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Sulfur Isotope Effects of Dissimilatory Sulfite Reductase

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The precise interpretation of environmental sulfur isotope records requires a quantitative understanding of the biochemical controls on sulfur isotope fractionation by the principle iso- tope-fractionating process within the S cycle, microbial sulfate reduction (MSR). Here we provide the only direct observation of the major (34S/32S) and minor (33S/32S, 36S/32S) sulfur isotope fractionations imparted by a central enzyme in the energy metabolism of sulfate reducers, dissimilatory sulfite reductase (DsrAB). Results from in vitro sulfite reduction experiments allow us to calculate the in vitro DsrAB isotope effect in 34S/32S (hereafter, 34εDsrAB) to be 15.3 ± 2‰, 2σ. The accompanying minor isotope effect in 33S, described as 33εDsrAB, is calculated to be 0.5150 ± 0.0012, 2σ. These observations facilitate a rigorous evaluation of the isotopic fractionation associated with the dissimilatory MSR pathway, as well as of the environmental variables that govern the overall magnitude of fractionation by natural communities of sulfate reducers. The isotope effect induced by DsrAB upon sulfite reduction is a factor of 0.3–0.6 times prior indirect estimates, which have ranged from 25 to 53‰ in 34εDsrAB. The minor isotope fractionation observed from DsrAB is consistent with a kinetic or equilibrium effect. Our in vitro constraints on the magnitude of 34εDsrAB is similar to the median value of experimental observations compiled from all known published work, where 34εr–p = 16.1‰ (r–p indicates reactant vs. product, n = 648). This value closely matches those of MSR operating at high sulfite reduction rates in both laboratory chemostat experiments (34εSO4−H2S = 17.3 ± 1.5‰, 2σ) and in modern marine sediments (34εSO4−H2S = 17.3 ± 3.8‰). Targeting the direct isotopic consequences of a specific enzymatic process is a fundamental step toward a biochemical foundation for reinterpreting the biogeochemical and geobiological sulfur isotope records in modern and ancient environments.

Keywords: microbial sulfate reduction, enzyme-specific isotope fractionation, minor sulfur isotopes, global sulfur cycle, dissimilatory sulfite reductase

INTRODUCTION

Microbial sulfate reduction provides a critical link between Earth’s surface sulfur, carbon, iron, and oxygen cycles (Thode et al., 1961; Holland, 1973; Garrels and Lerman, 1981; Canfield, 2001a). This metabolism is comprised of a set of enzymes working in concert to reduce sulfate (SO42−) to sulfide (H2S) (Peck, 1961; Pereira et al., 2011; Figure 1). During this transformation, MSR generates 34S/32S, 33S/32S, 36S/32S, 18O/16O, and 17O/16O stable isotope fractionations.
(Harrison and Thode, 1958; Kaplan and Rittenberg, 1964; Kemp and Thode, 1968; Chambers et al., 1975; Goldhaber and Kaplan, 1975; Fritz et al., 1989; Canfield, 2001b; Sim et al., 2011b; Leavitt et al., 2013), the biochemical source of which is unclear (Chambers and Trudinger, 1979). To construct a biochemically constrained perspective of sulfur isotope fractionations during MSR requires we quantify how material moves through the metabolic network, and gain an understanding of the isotopic effect(s) associated with each constituent enzymatic step (Hayes, 2001).

The enzyme catalyzed reaction network of MSR is represented in Figure 1. Sulfate is first imported into the cytoplasm by a variety of transporters (Cypionka, 1994; Piłsyk and Paszewski, 2009; Figure 1), and subsequently activated to a high-energy intermediate, adenosine 5-proofosphosulfate (APS). The latter reaction generates pyrophosphate (PPI) at the expense of ATP by the enzyme sulfate-adenyllyl transferase (Sat) (Peck, 1962). APS is reduced to sulfite (SO$_3^{2-}$) through a two-electron transfer by the soluble cytoplasmic enzyme APS oxidoreductase (ApsR) (Peck, 1959), which is linked to energy conservation by the membrane-bound complex QmoABC (Pires et al., 2003). APS reduction is highly reversible, depending on the in vivo or in vitro conditions (Peck, 1960). Sulfite has several potential fates. Sulfite can either be re-oxidized to sulfate (directly or via APS) or further reduced to sulfide by DsrAB with the involvement of DsrC (Oliveira et al., 2008b). A critical step is during the reduction of sulfite when it binds the iron of the siroheme in the DsrAB active site. The subsequent reduction occurs via electron transfer from an adjacent Fe-S cluster (Oliveira et al., 2008a,b; Parey et al., 2010). In vivo, DsrAB has been proposed to generate intermediate valence sulfur, which is then bound to DsrC and converted to sulfide via DsrC/MK (Oliveira et al., 2008b; Venceslau et al., 2013, 2014; Santos et al., 2015). Sulfide then leaves the cell by diffusion as H$_2$S (Mathai et al., 2009) or through anion transport (as HS$^-$ or S$^{2-}$) (Czyzewski and Wang, 2012), though the mechanism of sulfide exit in MSR is still not well known. In instances when DsrC is unavailable (e.g., when DsrAB is pure in vitro) or limiting (e.g., intracellular sulfite is in excess of reduced DsrC), intermediates such as thiosulfate (S$_2$O$_3^{2-}$) may become important, likely due to the reaction of sulfite with sulfide (in vivo) or the partially reduced sulfur from DsrAB (in vitro) (Chambers and Trudinger, 1975; Drake and Akagi, 1976, 1977, 1978; Kim and Akagi, 1985). A few examples exist where thiosulfate is a key component in closing $S$ mass balance during in vivo MSR (Sass et al., 1992; Leavitt et al., 2014; Price et al., 2014), and in one instance trithionate is observed (S$_3$O$_2^{2-}$) (Sass et al., 1992), though it is not clear in this case it is a physiological product. Under these conditions, accumulation and excretion of such compounds as thiosulfate may be important (Bradley et al., 2011). It is within this broader biochemical and physiological context that we examine the isotopic consequences of sulfite reduction by DsrAB, which as outlined above, is central to the biochemistry of dissimilatory sulfate reduction.

