Impact of Host Heterogeneity on the Efficacy of Interventions to Reduce *Staphylococcus aureus* Carriage

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Abstract

Background: *Staphylococcus aureus* is a common cause of bacterial infections worldwide. It is most commonly carried in and transmitted from the anterior nares. Hosts are known to vary in their proclivity for *S. aureus* nasal carriage and may be divided into persistent, intermittent, and non-carriers depending on duration of carriage. Mathematical models of *S. aureus* to predict outcomes of interventions have however typically assumed that all individuals are equally susceptible to being colonized.

Objective: To characterize biases created by assuming a homogeneous host population in estimating efficacy of control interventions

Design: Mathematical modeling

Methods: We developed a model of *S. aureus* carriage in the healthcare setting under the homogeneous assumption as well as a heterogeneous model to account for the three types of *S. aureus* carriers. In both models, we calculated the equilibrium carriage prevalence to predict the impact of control measures (reducing contact and decolonization).

Results: The homogeneous model almost always underestimates *S. aureus* transmissibility and overestimates the impact of intervention strategies in lowering carriage prevalence compared to the heterogeneous model. This finding is generally consistent regardless of changes in model setting to vary the proportions of various carriers in the population and the duration of carriage for these carrier types.

Conclusions: Not accounting for host heterogeneity leads to systematic and substantial biases in predictions of the effects of intervention strategies. Further understanding of the clinical impacts
of heterogeneity through modeling can help to target control measures and allocate resources more efficiently.
NOTE: This is the version of the manuscript accepted for publication. However, several errors were discovered after acceptance and have been corrected in this version, dated December 10, 2015. They are as follows.

Corrections underlined and in bold

Figure legends:

1) Figure 2: Impact of interventions of (a) reducing contact and (b) decolonization on S. aureus carriage prevalence under the homogeneous model and the heterogeneous model assuming three hosts classes (20% persistent, 30% intermittent, and 50% non-carriers) and that admission of those colonized is the proportion colonized among that host class. Note that in both models, 30% carriage prevalence is assumed in absence of any interventions.

2) Figure 3: Impact of interventions of (a) reducing contact and (b) decolonization on S. aureus carriage prevalence under the homogeneous model and the heterogeneous model assuming three hosts classes (20% persistent, 30% intermittent, and 50% non-carriers) and that only uncolonized individuals are admitted into the hospital. Note that in both models, 30% carriage prevalence is assumed in absence of any interventions.

Results: The Impact of Varying the Proportion of Carrier Classes in the Host Population

3) Third sentence: In scenario A, we compared the results of models with different proportions of host classes relative to the homogeneous model as a ratio of equilibrium carriage prevalence after a 25% reduction in the $\beta^*$ parameter or a decolonization regimen every 6 months ($\delta=1/180$ day$^{-1}$).

4) Second last sentence: In scenario B, all distributions of heterogeneous populations consistently predicted higher equilibrium prevalence compared with the simple model for both interventions (Online Figure S1).

Results: The Impact of Varying the Duration of Colonization

5) First sentence: We also examined the impact of varying the duration of colonization, and hence potential transmission, among the different classes of host assuming that admission of those colonized is the proportion colonized among that host class (Scenario A) and using the same intervention parameters described above.
6) Last sentence: Similarly, the finding that the heterogeneous model predicts higher equilibrium carriage prevalence compared with the homogeneous model regardless of durations of persistent and intermittent carriage for both interventions was also observed in scenario B (Online Figure S2).
Introduction

*Staphylococcus aureus* is a common cause of bacterial infections worldwide\(^1\), causing a range of diseases including community-acquired soft tissue infections and nosocomial infections. The majority of carriage episodes are asymptomatic, and this is the population responsible for transmission\(^2\). While multiple body sites can be colonized, the most frequent carriage site for *S. aureus* is the anterior nares: approximately one-third of healthy individuals asymptotically carry *S. aureus* in this location at any given point in time\(^3,4\).

