prescott, 1978; Hetland and Hager, 2005]. For the three-layer model, in which a Maxwell viscoelastic midcrustal layer is sandwiched between an elastic upper crust and an elastic upper mantle [Ryder et al., 2007; Segall, 2010] (Figure 2a), we use the propagator matrix method [e.g., Ward, 1985; Segall, 2010] to calculate the stresses and displacements due to a dislocation while requiring stress continuity at layer interfaces [Gilbert and Backus, 1966]. Following Segall [2010], we find the solution for the response to a single earthquake in the Fourier domain for the viscoelastic three-layer model, $v_1$ (Appendix A).

[13] Due to the fact that the Kunlun fault has accumulated tens of kilometers of offset over the last ~15 Ma [Fu and Awata, 2007; Jolivet et al., 2003], the most relevant calculation is not the response to a single earthquake but rather the response to a sequence of earthquakes that give rise to large fault offsets. Assuming a sequence of periodic earthquakes with recurrence interval $T$ and exploiting the fact that the Maxwell rheology is linear, we can sum the velocities from a single earthquake, $v_1$, to obtain the response from $N$ previous earthquakes, $v_N = \sum_{t=0}^{t-N} v_1(t + jT)$, where $t$ is the time since the most recent earthquake [Savage and Prescott, 1978; Savage, 2000; Hetland and Hager, 2005, 2006a]. As the number of earthquakes $N$ increases, interseismic velocity profiles approach a cycle invariant state (Figure 5) and in the limit that $N$ goes to infinity, the cycle invariant velocities, $\bar{v}$, become,

$$\bar{v} = \Delta u (C_1 e^{-\beta_1 t} + C_2 e^{-\beta_2 t})$$

(1)

where $\Delta u$ is the coseismic offset. The coefficients ($C_1$, $C_2$) and relaxation times ($\beta_1$, $\beta_2$) in equation (1) are complicated
functions of midcrustal viscoelastic layer thickness, depth of the upper elastic layer, depth to which the coseismic rupture extends, Maxwell time, earthquake recurrence interval, and wave number (Appendix A). Matlab code implementing this solution is given in the supporting information. This spun-up three-layer solution shares the layer-like geometry of previous three-dimensional models of postseismic deformation [Ryder et al., 2007] and the dual relaxation times of the single earthquake solution [Segall, 2010], but differs in that in addition to predicting near-fault postseismic variations it also satisfies the far-field plate motion constraints (Figure 6a).

[14] The reason that the spun-up three-layer model satisfies the plate motion boundary condition at a distance closer to the fault trace than does the two-layer model (Figure 6b) is that coseismically generated elastic displacements in the lowest (mantle-like) layer are slowly restored to their initial positions. This elastic rebound of the mantle induces flow at the base of the viscoelastic layer in the direction opposite to the sense of coseismic slip. The reverse flow at the base of the viscoelastic layer in turn limits the magnitude and spatial extent of interseismic velocities in the midcrustal layer, with the largest effects near the fault trace where the coseismic stresses in the mantle layer are largest. As a result, for the same viscosity, the three-layer model velocity gradients are more localized across the fault than those of the two-layer model [Hearn, 2003].

[15] To illustrate the differences in behavior between the two- and three-layer models, we consider a simple synthetic example of a fault slipping at a rate $s_0$ mm/yr with a recurrence interval of $T=300$ years. Fault-parallel velocity profiles for both the two- and three-layer models are calculated with a viscosity of $\eta=10^{19}$ Pa·s and a layer thickness of $h=20$ km is assumed for the three-layer model (Figure 6). Both models produce rapid pulses of deformation immediately after an earthquake where the near-fault velocities may exceed the long-term differential velocity by a factor of five or more (Figures 6). The primary difference between the two- and three-layer models is that late in the earthquake cycle, the two-layer model has a differential velocity of $<0.6 s_0$ mm/yr across a 600 km fault-perpendicular transect, while the three-layer model solution maintains a velocity gradient of $\sim 1 s_0$ mm/yr across same transect, equivalent to the long-term fault slip rate, $s_0$ (Figure 6). The two-layer model with a small recurrence interval or large viscosity can maintain a comparable near-field velocity gradient across a ~600 km fault-perpendicular transect, but at the cost of a much smaller magnitude ($<2 s_0$ mm/yr) pulse of postseismic deformation [Savage and Prescott, 1978]. Additionally, postseismic deformation is more limited in spatial extent in the three-layer model (within ~200 km of the fault trace) than in the two-layer model (Figure 6).