Reduction of sulfite by DsrAB breaks three of the four S-O bonds in the original sulfate (Venceslau et al., 2014). As such, the isotope effect of DsrAB likely plays a significant role in setting the overall fractionations observed from MSR (Harrison and Thode, 1958; Rees, 1973; Farquhar et al., 2003; Brunner and Bernasconi, 2005). Measured enzyme-specific isotope effects are lacking for MSR and the $S$ cycle in general. Such information has been transformative for the study of other biogeochemical elements like carbon. For example, experimental work quantifying the $^{13}$C/$^{12}$C effect of RuBisCO (Park and Epstein, 1960; Farquhar et al., 1982; Tcherkez et al., 2006), the core enzyme in carbon fixation, has greatly advanced the applicability of carbon isotope biogeochemistry. More specifically, understanding the fractionation associated with RuBisCO allowed greater insight into modern (Hayes, 1993) and ancient (Hayes et al., 1999) carbon cycling, and facilitated a better understanding of primary productivity in the both modern (Laws et al., 1995) and ancient (Pagani et al., 2009) oceans. Similar enzyme-specific approaches have also proven greatly informative in studies of methanogenesis (Scheller et al., 2013), nitrate assimilation (Karsh et al., 2012) and nitrogen fixation (Sra et al., 2004). With these studies as a guide, we look to further unlock the sulfur cycle through targeting a key microbial sulfite reduction enzyme, DsrAB.

To close the knowledge gap between whole-cell observations and enzyme-catalyzed reactions, as well as to turn natural isotope records into catalogs of environmental information, we conduct the first enzyme-specific sulfur isotope experiments. Here we report the sulfur isotope fractionation factors associated with in vitro sulfite reduction by the dissimilatory sulfite
reductase enzyme (DsrAB). Using these results and a new multi-component isotope distillation model, we are able to place improved constraints on the root of sulfur isotopic fractionation during MSR. This refines our understanding of the predominant biological process responsible for generating environmental S isotope records throughout geological history.

**EXPERIMENTAL METHODS SUMMARY**

We conducted a series of closed system *in vitro* sulfite reduction experiments with purified DsrAB from *Desulfovibrio vulgaris* str. Hildenborough (DSM 644) and *Archaeoglobus fulgidus*. These enzymes are structurally similar and evolutionarily related (Parey et al., 2013), and we chose them to attempt to determine conservation of isotope fractionation in *D. vulgaris* and *A. fulgidus* DsrAB. The complete isolation and purification details are available in the Supplementary Material.

DsrAB experiments were conducted *in vitro* under strictly anoxic conditions with H₂, [NiFe] hydrogenase, and methyl viologen as the electron donation system. Key considerations in experimental design are: (i) to provide enough sulfur at each time point for isotope characterization of residual reactant and products; (ii) to provide the proper reaction conditions to allow for optimal DsrAB activity (pH = 7.1, T = 20°C or 31°C for *D. vulgaris* and 65°C for *A. fulgidus*); (iii) to ensure hydrogenase activity is not inhibited by the experimental pH (optimum at pH 7.5, activity significantly depleted below pH 6.5, so we chose pH 7.1, to account for optima of both DsrAB and [NiFe]-hydrogenase); and finally (iv) to ensure the sulfite to hydrogen ratio strongly favors sulfite reduction. Experiments setup is detailed in the Supplementary Material.

Each experiment was performed in duplicate and sampled as sulfite was consumed (reaction progress tracked as f₃0S, equivalent to the fraction of remaining sulfite). The reaction consumed sulfite to form products thiosulfate and trithionate, with no detectable sulfide. Thiosulfate and trithionate concentrations were quantified following published cyanalysis protocols (Kelly and Wood, 1994), where we used a modified “Fuschin” method (Grant, 1947) to quantify sulfite and a modified Cline method (Cline, 1969) to measure sulfide. All quantification and experimental methods are fully detailed in the Supplementary Material. In addition to concentrations, we measured the major and minor sulfur isotopic compositions of three operationally defined and precipitated pools: sulfite (both initial and residual reactant), product selenate (from trithionate or thiosulfate) and the “reduced sulfur” products (central and terminal sulfurs in trithionate and thiosulfate, respectively). Complete IUPAC definitions of each S reservoir, along with all isotopic measurement methods and error propagation calculations are fully articulated in the Supplementary Material.

**ISOTOPE NOTATION**

The variability in 34S of a measured pool is reported in standard delta notation (for instance δ34S, in ‰ units), where 34S/32S of the sample is the relative difference from a standard (Hayes, 1983), and is reported as the isotopic offset between two measured pools of sulfur, 34δ = (10×(34S/32S−1)), still in ‰ units. Fractionation factors (α’s and associated ε’s) are annotated with a subscript to denote the process of interest or pools being related, such as 34δ₃₀S, 34δ₃₀MSR, 34δ₃₀ox, 34δ₃₀red, or 34δ₃₀SO₄⁻. The same nomenclature convention is followed when a minor isotope, 33S, is included. The only exception is the addition of one new term, 33λ, which is approximately the slope of a line on a plot of 33S vs. 34S (Miller, 2002; Farquhar et al., 2003), but can be simply interpreted as a measure of mass-dependent minor isotope fractionation. Mathematical definitions are provided below.