Longitudinal studies have shown that the probability and duration of *S. aureus* nasal carriage vary. Typically such studies have classified participants into three host classes: persistent carriers, defined as those in whom carriage lasts for many months (about 20% of the adult population); intermittent carriers, defined as individuals who harbor *S. aureus* intermittently (about 30% of the adult population); and non-carriers, who almost never carry *S. aureus* (about 50% of the adult population)\(^5-7\). While this classification is somewhat arbitrary (as “persistence” for example, will depend on length of follow-up), it is a convenient summary of the observed heterogeneity. In such a population, an individual observed as a carrier may be either a persistent or an intermittent carrier, while a non-carrier at a particular moment may be either a non-carrier or an intermittent carrier.

Reduction of *S. aureus* transmission by interventions including hand hygiene, isolation, and decolonization reduces the incidence of nosocomial infections\(^8,9\). To examine the effectiveness of these interventions and the transmission dynamics of the pathogen, several mathematical
models have been developed\textsuperscript{10–18}. These models have assumed a homogenous population in which all individuals are equally susceptible to colonization. This assumption is clearly incorrect, and the failure to discriminate between hosts that are highly resistant to colonization and those that may play a disproportionate role in transmission may alter the predicted impact of control strategies.

We show here that assuming a homogeneous population causes systematic and substantial biases in model outcomes and illustrate how incorporation of a heterogeneous host population changes the predictions of the model. In particular, homogeneity assumptions tend to underestimate transmissibility and overestimate the impacts of control interventions.

\textbf{Methods}

\textit{Model Description}

We used a deterministic SIS (susceptible-infected-susceptible)-type transmission model of \textit{S. aureus} colonization in the healthcare setting, though we use \textit{U} (uncolonized) and \textit{C} (colonized) to emphasize that we are tracking colonization not infection (Figure 1). The proportions of colonized and uncolonized patients for any time \textit{t}, \textit{U}(t) and \textit{C}(t), sum to 1. The transmission parameter, \(\beta\), is the rate at which hosts contact each other and transmit per unit time and \(v\) is the natural rate with which \textit{S. aureus} is cleared per unit time, both of which in the homogenous case are assumed to be the same for all patients. We assumed that the discharge rate, \(\gamma\), is the same for
uncolonized and colonized patients and that the number of patients remains fixed such that the admission rate equals the discharge rate. In addition, the probability that an individual is colonized at admission is \( \lambda \). The transmission model in the homogeneous case is then given by the following differential equations:

\[
\begin{align*}
\dot{U} &= (1 - \lambda)(\gamma U + \gamma C) - \beta UC + vC - \gamma U \\
\dot{C} &= \lambda(\gamma U + \gamma C) + \beta UC - vC - \gamma C \quad \text{or} \quad C = 1 - U
\end{align*}
\]

For comparison, we analyzed a stratified version of the transmission model that incorporates host heterogeneity. Let \( N_1, N_2, \) and \( N_3 \) be the proportion of the population who are non-carriers, intermittent carriers, and persistent carriers. In each of these groups, a proportion \( U_1(t), U_2(t), \) \( U_3(t) \) (of the entire population) is uncolonized at any moment, and proportions \( C_2(t) \) and \( C_3(t) \) are the respective proportions colonized (there is no \( C_1 \) category since this part of the population is highly resistant to colonization). Then \( N_1 = U_1; \ N_2 = U_2 + C_2, \) and \( N_3 = U_3 + C_3. \) We also model heterogeneity such that \( v_2 \) and \( v_3 \) are the natural rate at which \( S. \) \textit{aureus} is cleared per unit time from an intermittent carrier and a persistent carrier, respectively. In addition, \( \lambda_2 \) is the probability that an intermittent carrier is colonized at admission while \( \lambda_3 \) is the probability that a persistent carrier is colonized at admission. While studies have shown that persistent carriers have higher risk of infection, the colonization rate in different nasal carrier types remains unknown \(^{19,20}\). Given the limited data on the transmission parameter, we assumed that intermittent carriers and persistent carriers have the same per capita rate of effective contact; hence the transmission parameter \( \beta \) is the same. This model is given by the following system of differential equations:
\[ \dot{U}_2 = (1 - \lambda_2)(\gamma U_2 + \gamma C_2) - \beta U_2(C_2 + C_3) + v_2 C_2 - \gamma U_2 \]
\[ \dot{C}_2 = \lambda_2(\gamma U_2 + \gamma C_2) + \beta U_2(C_2 + C_3) - v_2 C_2 - \gamma C_2 \]
\[ \dot{U}_3 = (1 - \lambda_3)(\gamma U_3 + \gamma C_3) - \beta U_3(C_2 + C_3) + v_3 C_3 - \gamma U_3 \]
\[ \dot{C}_3 = \lambda_3(\gamma U_3 + \gamma C_3) + \beta U_3(C_2 + C_3) - v_3 C_3 - \gamma C_3 \]