### Table 1. Summary of Preseismic and Postseismic Geodetic Velocities and Inferred Viscosity Estimates for Both Two- and Three-Layer Models

<table>
<thead>
<tr>
<th>Layer Type</th>
<th>$\Delta v$ (200 km)</th>
<th>$\Delta v$ (600 km)</th>
<th>Postseismic velocity</th>
<th>$\Delta \log \eta$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Preseismic</td>
<td>$3 \pm 1$ mm/yr $^a$</td>
<td>-</td>
<td>$12 \pm 2$ mm/yr $^b$</td>
<td>-</td>
</tr>
<tr>
<td>Postseismic</td>
<td>$75 \pm 19$ mm/yr $^c$</td>
<td>$62 \pm 4$ mm/yr $^d$</td>
<td>$10^{18.4}$ Pa·s $^e$</td>
<td>$10^{18.8}$ Pa·s</td>
</tr>
<tr>
<td>2-Layer preseismic $\eta$</td>
<td>$10^{19.1}$ Pa·s</td>
<td>$10^{18.6}$ Pa·s</td>
<td></td>
<td></td>
</tr>
<tr>
<td>2-Layer postseismic $\eta$</td>
<td>$10^{18.4}$ Pa·s</td>
<td>$10^{18.8}$ Pa·s</td>
<td></td>
<td></td>
</tr>
<tr>
<td>3-Layer preseismic $\eta$</td>
<td>$10^{17.7}$ Pa·s</td>
<td>$10^{17.5}$ Pa·s</td>
<td></td>
<td></td>
</tr>
<tr>
<td>3-Layer postseismic $\eta$</td>
<td>$10^{18.0}$ Pa·s</td>
<td>$10^{17.9}$ Pa·s</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

The preseismic $\Delta v$ is the differential velocity over apertures of 200 and 600 km wide for the Manyi and Kokoxili cases respectively (Figure 3). For the three-layer case the midcrustal thickness is assumed to be $h=10$ km, with other layer thickness models in the Appendix.

$^a$Bell et al. [2011].
$^b$Zhang et al. [2004].
$^c$Ryder et al. [2007].
$^d$ChaoJun et al. [2009].
fault slip rate, and effective fault locking depth. Geologic observations of long-term terraces and channel offsets have been used to suggest a recurrence interval of 300±50 years for ruptures similar to the Kokoxili event [Haibling et al., 2005]. We also assume a slip rate on the Kunlun fault of 10 mm/yr, consistent with Pleistocene slip rates on the central and western Kunlun fault of ~11 ± 2 mm/yr [Van der Woerd et al., 1998, 2000, 2002] and 6.5–8.7 ± 1.8 mm/yr [Cowgill et al., 2009]. We take \( s_0 = 10 \) mm/yr as a representative fault slip rate and \( T = 300 \) years as the average earthquake recurrence interval. We assume that the slip rate and recurrence interval on the Manyi fault splay are identical to those along the central Kunlun fault (94'E) as we are unaware of any currently published local constraints on these parameters. Furthermore, we assume an effective locking depth of \( D = 20 \) km, consistent with estimates of coseismic slip during the earthquakes [e.g., Antolik et al., 2004; Lasserre et al., 2005; Funning et al., 2007] and the fact that most major earthquakes rupture the entire upper crust.

For the three-layer model with a 10 km thick midcrustal layer, the preseismic and postseismic data from the Manyi earthquake are best explained by a viscosity of \( \sim 10^{17.8} \) Pa-s (Figure 7, supporting information). The minimum postseismic residual is \( <1 \) mm/yr with viscosity \( \eta = 10^{18.0} \) Pa-s and the minimum preseismic sum of residuals is 12 mm/yr with viscosity \( \eta = 10^{17.7} \) Pa-s. The goodness-of-fit decreases markedly for models using the same layer thickness (\( h = 10 \) km) but a viscosity of \( \eta = 10^{21.0} \) Pa-s, where the residuals increase to \( \sim 63 \) mm/yr (preseismic) and \( \sim 72 \) mm/yr (postseismic). In contrast, the two-layer model requires a viscosity of \( 10^{18.4} \) Pa-s to explain the Manyi earthquake postseismic data equally well (minimum postseismic residual of \( <1 \) mm/yr), and a significantly higher viscosity, \( 10^{19.5} \) Pa-s, to explain the preseismic data (minimum preseismic sum of residuals of 12 mm/yr; Figure 7 and Table 1). The difference between the best-fit viscosity for the preseismic velocities and the best-fit viscosity for the postseismic velocities can be described by the quantity \( |\Delta \log \eta| \), where the residuals increase to \( \sim 63 \) mm/yr (preseismic) and \( \sim 72 \) mm/yr (postseismic).