**FRACTIONATION MODELING**

Calculation of the isotopic fractionation imposed by the reduction of sulfite through DsrAB requires tracking the concentration of the reactant, accumulation of the products, and determining the isotopic composition of all as the reaction progressed. This necessitates the application of a closed-system model in order to calculate fractionation factors. Determining the intrinsic isotope effect associated with a closed system reaction can be approached in a number of ways. Normally, in a system where one reactant is consumed in order to generate a single product, a Rayleigh model is employed (Nakai and Jensen, 1964; Mariotti et al., 1981). This approach assumes that the reaction of interest is unidirectional, generates only one product, and that the fractionation factor is invariant throughout the reaction. In this case, the isotope effect is calculated as a function of the isotope ratio, R, of the starting composition (R₀) and evolving product pool (Rₚ, defined below), equal to the mass balance on sulfite:

\[ \alpha_{\text{total}} = \frac{\ln\left(\frac{R_{p}}{R_{0}} (f - 1) + 1\right)}{\ln(f)} \]  

(1)

In this solution, f tracks the fractional amount of reactant remaining (SO₃⁻). For our experiments, we define f₃₀S:

\[ f_{SO_3} = \left[\frac{SO_3^-}{SO_3^-}_0\right] \]  

(2)

In the specific case of our experiments and the reduction of sulfite by DsrAB, however, the standard closed-system isotope distillation models (Equation 1) requires expansion. Recall that the *in vitro* reaction involves the accumulation of two products (trithionate and thiosulfate). Each of these products further contains sulfur moieties in more than one oxidation state (Suh and Akagi, 1969; Kobayashi et al., 1974; Drake and Akagi, 1976, 1977, 1978). This means that, rather than Rₚ being the isotope composition of a single product pool, we define it as the mass-weighted sum of the oxidized (Rₐox) and reduced (Rₐred) products in trithionate and thiosulfate:

\[ R_p = \left[\frac{1}{2} j + \frac{1}{3} (1 - j)\right] R_{\text{red}} + \left[\frac{1}{2} j + \frac{2}{3} (1 - j)\right] R_{\text{ox}} \]  

(3)

Here the reduced and oxidized pools are the operationally defined reservoirs discussed above. In the mass balance
accounting equation we introduce a term to quantify the ratio of products, \( j \) (Figure 2). The concentrations of sulfite, trithionate, and thiosulfate were measured at each time-point, ensuring the closure of mass balance and validating the use of a relative mass term. The \( j \) term is thus the fraction of products residing in thiosulfate:

\[
\frac{2[S_2O_2^{2-}]_t}{2[S_2O_2^{2-}]_t + 3[S_3O_6^{2-}]_t}.
\]

For isotopic measurements we quantitatively separated the oxidized moieties from trithionate and thiosulfate from the partially reduced moieties of both products. There were no available methods to separate trithionate and thiosulfate and isolate each S site within those products (a target for future work). We then measured the isotopic compositions of the pooled oxidized and pooled reduced products. As the goal is to identify the fractionation between the residual sulfite and either the oxidized \((^{3x}\alpha_{ox})\) or reduced \((^{3x}\alpha_{red})\) moieties in trithionate and thiosulfate, we present the general equation, \((^{3x}\alpha_z)\):

\[
^{3x}\alpha_z = \frac{R_z}{R_{z0}} \frac{\alpha_{total}}{(f^{total} - 1)} (f-1),
\]

where \( z \) is either \( ox \) or \( red \). This solution is then translated into standard \(^{3x}\varepsilon\) notation. Fractionation factors are then related in triple isotope space with:

\[
^{3x}\lambda = \frac{\ln (^{3x}\alpha)}{\ln (^{34}\alpha)}
\]

a term which finds common application in mass-dependent studies (Young et al., 2002; Farquhar et al., 2003). Finally, we note the models assumptions: (1) sulfite and its isomers carry the same isotopic composition as each other, (2) the isotopic composition of the sulfonate groups (in trithionate and thiosulfate) are isotopically identical, and (3) similar to 2, the isotopic composition of reduced sulfur in trithionate and thiosulfate are isotopically identical.

The complexity added above in equation 6 allows for numerous products for a given reaction, but still assumes that the fractionation factors involved are static over the time series of the experiment \((f_{SO3})\) and that there is only one reaction present. If this is true, then the model prediction will match the observation over all values of \( f_{SO3} \). Although, we observed a statistically invariant ratio of thiosulfate to trithionate production throughout the reaction (\( j \) in Figure 2), suggesting a static set of reactions through the entire experiment, it appears that the net fractionation factor was indeed time-dependent. In the event of an evolving \( \alpha \), the fractionation factor early in the experiment, where the concentration of products remains low, most closely approximates the isotope effect of DsrAB solely reducing sulfite. We explore this time-dependence further in the

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**FIGURE 2 | Reaction progress during sulfite reduction with *D. vulgaris* DsrAB *in vitro*.** Errors are included in all measurements (2\( \sigma \)) and are smaller than the symbol if not seen. (A) The mol fraction of sulfur in each sulfur product pool as a function of reaction progress, \( f_{SO3} \). Mass balance conservation is discussed in the text. (B) The ratio of products at each time point, demonstrating the constancy of the reaction scheme (denoted as \( j \) in the model). This is the ratio of the slopes of the products from (A). (C) Major isotope data for each operationally defined sulfur pool as a function of reaction progress, and normalized to the initial sulfite composition. (D) A triple isotope cross plot of the data presented in frame C, normalized to V-CDT.
Supplementary Material for all sampled points on the reaction progress coordinate ($f_{SO3}$). Thus, for extracting the intrinsic isotope effect associated with enzymatic reduction of sulfite, we focused on data where $f_{SO3} > 0.85$. To do so, we have used our modified Rayleigh-type isotope distillation model in which we account for the production of reduced and oxidized sulfur within aqueous products trithionate and thiosulfate. Procedures for error propagation associated with these calculations are described in the Supplementary Material.

RESULTS

We tracked all S pools at each time point. Mass balance was satisfied within ±10% of the initially provided sulfite in every experiment, and within ±5% in 27 of 33 experiments (Figure 2A). The majority of this variance is due to analytical error in the sulfite quantifications. In experiments with the *D. vulgaris* DsrAB, the products were generated with a mean of 19% of the product sulfur forming thiosulfate and the remainder accumulating as trithionate (Figure 2B). This is consistent with previous reports (Drake and Akagi, 1976, 1978), and expected given the absence of active DsrC in these experiments. Some inactive DsrC does accompany the *D. vulgaris* DsrAB during isolation and purification (Oliveira et al., 2008a,b, 2011), however there is no means to recycle this component, and as such, it is not a functional part of the experiment. Therefore, the *in vitro* sulfite reduction reactions produce thionates rather than sulfide. In our experiments, sulfite was always in excess of H$_2$, and therefore was not limiting at any point.