Our goal here was to examine the impact of including carriage heterogeneity by comparison with a homogeneous model.

*Parameter Estimates*

We used median *S. aureus* nasal survival time of 14 days among intermittent carriers and >154 days among persistent carriers \(^{21}\) as the average carriage duration to parameterize the clearance rates, \(v_2\) and \(v_3\), in the heterogeneous model (Table 1). We used the average median *S. aureus* nasal survival times for the various carrier types \((0.30 \times 14 + 0.20 \times 154 = 35\) days\) to parameterize the clearance rate, \(v\), in the homogeneous model. Furthermore, we used an average length of stay of 7 days \(^{13}\) to parameterize hospital discharge rate.

Empirical observations show a 30% prevalence of *S. aureus* carriage in multiple settings \(^{22}\). We used this to find the transmission parameter, \(\beta\), for both models under two extreme scenarios: Scenario A in which the proportion colonized at admission is the same as the proportion of that host class colonized in the inpatient population \((\lambda_i = C_i/(U_i+C_i))\) and Scenario B in which all individuals are uncolonized at admission \((\lambda_i=0)\). Scenario B can be thought of as an extreme case
in which all transmission is limited to the hospital, and the Scenario A as the alternate extreme where either transmission is equally intense outside and inside the hospital or where individuals are very rapidly readmitted after discharge. Alternatively, Scenario A can also be thought of as a model for a community in which the population of hosts does not appreciably change over the time scale that would be considered in an intervention study (months to a few years).

**Modeling Interventions**

We considered two classes of control measures. The first aims to reduce the contact rate and thus the transmission parameter $\beta$ through isolation of carriers or other infection control measures such as handwashing. The second class of control measures is targeted at decolonizing carriers, such as through intranasal application of mupirocin alone or with antiseptic soaps or antimicrobial agents. This is modeled through the parameter $\delta$, the rate of successful decolonization. In both the homogeneous and heterogeneous model, we calculated the new equilibrium carriage prevalence after the implementation of control measures (reducing $\beta$ or varying $\delta$). We examined the impact of interventions on carriage prevalence when varying the proportions of carrier types and the durations of persistent and intermittent carriage. All equilibrium prevalence predictions were calculated analytically and graphed using R.

**Results**

*Heterogeneous carriage reduces the expected impact of interventions*
In Scenario A where those colonized at admission is the same as the proportion colonized among that host class \( \lambda_i = \frac{C_i}{(U_i + C_i)} \), the homogeneous model predicts that even a modest reduction in \( \beta \) through interventions aimed at contact rates has a marked impact on carriage prevalence (Figure 2a). A 30% reduction in \( \beta \) is expected to eliminate \textit{S. aureus} from the population. In contrast in the heterogeneous model, elimination requires reducing \( \beta \) by more than 80%.

Similarly, the homogeneous model predicts that decolonization every 120 days or so will almost eliminate carriage, whereas the same regime applied to the heterogeneous population will have very little effect (Figure 2b).

In Scenario B where all individuals are uncolonized at admission \( (\lambda_i=0) \), the homogeneous model consistently overestimates the prevalence of overall carriage for both types of interventions, but to a lesser degree than Scenario A. Reducing \( \beta \) by approximately 30% is expected to eliminate \textit{S. aureus} in the homogeneous model while the same outcome in the heterogeneous model requires reducing \( \beta \) by approximately 60% (Figure 3a). Under this scenario, decolonization strategies have little impact on reducing \textit{S. aureus} carriage in both models, and in the heterogeneous model, it becomes almost impossible to eliminate carriage.