Furthermore, we assume an effective locking depth of \( h = 20 \) km, consistent with estimates of coseismic slip during the earthquakes [e.g., Antolik et al., 2004; Lasserre et al., 2005; Funning et al., 2007] and the fact that most major earthquakes rupture the entire upper crust.

For the Kokoxili earthquake, 500 km to the east of the Manyi epicenter, the three-layer model with \( h = 10 \) km fits the preseismic and postseismic data best with \( 10^{18.8} \) Pa-s (minimum preseismic sum of residuals of 20 mm/yr) and \( 10^{18.2} \) Pa-s (minimum postseismic residual of \( <1 \) mm/yr), respectively (Figure 8, supporting information). In contrast to the three-layer model, the two-layer model requires a viscosity of \( 10^{18.6} \) Pa-s to explain the postseismic data equally well (minimum postseismic residual of \( <1 \) mm/yr), and a viscosity two orders of magnitude larger (\( 10^{20.9} \) Pa-s) to explain the preseismic velocities (Figure 8). Similar to the differential viscosities estimated from the preseismic and postseismic Manyi observations, we find \( |\Delta \log \eta| = 0.6 \) for the three-layer model while \( |\Delta \log \eta| = 2.3 \) for the two-layer model.

4. Inference of Midercrustal Viscosity in Tibet

4.1. The Manyi and Kokoxili Earthquakes

To determine which viscosities best-fit both the preseismic and postseismic velocities associated with the Manyi and Kokoxili earthquakes, we systematically compare the predictions from two- and three-layer models with viscosities ranging from \( 10^{16} \) to \( 10^{21} \) Pa-s. For the three-layer models we also vary the thickness of the viscoelastic layer, \( h \), between 1 and 20 km below a 20 km thick upper crust. In addition to the geodetic observables, these models require estimates of the earthquake recurrence interval, long-term

Figure 9. Repeatability of the differential viscosity estimates. Uncertainties in geodetic data are assumed to be normally distributed and 10,000 synthetic data sets are realized based on the 1σ uncertainties in the data. The resultant histograms show variation in best-fitting preseismic and postseismic estimates of differential viscosity, \( |\Delta \log \eta| \). Results for a three-layer model with midcrustal thicknesses of \( h = 10 \) km are shown in red \( (\Delta \log \eta) = 0.2 \pm 0.2 \) Manyi, \( |\Delta \log \eta| = 0.5 \pm 0.3 \) Kokoxili) and in blue for the two-layer case \( (\Delta \log \eta) = 0.7 \pm 0.2 \) Manyi, \( |\Delta \log \eta| = 1.5 \pm 0.5 \) Kokoxili). Differential viscosity estimates are generally repeatable for both the Manyi and Kokoxili earthquakes, though for both cases there are a small number of data noise realizations where \( |\Delta \log \eta| \) is equivalent for both the two- and three-layer cases. For both models, a larger differential viscosity is required to explain the Kokoxili preseismic and postseismic velocities than for Manyi case.

[16] To determine which viscosities best-fit both the preseismic and postseismic velocities associated with the Manyi and Kokoxili earthquakes, we systematically compare the predictions from two- and three-layer models with viscosities ranging from \( 10^{16} \) to \( 10^{21} \) Pa-s. For the three-layer models we also vary the thickness of the viscoelastic layer, \( h \), between 1 and 20 km below a 20 km thick upper crust. In addition to the geodetic observables, these models require estimates of the earthquake recurrence interval, long-term
analyze simulations based on synthetic realizations of data noise. Assuming that the geodetic data uncertainties are normally distributed, we generated 10,000 synthetic data sets based on the 1σ uncertainties in the data. The best-fitting parameter pairs (channel thickness $h$, $|\Delta \log \eta|$) are mapped for each simulation run in red. Underneath, a histogram of the numbers of simulation runs that resulted in each best-fitting channel thickness is shown in grey. In most (49%) of the simulations, a thin channel (~2 km) fits the data best, but this result is not unique. Models with thicker channels also explain the data in a significant number of simulations (51%).