To extend our studies to a different taxonomic form of the enzyme, we also experimented on the DsrAB from the thermophilic archaeon *A. fulgidus*. This enzyme operates at higher temperature and lacks DsrC in the complex (Schiffer et al., 2008). *A. fulgidus* experiments showed consistent loss of sulfite and accumulation of products between replicates at each time point. Unlike *D. vulgaris* DsrAB experiments, however, only small quantities of product were generated. From these experiments we were able to resolve a complete sample set (i.e., sulfite, sulfonate, and reduced S) from one time-point and partial sets from another (i.e., sulfite and sulfonate). Special efforts were made to correct data available on *A. fulgidus* experiments (see the Supplementary Material). The results using DsrAB from *A. fulgidus* are consistent with those of *D. vulgaris*, but with a large calculated uncertainty. We therefore focus our interpretations on the results from the *D. vulgaris* experiments.

We use the concentrations of sulfite, trithionate, and thiosulfate, as well as the isotopic compositions of each operationally defined product to solve for the fractionations associated with DsrAB. The calculated $^{34}_{E_{DsrAB}}$ for sulfite reduction by the *D. vulgaris* DsrAB is 15.3 ± 2.0% (2σ, Figure 3), where the concurrent fractionation associated with the generation of the sulfonate is −3.2 ± 0.8% (2σ). The $^{34}_{E_{DsrAB}}$ from *A. fulgidus* is generally consistent with the *D. vulgaris* experiments, yielding a reductive fractionation of 16% (2σ from 22 to 12%) at 65°C. Large and asymmetric errors on the *A. fulgidus* data are the result of exceptionally small sample sizes, which also precluded the collection of $^{33}$S data (see the Supplementary Material). Together, these experiments demonstrate a broad consistency in fractionation by DsrAB over a wide range of temperatures (20 and 30°C for *D. vulgaris*, and 65°C for *A. fulgidis*) and across two Domains of life.

Fractionation of $^{33}$S between sulfite and reduced sulfur by *D. vulgaris* DsrAB is reported as $^{33}_{\lambda_{DsrAB}}$, with a calculated result of 0.5150 ± 0.0012 (2σ) over the initial range of $f_{SO3}$. The conversion of sulfite to sulfonate yielded a calculated $^{33}_{\lambda_{DsrAB}}$ that changes as the reaction progressed, from 0.495 ± 0.017 (2σ) at $f_{SO3} > 0.85$, toward 0.510 at $f_{SO3} < 0.85$. The experimental error on $^{33}_{\lambda_{DsrAB}}$ is inversely related to the magnitude of $^{34}_{E_{DsrAB}}$ (Johnston et al., 2007), thus is larger for sulfonate generation. We interpret the observed fractionation factors between sulfite and reduced S as representing the binding and reduction of sulfite by DsrAB. The fractionation associated with sulfonate production is more difficult to uniquely diagnose given the wide array of potential biotic and abiotic reactions.

DISCUSSION

Microbial sulfate reduction is a major process in the sulfur cycle and generates characteristic isotopic fractionations. These fractionations are critical in tracing the movement of sulfur within natural settings (marine and lacustrine). Determining the isotope effects associated with key enzymes in this pathway is critical to disentangling biological and physical controls on the distribution of sulfur isotopes among environmental pools of sulfur. In this study we provide the first constraints ($^{34}_{E}$ and $^{33}_{\lambda}$) on the isotope effects associated with one such enzyme: DsrAB, the central redox enzyme in dissimilatory sulfate reduction. This experimental constraints generated herein provides insight and critical boundary conditions for understanding sulfur isotope fractionation by sulfate reducers. Fortunately, half a century of
research on sulfur isotope fractionation by MSR in vivo puts in place a series of useful observations that help to guide our interpretation as to the role of DsrAB. This in turn allows significantly greater access to the information locked in sulfur isotope records.

**Fractionation at the Cellular Scale**
The rich literature of whole cell isotope fractionation data associated with MSR lacks information about kinetic isotope effects associated with specific enzymes within the metabolism. Cellular-level observations include secular and spatial trends in sulfur isotope records attributed to changes in the environmental conditions at the site of MSR, and degree to which biogenic sulfide is preserved in marine sediments (Holland, 1973; Canfield and Farquhar, 2009; Leavitt et al., 2013). The environmental variables most commonly invoked to explain isotopic variability are aqueous sulfate and organic carbon concentrations (Goldhaber and Kaplan, 1975; Habicht et al., 2002; Bradley et al., 2015). Both of these variables ultimately contribute to the net reduction rate and carry independent biological thresholds, one of which ultimately becoming rate-limiting (Bradley et al., 2011, 2015). More specifically, variability in these substrates is manifested as changes in the cell-specific rates of MSR in both the laboratory and natural environment (Chambers et al., 1975; Goldhaber and Kaplan, 1975; Leavitt et al., 2013). In laboratory experiments and natural marine and lacustrine systems, volumetric sulfate reduction rates scale primarily as a function of the availability of sulfate relative to common electron donors like organic carbon (Chambers et al., 1975; Goldhaber and Kaplan, 1975; Sim et al., 2011b; Leavitt et al., 2013). Indeed, sulfate can be non-limiting even in environments with as little as μM sulfate (Nakagawa et al., 2012; Gomes and Hurtgen, 2013; Crowe et al., 2014; Bradley et al., 2015), assuming organic matter is more limiting to allow a fractionation to occur (Wing and Haley, 2014; Bradley et al., 2015). Constrained whole cell (in vivo) laboratory experiments demonstrate that when electron donors are limiting, the magnitude of fractionation between sulfate and sulfide ($^{34}S$) carries a nonlinear inverse relationship with cell-specific sulfate reduction rates (Harrison and Thode, 1958; Kaplan and Rittenberg, 1964; Chambers et al., 1975; Sim et al., 2011b; Leavitt et al., 2013). Thus, the range of isotopic compositions produced and preserved in natural environments are interpreted as an output of intracellular rates, which scales with enzyme activity associated with microbial sulfate reduction (Goldhaber and Kaplan, 1975; Leavitt et al., 2013).