\textit{The impact of varying the proportion of carrier classes in the host population}

The exact proportions of persistent, intermittent, and non-carriers have been studied in only a few populations\(^{5,22}\) and may vary in different settings. We hence examined how varying the population composition impacts carriage prevalence. In Scenario A, we compared the results of
models with different proportions of host classes relative to the homogeneous model as a ratio of equilibrium carriage prevalence after a 25% reduction in the $\beta^*$ parameter or a decolonization regime every 6 months ($\delta = 1/180$ day$^{-1}$). For interventions targeting transmission, all distributions of heterogeneous populations resulted in higher equilibrium prevalence compared with the homogeneous model with the largest proportions of non-carriers giving the highest ratio of roughly 4.25 (Figure 4a). For intervention based on decolonization, the carriage prevalence in the heterogeneous model was at worst 3-fold higher compared to the homogeneous model (Figure 4b). An exception to the otherwise general finding that incorporating heterogeneity reduces the predicted impact of interventions is found in populations where 40-45% are persistent carriers (the contour line with ratio=1 in Figure 4b). Here, decolonization in the heterogeneous model is more effective compared to the homogeneous model and the effect is markedly increased as the proportion of persistent carriers increases beyond this threshold. In Scenario B, all distributions of heterogeneous populations consistently predicted higher equilibrium prevalence compared with the simple model for both interventions (Figure S1). For both scenarios, the distributions of hosts that we predict will have the largest negative impact on the effectiveness of both interventions was close to the range of proportions of different host classes reported in longitudinal studies $^5,6,22$.

*The impact of varying the duration of colonization*

We also examined the impact of varying the duration of colonization, and hence potential transmission, among the different classes of host assuming that admission of those colonized is the proportion colonized among that host class (Scenario A) using the same intervention
parameters as above. Again the homogeneous model is consistently overoptimistic. As shown in Figure 5a, the heterogeneous model predicted carriage prevalence roughly 4 times that of the homogeneous model and this is robust to the durations of intermittent and persistent carriage. Similarly as shown in Figure 5b, decolonizing individuals every six months was more effective in reducing the prevalence of overall carriage as predicted in the homogeneous model compared to that of the heterogeneous model, regardless of the durations of carriage assumed. Similarly, the finding that the heterogeneous model predicts higher equilibrium carriage prevalence compared to the homogeneous model regardless of durations of persistent and intermittent carriage for both interventions is also observed in Scenario B (Figure S2).

**Discussion**

Mathematical models of *S. aureus* transmission can quantitatively predict outcomes of interventions and guide decision-making. These models have made the assumption that all individuals have the same probability and duration of carriage. This is often supported by the notion that variation in susceptibility is considered to result in smaller outbreaks and therefore models assuming equal susceptibility are considered the worst-case scenario in the sense of the extent of transmission they produce. However, this perception does not account for the fact that a model ignoring heterogeneity in the population will be "fooled" by the overall low prevalence of colonization into underestimating the transmissibility of the pathogen. In turn, the lower estimate of transmissibility can lead to an overestimate of the estimated impact of interventions.
We have examined two scenarios that represent two extremes of time between hospital admissions. Scenario B where only uncolonized individuals are admitted simulates a very long, or even infinite, time between admissions while Scenario A where newly admitted patients are assumed to be colonized in the proportion that would be expected for hosts of that class simulates a feedback loop in which people are frequently readmitted. Mathematically, the latter scenario is equivalent to a model of community-acquired *S. aureus*. In both scenarios, the homogeneous assumption consistently overestimates the effectiveness of control strategies. Moreover, this observation was robust to the proportions of carrier types and the carriage duration for each type. The exception was when persistent carriers make up 40-45% of the population or more, the heterogeneous model made the opposite prediction: decolonization would reduce carriage more than one would assume from the homogeneous model. This reflects the disproportionate contribution of the persistent carriers to transmission as a result of being colonized for a longer period.