![Figure 10](image)

**Figure 10.** Nonuniqueness of parameter estimates inferred from model postseismic GPS time series. Assuming that the data are normally distributed, we generated 1000 synthetic data sets based on the reported 1σ position uncertainties (15 mm) [ChaoJun et al., 2009] reveal cases where higher-viscosity ($\sim 10^{18}$ Pa s) thick ($h \sim 15$–20 km) layers can explain the data as well as low-viscosity ($10^{16.5}$ Pa s) thin layer ($h \sim 1$–5 km) cases (Figure 10). Thus, although the inference of a weak midcrustal ($\eta<10^{18.5}$ Pa s) layer beneath the upper crust of the Tibetan plateau is consistent with the average preseismic and postseismic velocities, further constraints on the thickness and viscosity of the midcrust underneath Tibet will require postseismic time series with smaller uncertainties and other supporting constraints such as seismic estimates of layer thickness. A similar tradeoff between channel thickness and viscosity exists in Poiseuille flow models designed to explain topographic gradients at the margins of the Tibetan plateau [e.g., Clark and Royden, 2000].

5. Discussion

[21] The two-layer Maxwell viscoelastic earthquake cycle model [e.g., Savage and Prescott, 1978] has been used extensively to estimate fault slip rates based on interseismic velocities in California [Savage, 1990; Segall, 2002; Dixon et al., 2002, 2003], Tibet [Hilley et al., 2005], and Turkey [Ergintav et al., 2002; Motagh et al., 2007]. However, due to the fact that recurrence intervals for large earthquakes may reach hundreds of years and that high-precision space-based geodetic observations have decadal durations, these observations provide only a snapshot of deformation throughout the seismic cycle. Information about the maximal variations in earthquake cycle activity may be inferred from the differences between preseismic and postseismic deformation. Unfortunately, few large ($M_W > 7.5$) strike-slip earthquakes have occurred with high-precision geodetic observations of both preseismic and postseismic velocities. In addition to 1997 $M_W=7.6$ Manyi and 2001 $M_W=7.8$ Kokoxili earthquakes in Tibet, the 1999 $M_W=7.6$ Izmit earthquake meets this criteria [Ergintav et al., 2009]. Before the Izmit event ruptured the westernmost North Anatolian fault zone, GPS observations indicate a localized velocity gradient of ~25 mm/yr within ~200 km of the fault trace [Ergintav et al., 2002; Bürgmann et al., 2002]. In the years following the coseismic rupture, rapid postseismic deformation occurred (>60 mm/yr), but within a decade, postseismic velocities had decayed to within 15% of preseismic magnitudes [Ergintav et al., 2009]. Assuming a two-layer model of the Earth with an elastic upper crust and a Maxwell viscoelastic upper mantle, the effective viscosity of the lower layer would have to increase by a factor of 10 several months after the earthquake to explain the time evolution of the postseismic velocities [Hearn et al., 2009]. Similar to the geodetic observations from across the Manyi and Kunlun rupture zones, these North Anatolian fault zone observations [Ergintav et al., 2009] suggest that a two-layer Maxwell viscoelastic earthquake cycle model alone may not adequately explain both preseismic and postseismic velocities following large earthquakes [Hetland and Hager, 2006a]. However, caution must be exercised when directly comparing the viscosity estimates inferred from three-dimensional models to the viscosity estimates reported here for two reasons: our model does not incorporate...
three-dimensional effects, and published three-dimensional models do not incorporate spin-up effects, limiting their application to only postseismic deformation.

[22] In addition, other rheologies (e.g., Burgers, standard linear solid, nonlinear), depth-varying Maxwell viscosities, and afterslip have been suggested as alternative candidates to explain similar behavior across the earthquake cycle [e.g., Hetland and Hager, 2005, 2006a, 2006b; Ryder et al., 2007; Pollitz, 2005; Hearn et al., 2009; Ryder et al., 2011; Yamazaki and Houseman, 2012]. More complicated rheologies may also be required in Tibet as we find that ~50% higher viscosities are required to explain the geodetic data prior to and following the Kokoxili earthquake than for the Manyi earthquake in both two- and three-layer models (Figure 9, Appendix A).