In addition to following a rate relationship, fractionation in MSR isotope studies often approaches characteristic upper and lower fractionation limits. Recent experimental work at low sulfate reduction rates captures a $^{34}S_{\text{MSR}}$ (the net isotope effect of microbial sulfate reduction) of nearly 70% (Canfield et al., 2010; Sim et al., 2011a). This magnitude of fractionation approaches the theoretical low temperature equilibrium prediction of 71.3 to 67.7% between 20°C and 30°C (Tudge and Thode, 1950; Farquhar et al., 2003), inspiring research more directly comparing the biologically catalyzed reversibility of MSR enzymes and that of equilibrium (Wing and Haley, 2014; see also Rees, 1973; Farquhar et al., 2003, 2008; Brunner and Bernasconi, 2005; Johnston et al., 2007; Mangalo et al., 2008; Bradley et al., 2011, 2015; Holler et al., 2011). These studies are fueled by the knowledge that direct (abiotic) equilibration between sulfate and sulfide at Earth surface temperatures is exceedingly slow, with a half-life of exchange estimated at $1.1 \times 10^{10}$ (at 30°C) to $1.6 \times 10^{12}$ years (at 20°C; these values are extrapolated from Ames and Willard, 1951). Thus, large fractionations between sulfate and sulfide at Earth surface conditions strongly suggest a role for biology, and likely multiple enzyme catalyzed steps with associated fractionations.

Most experiments with sulfate reducing microorganisms result in isotope fractionations much smaller than would be predicted from abiotic equilibrium estimates. Indeed, more than half a century of research and 648 observations from in vivo MSR experiments capture a median isotope fractionation of $^{34}S_{\text{MSR}} = 16.1\%$ (in both sulfate and sulfite reduction experiments: Figure 4). In fact, half of experimental data fall between 10 and 22.5%. This is consistent with the phenomenology of laboratory experiments being conducted at significantly higher sulfate reduction rates than occur in most natural settings. However, given that all these experiments occurred with the same biochemical network, any enzyme-level explanation for the range of fractionations observed at both high and low sulfate reduction rates must be internally consistent.

![Figure 4](http://dx.doi.org/10.6084/m9.figshare.1436115), where all compiled values are from the following sources: (Thode et al., 1951; Ford, 1957; Harrison and Thode, 1957, 1958; Jones and Starkey, 1957; Kaplan and Rittenberg, 1964; Kemp and Thode, 1968; Krouse et al., 1968; Chambers et al., 1975; McCready, 1975; McCready et al., 1975; Smoak et al., 1998; Bottcher et al., 1999; Bolliger et al., 2001; Detmers et al., 2001; Farquhar et al., 2003; Kleikemper et al., 2004; Habicht et al., 2005; Johnston, 2005; Canfield, 2006; Hoek et al., 2006; Knöller et al., 2006; Johnston et al., 2007; Mangalo et al., 2007, 2008; Pallud et al., 2007; Davidson et al., 2009; Sim et al., 2011a,b, 2012, 2013; Leavitt et al., 2013, 2014).
Fractionation at the Intracellular Scale

As described above, a suite of enzymes and cofactors drives dissimilatory sulfate reduction. During the reduction of sulfate to sulfide, sulfur isotope effects are likely to result primarily from transformations that involve the making or breaking S related bonds. Initial steps in sulfate reduction, such as transport into the cell and activation via a reaction with ATP to generate APS (Figure 1; Fritz, 2002), do not involve the formation of new S linkages, and are not predicted to be associated with primary isotope effects. Influence on the expressed isotopic fractionation due to transport limitation is, however, conceivable. That is, the concentration of sulfate in the cell may influence the expression of downstream isotope effects, altering the net observed \( ^{34}\varepsilon_{\text{MSR}} \). Sulfate transporters may also induce an isotope effect associated with varying membrane fluidity or other strain-specific optimia, in response to changing temperature (Kaplan and Rittenberg, 1964; Canfield, 2006), pH (Furusaka, 1961), or as environmental sulfate concentrations become metabolically limiting (Habicht et al., 2005; see discussion in Bradley et al., 2015).

Primary isotope effects are predicted where bonds are made or broken. APS reductase catalyzes a two-electron exchange that breaks a S-O bond during reduction of APS to generate free sulfite. From the crystal structure of ApsR (Fritz, 2002), it is apparent that the enzyme binds with the APS bound sulfur directly on a nitrogen in the FAD (flavin adenine dinucleotide) cofactor. The product sulfite is then available to interact with DsrAB. This heterodimeric enzyme binds sulfite in an active site containing siroheme. The formation of the Fe-S bond between siroheme and sulfite may be the critical reaction controlling isotope fractionation. Following this, sulfite is reduced by the transfer of two electrons to form a \( S^{2+} \) intermediate (Santos et al., 2015). Under in vivo conditions, the sulfur intermediate was suggested to be withdrawn from the DsrAB complex by the small transfer protein DsrC (Oliveira et al., 2008b; Venceslau et al., 2014), and this has been recently demonstrated (Santos et al., 2015). Under in vitro conditions, DsrC is generally absent, and the reduced sulfur in the active site may react with excess sulfite, forming thiosulfate and trithionate (Figure 1; Drake and Akagi, 1976). DsrC is independently regulated in vivo (Karkhoff-Schweizer et al., 1993), and generates the terminal sulfide from DsrAB-bound sulfur derived from sulfite (Venceslau et al., 2014). The relative importance of this protein has only been realized in the last few years (Oliveira et al., 2008b; Venceslau et al., 2014), and has an unconstrained isotope effect.