Other studies have considered the effects of heterogeneity on the spread of sexually-transmitted \(^{27}\) and vector-borne \(^{28}\) infections. These studies have in common the idea that the existence of particularly high-risk hosts contributes disproportionately to transmission. The key issue in both cases is that such hosts are simultaneously more likely to become infected and to transmit infection, as the same activity (being bitten or sex) is necessary for both. In these settings, the basic reproductive number \((R_0)\) is proportional to the sum of the mean and the variance/mean ratio for sexual activity or rate of being bitten in simple models of heterogeneous host populations. We have considered and analyzed a different phenomenon here. In our model, hosts
differ in their durations of carriage, which affects transmission but not acquisition rate (and we assume that all hosts are equally likely to become colonized, though some may have effectively zero duration). In this setting, the $R_0$ is a simple average of the transmission from the different types of hosts, weighted by the frequency of each host type and the carriage duration in that host type. In our heterogeneous model, the non-carriers are not capable of transmitting, and persistent or intermittent carriers are colonized at a faster rate and naturally decolonize at a slower rate. The consequence of this is an increase of $R_0$. Thus ignoring heterogeneity leads us to underestimate transmissibility and overestimate an intervention’s effectiveness.

Our models do not take into account factors such as antibiotic resistance, compliance with interventions, environmental or healthcare related transmission. We developed our models to demonstrate the biases created by the failure to incorporate heterogeneity in carriage types. Our analysis is deliberately focused on variation arising from susceptibility and duration of carriage, but this is only one possible source of heterogeneity. Alternatively, hosts may be equally susceptible, but vary in their ability to transmit. This has been experimentally observed in finger-finger transmission of enterococci. Host susceptibility may be a general issue in nosocomial epidemiology across different bacteria species and colonization sites.

Improved understanding of host heterogeneity in carriage through modeling may significantly change ways in which dynamics of colonization and disease are characterized, as well as the approaches for implementing control measures. In a randomized clinical trial, findings of limited reduction in methicillin-resistant *S. aureus* carriage despite decolonization with mupirocin may be explained in part by our analysis, which predicts the effort required to achieve
control is greater than expected. We also note that strategies that might be particularly effective in one setting may not directly translate to another setting where the population may have a different distribution of carrier types. Future work to understand the mechanisms underlying the heterogeneity in *S. aureus* carriage will aid in targeted interventions that ensure optimal allocation of resources.
Acknowledgments

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References


Figure Legends

Figure 1: Transmission models of *S. aureus* colonization for (a) the homogeneous model and (b) the heterogeneous model. The diagram shows the inflow and outflow of uncolonized and colonized patients (U, C). Subscripts indicate each of the three host classes (non-carriers, intermittent carriers, and persistent carriers).

Figure 2: Impact of interventions of (a) reducing contact and (b) decolonization on *S. aureus* carriage prevalence under the homogeneous model and the heterogeneous model assuming three hosts classes (20% persistent, 30% intermittent, and 50% non-carriers) and that admission of those colonized is the proportion colonized among that host class. In both models, 30% carriage prevalence is assumed in absence of any interventions.

Figure 3: Impact of interventions of (a) reducing contact and (b) decolonization on *S. aureus* carriage prevalence under the homogeneous model and the heterogeneous model assuming three hosts classes (20% persistent, 30% intermittent, and 50% non-carriers) and that only uncolonized individuals are admitted into the hospital. In both models, 30% carriage prevalence is assumed in absence of any interventions.

Figure 4: A heat-map of the ratios of carriage prevalence in the heterogeneous model to the homogeneous model when varying proportions of carrier classes under Scenario A (admission of those colonized is the proportion colonized among that host class) with intervention of (a) reducing $\beta^*$ parameter (see Table 1) by 25% and (b) setting $\delta$ parameter to $1/180$ day$^{-1}$. The ratio
represents the magnitude of difference between the models, with >1 indicating that the heterogeneous model predicts higher carriage prevalence compared to the homogeneous model. The dotted lines enclose all possible combinations of the proportions of persistent, intermittent, and non-carriers. Complete elimination of *S. aureus* carriage in the heterogeneous model is shown in grey. The red dot represents assumed proportions of each carrier type for the initial analysis.