6. Conclusions

[23] Using time-dependent earthquake cycle models, geodetic data near active faults can be used to constrain crustal and upper mantle rheology. Although few geodetic observations of deformation throughout an entire earthquake cycle exist (e.g., Parkfield), both the beginning and end of the earthquake cycle have been observed in Tibet and show both somewhat localized velocity gradients late in the earthquake cycle and rapid postseismic deformation immediately following coseismic ruptures [e.g., Ryder et al., 2007, 2011]. These observations are not consistent with the predictions of the single Maxwell viscosity two-layer earthquake cycle model that can effectively explain either localized preseismic deformation or rapid postseismic velocities [e.g., Savage and Prescott, 1978]. In contrast, the spin-up three-layer earthquake cycle model developed here may provide a more unified representation of earthquake cycle phenomenology than the two-layer model solution. In addition to predicting rapid postseismic deformation within ~50 km of the fault trace, the three-layer model predicts localized pre-earthquake strain satisfying far-field kinematic boundary conditions (i.e., plate motion constraints) within 20 locking depths of the fault trace. This distance is greater than predicted by steady elastic half-space models [Savage and Burford, 1973] but less than two-layer viscouselastic models [Savage and Prescott, 1978]. Applied to preseismic and postseismic geodetic observations in Tibet, the three-layer model with a relatively weak ($\eta = 10^{16.5-18.5}$ Pa s) midcrustal layer can explain geodetic observations before and after the 1997 $M_w$=7.6 Manyi and 2001 $M_w$=7.8 Kokoxili earthquakes. Our estimate of a midcrustal viscosity of $\eta = 10^{16.5-18.8}$ Pa s is 1–3 orders of magnitude lower than that inferred from a two-layer Earth model constrained by preseismic observations alone [Hilley et al., 2005]. Within the context of channel flow models for the evolution of the Tibetan plateau [Bird, 1991; Royden, 1996; Royden et al., 1997; Clark and Royden, 2000; Shen et al., 2001; Beaumont et al., 2001, 2004; Jamieson et al., 2004, Clark et al., 2005; Cook and Royden, 2008] and contemporary seismic inferences of midcrustal structure [Nelson et al., 1996; Makovsky et al., 1996] the three-layer model developed here is consistent with the idea of a relatively weak midcrustal layer only if it located at the base of the upper crust.

Appendix A: Complete Three-Layer Model Solution for an Infinite Sequence of Earthquakes

[24] The velocity solution is,

$$v = \Delta u (C_1 e^{-\beta_1 t} + C_2 e^{-\beta_2 t})$$

where the coefficients ($C_1$, $C_2$) and relaxation times ($\beta_1$, $\beta_2$) are complicated functions of the midcrustal viscoelastic layer thickness $h$, the depth of the upper elastic layer $H$, the depth to which the coseismic rupture extends $D$, the earthquake recurrence interval $T$, the wave number $k$, the slip on the fault during the earthquake $\Delta u$, and the reciprocal of the Maxwell time $\beta = \mu/2\eta$, where $\mu$ is shear modulus and $\eta$ is viscosity,

$$C_1 = -2ik\beta_1 k_2 (k_3 - k_4)/(k_9 k_5) \left( (k_9 + k_{10}) \left( e^{-\beta T_{K11}} - 1 \right) \right)$$

$$C_2 = -2ik\beta_2 k_2 (k_3 - k_4)/(k_9 k_5) \left( (k_9 + k_{10}) \left( e^{-\beta T_{K12}} - 1 \right) \right)$$

$$\beta_1 = -\beta k_{11}$$

$$\beta_2 = -\beta k_{12}$$

where the geometric constants $k_1$ are,

$$k_1 = \sinh (h/k_1)$$

$$k_2 = \sinh (D/k_1)$$

$$k_3 = \cosh (H/k_1)$$

$$k_4 = \sinh (H/k_1)$$

$$k_5 = \cosh (h/k_1)$$

$$k_6 = 2(k_3 k_5 + k_4 k_3 + 2k_1 k_4)$$

$$k_7 = 2(k_3 k_5 + k_1 k_3 + k_4 k_5 + k_1 k_4)$$

$$k_8 = (k_1 + k_5)(k_1 + k_4)$$

$$k_9 = \sqrt{-4k_1^2 k_3^2 k_4 + k_3^2 k_5^2 + 2k_3 k_4 k_2^2 + k_2^2 k_5^2}$$

$$k_{10} = k_1 k_3 - k_1 k_4$$

$$k_{11} = k_9 / k_8 - k_6 / k_7$$

$$k_{12} = k_9 / k_8 + k_6 / k_7$$

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