In general, the magnitude of the thermodynamically predicted sulfur isotope effect scales positively with the number of bonds are made or broken (Tudge and Thode, 1950; Bigeleisen and Wolfsberg, 1958). As described above, sulfite reduction by DsrAB is a central enzyme in MSR, breaking three S-O bonds (Oliveira et al., 2008b; Venceslau et al., 2014), and therefore knowing the fractionation associated with this step is critical to any predictive MSR isotope model (c.f. Rees, 1973; Brunner and Bernasconi, 2005; Farquhar et al., 2007, 2008; Johnston et al., 2007; Bradley et al., 2011, 2015; Wing and Halsey, 2014). Our direct constraint on the fractionation imposed by sulfite reduction indicates that the published assignments of 25% (Harrison and Thode, 1958; Rees, 1973) and 53% (Brunner and Bernasconi, 2005) for DsrAB are significant over-estimates. It is perhaps not surprising, given that previous appraisals were generated through various indirect approaches (Harrison and Thode, 1958; Rees, 1973; Farquhar et al., 2003; Brunner and Bernasconi, 2005; Johnston et al., 2007). As previously stated (Chambers and Trudinger, 1979), the lack of direct experimental constraints on enzyme-specific fractionation factors leave significant uncertainty in metabolic, geochemical, and geological models that simply assign values to each enzymatic step.

Enzymatic Constrains (This Study)

Our measured \( ^{34}E_{\text{DsrAB}} \) value for sulfite reduction (15.3 ± 2.0‰) is large enough to account for a large portion of the fractionations observed in published whole-cell MSR experiments over the last 65 years (median of 16.1‰, \( n = 648 \); Figure 5). As noted previously, laboratory experiments carry a strong bias toward higher rates of sulfate reduction, and as such, the data compilation should be viewed in this light. As most recently articulated through a series of chemostat experiments (Sim et al., 2011a; Leavitt et al., 2013), the consequence of elevated metabolic rate is a smaller relative \( ^{34}e \). In isotope biogeochemistry, relationships like this often depend on the single slowest overall rate-limiting step within a metabolism (Mariotti et al., 1981; Hayes, 1993). The fractionation limit at high metabolic rates in cultures \( (^{34}e = 17.3 ± 1.3%) \), marine sediments \( (^{34}e = 17.3 ± 3.8%) \) and DsrAB are statistically indistinguishable (Figure 5).

![FIGURE 5](image-url)
This similarity is consistent with DsrAB as a rate-limiting step explaining the majority of observed fractionation (Figure 5). However, this interpretation omits complexity associated with the metabolic network.

This raises an essential question: how does the DsrAB constraint change our understanding of the possible range of fractionations imposed by MSR? For instance, if we assume that DsrAB is the slowest reaction in MSR, then the metabolic steps preceding sulfite (SO$_4^{2-}$ ⇔ APS ⇔ SO$_2^{2-}$) will necessarily approach equilibrium (Wing and Halevy, 2014). The thermodynamic predictions would then require an accompanying fractionation approaching 25% between sulfate and sulfite at biologically relevant temperatures (the equilibrium fractionation estimate; Farquhar et al., 2003). At its simplest, this effect would be additive with that of DsrAB (25 + 15.3%, or 40.3%), which encompasses a majority of experimental MSR isotopic fractionations. However, the lower plateau in fractionation approached at high rates, stemming from the calculations using both modern marine sediment and chemostat data (see the Supplementary Material)—is less than half of this magnitude. That is, the lower plateaus for in vivo fractionation at high rates of 17.3‰ allows only a ≈2‰ fractionation partitioned among these upstream steps, if in fact DsrAB is fully expressed. This smaller “upstream” kinetic fractionation is, however, consistent with the few loose estimates from crude cell extracts and resting cell studies (i.e., not purified enzymes), which putatively suggests a $\Delta^{34}S$ of 4–15‰ for the cumulative activation of sulfate to APS and reduction to sulfite (Ford, 1957; Kemp and Thode, 1968). This may suggest that the sulfate-sulfite conversion (in vivo and in vitro) reflects a predominately kinetic (rather than equilibrium) control. This requires, however, we loosen the degree to which DsrAB is called upon to fully control the net MSR isotopic fractionation, invoking some delicate balance between upstream reactions and that of DsrAB, but maintaining the model where enzyme kinetics (especially DsrAB) will win out over equilibrium effects as sulfate reduction rates move from low to high.

An alternate explanation is that APS reductase (ApsR) is the rate-limiting step under sulfate replete conditions (Rees, 1973). If this is the case, fractionation imposed by DsrAB is unexpressed, as it is downstream of ApsR (Rees, 1973; Hayes, 2001). If fractionation associated with APS reductase is near 17‰, it could alone account for most of the observed fractionation observed at high sulfate reduction rates. The fractionation imposed by ApsR has not been directly measured, though can be preliminarily estimated from the discussion above. However, evidence against ApsR as the rate-limiting step is shown by studies indicating reversibility of the ApsR (Peck, 1960) and the sulfate reduction pathway (Chambers and Trudinger, 1975; Holler et al., 2011). Recent studies using oxygen isotopes as tracers have demonstrated that some intracellular sulfite is oxidized in vivo back to sulfate (Mangalo et al., 2007, 2008; Einsiedl, 2008; Farquhar et al., 2008; Turchyn et al., 2010). These studies demonstrate that sulfite re-oxidation is commonplace in MSR and often quantitatively significant (Antler et al., 2013). This reoxidation is inconsistent with ApsR being rate-limiting under the range conditions tested.