**Figure 5:** A heat-map of the ratios of carriage prevalence in the heterogeneous model to the homogeneous model when varying persistent and intermittent carriage durations under Scenario A (admission of those colonized is the proportion colonized among that host class) with intervention of (a) reducing $\beta^*$ parameter (see Table 1) by 25% and (b) setting $\delta$ parameter to $1/180$ day$^{-1}$. The ratio represents the magnitude of difference between the models, with >1 indicating that the heterogeneous model predicts higher carriage prevalence compared to the homogeneous model. The red dot represents assumed carriage durations of each carrier type for the initial analysis.
### Tables

Table 1: Description of model parameters for the homogeneous and heterogeneous models of *S. aureus* carriage

<table>
<thead>
<tr>
<th>Model</th>
<th>Parameter</th>
<th>Value</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Homogeneous</td>
<td>β</td>
<td>( \lambda = \frac{c}{u+c} \cdot 0.028 \text{ day}^{-1} ) ( \lambda = 0: 0.232 \text{ day}^{-1} )</td>
<td>Transmission parameter</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td></td>
<td>( \nu )</td>
<td>( \ln(2)/35 \text{ day}^{-1} )</td>
<td>Natural clearance rate</td>
</tr>
<tr>
<td></td>
<td>( \gamma )</td>
<td>7 days(^{-1} )</td>
<td>Discharge rate</td>
</tr>
<tr>
<td>Heterogeneous</td>
<td>β</td>
<td>( \lambda_i = \frac{c_i}{u_i+c_i} \cdot 0.115 \text{ day}^{-1} ) ( \lambda_i = 0: 0.866 \text{ day}^{-1} )</td>
<td>Transmission parameter assuming 20% persistent, 30% intermittent, and 50% non-carriers (Figure 2)</td>
</tr>
<tr>
<td></td>
<td>( \beta^* )</td>
<td>( \lambda_4 = 0: 1 = \frac{x_2\beta^<em>}{0.3\beta^</em>+\nu_2} + \frac{x_3\beta^<em>}{0.3\beta^</em>+\nu_3+\gamma} )</td>
<td>Transmission parameter for 30% overall carriage prevalence in populations with varying proportions of carrier classes (Figure 3)</td>
</tr>
<tr>
<td></td>
<td>( \nu_2 )</td>
<td>( \ln(2)/14 \text{ day}^{-1} )</td>
<td>Natural clearance rate for intermittent carriers</td>
</tr>
<tr>
<td></td>
<td>( \nu_3 )</td>
<td>( \ln(2)/154 \text{ day}^{-1} )</td>
<td>Natural clearance rate for persistent carriers</td>
</tr>
<tr>
<td></td>
<td>( \gamma )</td>
<td>7 days(^{-1} )</td>
<td>Discharge rate</td>
</tr>
</tbody>
</table>
a) Reduction in Beta

Prevalence of Carriage (%)

% Reduction in Beta

b) Frequency of Decolonization (1/days)

Prevalence of Carriage (%)

Frequency of Decolonization (1/days)
Figure S1: A heat-map of the ratios of carriage prevalence in the heterogeneous model to the homogeneous model when varying proportions of carrier classes under Scenario B (all individuals are uncolonized at admission) and intervention of (a) reducing $\beta^*$ parameter (see Table 1) by 25% and (b) setting $\delta$ parameter to $1/21$ day$^{-1}$. The ratio represents the magnitude of difference between the models, with $>1$ indicating that the heterogeneous model predicts higher carriage prevalence compared to the homogeneous model. The dotted lines enclose all possible combinations of the proportions of persistent, intermittent, and non-carriers. The red dot represents assumed proportions of each carrier type for the initial analysis.
Figure S2: A heat-map of the ratios of carriage prevalence in the heterogeneous model to the homogeneous model when varying persistent and intermittent carriage durations under Scenario B (all individuals are uncolonized at admission) and intervention of (a) reducing $\beta^*$ parameter (see Table 1) by 25% and (b) setting $\delta$ parameter to $1/21$ day$^{-1}$. The ratio represents the magnitude of difference between the models, with $>1$ indicating that the heterogeneous model predicts higher carriage prevalence compared to the homogeneous model. The red dot represents assumed carriage durations of each carrier type for the initial analysis.