Any explanation for the net MSR isotopic fractionation must also account for the large fractionations observed at low sulfate reduction rates. These large fractionations are common in nature, and require another type of mechanism. These isotopic fractionations approach but do not reach the theoretical equilibrium values for sulfur isotope exchange between sulfate and sulfide (Figures 4, 5; Tudge and Thode, 1950; Farquhar et al., 2003; Johnston et al., 2007). In this context, further analysis to understand intracellular thermodynamics is critical (the redox pairs responsible for various reactions, see Wing and Halevy, 2014), along with measurements of the intrinsic isotope effects of other key enzymes in the metabolic network, including ApsR and DsrC. In that sense, this study represents a key first step.

In parallel to examining the $\Delta^{34}S$ effects, measuring minor S isotope ($^{33}S^{32}S$) fractionation provides additional information about the class of reaction mechanism associated with in vitro DsrAB activity. In our experiments, the conversion of sulfite to sulfonate carries a $\Delta^{33}S$ of from ~0.496 (±0.012, 2σ), evolving toward 0.510 as the reaction proceeds. Sulfite reduction via DsrAB has an invariant $\Delta^{33}S$ of 0.5150 (±0.0012, 2σ). In cases where $\Delta^{33}S$ is 0.515, a purely equilibrium fractionation is often inferred but not required, while values less than this require kinetic effects (Young et al., 2002; Farquhar et al., 2003). In this framework, in vitro sulfonate formation falls under kinetic control, while formation of reduced S could be interpreted as a kinetic or equilibrium reaction. Thus, specific predictions for the DsrAB enzyme require more detailed modeling of the structure and function of the DsrAB enzymatic active site. This level of analysis—where inroads joining empirical work with theory are constructed—is present in analogous systems (Karsh et al., 2012), but absent within the S cycle. Nonetheless, the work here provides the only triple-isotope constraints on enzyme-specific fractionation factors in both MSR and the global biogeochemical S cycle. Further, this approach may prove useful in other enzymatic systems where elements with ≥3 stable isotopes are involved (e.g., O, Fe, Ca, Mg, Se, Zn, and Mo).

CONCLUSIONS

Direct constraints on enzymatic isotope effects, when placed in context of laboratory and field observations, represent a key step toward improving our understanding of how environmental factors come to control biochemical sulfur isotope fractionations in nature. Experimental results indicate that the kinetic isotope effect generated by dissimilatory sulfite reductase, the enzymatic core of MSR, generates less than a quarter of the maximum fractionation observed in sulfate reduction experiments and modern marine sediments. However, the $\Delta^{34}S_{DsrAB}$ aligns nicely with the vast majority of experimental data generated over the last 65 years, as well as chemostat and marine sediment studies sampling high rates of sulfate reduction. The consistency between these published fractionations and the DsrAB isotope effect suggests a fundamental role of this enzyme in setting sulfur isotope compositions. This work highlights the need for further consideration of the allied enzymes in MSR and the likelihood of abiological (and/or equilibrium) effects as microbial sulfate reduction rates slow. Though questions remain,
placing quantitative constraints on a core component of sulfate reduction—DsrAB—represent a fundamentally new direction in exploring experimental and environmental sulfur isotope records today and throughout Earth history.

DETAILED METHODS

Operational Definitions of S Moieties

In this study we measured the concentrations of three pools: sulfite, trithionate, and thiosulfate; hydrogen sulfide was not detected. We measured the major and minor sulfur isotopic compositions of three operationally defined pools: “reactant” sulfite (initial and residual), product “sulfonate,” and “reduced product” S. What we refer to as the pooled product “sulfonate” sulfurs are known in inorganic chemistry as sulfuryl groups (O=S-X₂), where one of the X’s represents an O=O=O and the other a S in oxidation state 0 (trithionate) or −1 (thiosulfate), meaning the outer sulfuryl-S’s are in approximately oxidation state +5 (thiosulfate) or +4 (trithionate), with initial and residual reactant sulfite sulfur in the standard +4. The sulfonate S differs from sulfite S in that it is bound to either an approximately −1 valent sulfur in thiosulfate (S-S(O)32−) (Vairavamurthy et al., 1993) or as two sulfonates each bound to one sulfur of valence approximately 2+, in trithionate ((O₃S-S-SO₃)²⁻). In this study we refer to the 0 and −1 oxidation state sulfurs from trithionate and thiosulfate, respectively, as the “reduced product” S pool. They are grouped by our operational extraction (see below).

For explicit definitions and nomenclature refer to the “IUPAC Goldbook” (McNaught and Wilkinson, 1997).

Enzyme Purification and In vitro Experiments

DsrAB Isolation and Purification

DsrAB was purified from Desulfovibrio vulgaris Hildenborough (DSM 644) and Archaeoglobus fulgidus cells grown in a 30 or 300 L batch culture in a modified lactate/sulfate medium (Oliveira et al., 2008a) at iBET (Instituto de Biologia Experimental Tecnológica; www.ibet.pt), grown at 37 or 80 °C, respectively. The soluble cell fraction was obtained as previously described (Le Gall et al., 1994; Oliveira et al., 2008a). All purification procedures were performed under atmosphere at 4°C using an AKTA FPLC (Amersham Biotech Pharmacia) with two buffers, (A) 20 mM TrisHCl and (B) 50 mM TrisHCl with 1 M of NaCl (both pH 7.6 and containing 10% glycerol). Buffer (A) was used to equilibrate the columns and buffer (B) to generate theionic strength gradient. The soluble cell fraction was loaded into a Q-Sepharose fast-flow (26/10) column, and a stepwise salt gradient applied, with the DsrAB-containing fraction eluting at 300 mM NaCl. The characteristic DsrAB (“desulfoviridin”) absorption peak at 630 nm was used to track the protein, as previously described (Wolfe et al., 1994; Marriott and Hagen, 1996). DsrAB-containing fractions were then loaded into a Q-Sepharose fast-flow (26/10) column and eluted in 250 mM NaCl. To verify enzyme purity, the final DsrAB-containing sample was analyzed by 12% SDS-PAGE gel electrophoresis. DsrC is present in the DsrAB preparation from D. vulgaris, but remains functionally inactive during in vitro assays as previously described (Oliveira et al., 2008b), and also due to the lack of DsrMKJOP (Vencea et al., 2014). Thus, we refer only to the “DsrAB” fraction in the D. vulgaris experiments.

In the A. fulgidus experiments, DsrAB is free of any DsrC. Protein was quantified by the method of Bradford (Bradford, 1976). The Desulfovibrio gigas [NiFe] hydrogenase used in all assays was purified as described previously (Romão et al., 1997).

To ensure the activity of purified DsrAB was not strongly influenced by the high initial concentration of sulfite used in the fractionation experiments (10 or 15 mM), we performed small-volume kinetic assays under the same conditions as for isotope measurements. Sulfite alone was measured by HPLC on monobromobimane (MBBr) derivatized samples (Newton et al., 1981). Once the sulfite concentrations for each initial and final (0 and 2 h) time points were sampled, derivatized, measured and calculated, we applied a non-linear regression formulated from the standard Michaelis-Menten equation, solving for the Vₘₐₓ and Kₘₚ.

D. vulgaris DsrAB In vitro Fractionation Experiments in Detail

To determine the DsrAB-specific S isotope fractionation factors we designed and executed a series of batch (closed-system) sulfite reduction experiments. The key considerations in experimental design are: (i) to provide enough sulfite at t₀ to ensure we generate significant enough quantities of all the product pools so we can measure, at high precision and accuracy, and at multiple [time] points on f, the multiple S isotopic composition of each pool (i.e., 2 µmol of S per pool per SF₆ measurement on the DI-IRMS, which means 2 µmol per fluorination reaction); (ii) to provide the proper reaction conditions to allow DsrAB optimal activity for goal (pH = 7.1, T = 20 or 31°C); (iii) to ensure hydrogenase activity is not inhibited by the pH chosen (optimum above pH 7.5, activity significantly depleted below pH 6.5, so we chose pH 7.1, to account for optima of both DsrAB and [NiFe]-Hydrogenase); and finally (iv) to ensure the sulfite to hydrogen ratio favors sulfite over reductant capacity (i.e., pH₂ in the headspace relative to [sulfite]₀), such that no more than 75% of t₀ sulfite is consumed to all products, and less than 50% to the reduced S (dictated by the amount of H₂ in the headspace. Finally, (v) determining the sampling interval to ensure proper distribution of points along f, such that applying a closed system distillation model is possible, and statistically robust. Data plotted in Figure 3 represents experimental results that met all of these conditions. The full experimental results (33 experiments) are contained as a supplemental file (http://dx.doi.org/10.6084/m9.figshare.1436115).

All experiments were prepared in an anaerobic chamber. In vitro reactions were carried out in 100 mL acid-washed, autoclave-sterilized, borosilicate glass bottles sealed with butyl-rubber septa and aluminum crimps. Each bottle contained 50% reaction buffer and 50% gaseous headspace. This was done to sufficient H₂ was present in the headspace to reduce at most 50% of the sulfite, based on an estimate using Henry’s law and available solubility constants for H₂ at the given preparation temperatures and headspace pressures. During manipulations in the anaerobic chamber the chamber gas was initially 95.5 N₂:H₂. Upon
removing the reaction mixture-filled bottles from the chamber, these were capped and crimped, and headspace completely exchanged with deoxygenated 100% Ar, then finally exchanged for 100% H2 to initiate the experiments. Experimental buffer is 50 mM phosphate buffer (KPi) prepared at pH 6.9 ± 0.05, with final pH is 7.1 ± 0.05 following the addition of the stock Na2SO3 solution (the reaction is therefore initiated at 7.1). All reaction solutions contained the following: 50 mM KPi buffer (final pH 7.1 ± 0.05), 10 or 15 mM sodium sulfite, 0.832 mM methyl viologen, 242 nm or 315 nm of D. vulgaris DsrAB (calculated to give the same activity depending on the DsrAB aliquot selected), and 8.25 nm [NiFe] hydrogenase (297 U/mg). All experimental mixtures and reagents were prepared in previously boiled 18.2 MΩ water, cooled under O2-free N2.

**A. fulgidus DsrAB In vitro Fractionation Experiments in Detail**

To extend our studies to a different taxonomic form of the enzyme, we used DsrAB from the thermophilic archaeon A. fulgidus. This enzyme operates at higher temperature and does not have DsrC present in the complex (Schiffer et al., 2008). The results from these experiments are significantly limited compared to those with D. vulgaris, due to too few time points to apply the closed-system model (specifically due to significantly low sample sizes of reduced S for isotope measurements, note the effort made to correct the two data points on *A. fulgidus* reduced-S). Nevertheless, the results obtained are comparable, when considering the measured δ34S. The values for these experiments are presented with *D. vulgaris* values in Figure A2.

**A. fulgidus** DsrAB experiments were conducted 15 mM initial sulfite and 65°C, and showed consistent loss of sulfite and accumulation of products between replicates. We selectively precipitated, separated, and directly measured the 32S, 33S, 34S, 36S compositions from the residual reactant (“sulfite S”) and the “sulfonate S” ([SO3]2−). Only the 34S/32S compositions of the “reduced product S” ([S]2−) reservoirs were measured (again, due to significantly small reduced-S samples recovered). From these experiments we were able to get a complete set of samples (i.e., sulfite, sulfonate, and reduced S) from one time-point and partial sets from another (i.e., sulfite and sulfonate). We are unable to calculate the 34E_DsrAB for *A. fulgidus* directly using our model of sulfite reduction experiments due to the dearth of time points (points on f). However, the *A. fulgidus* isotope values agree with those measured sulfite, sulfonate, and reduced S moieties for *D. vulgaris* (Figure A2). This general agreement between *D. vulgaris* and *A. fulgidus* DsrAB, independent of temperature or phylogenetic origin is perhaps unsurprising, given that previous theoretical predictions deemphasize the role of temperature in determining the magnitude of kinetic isotope effects (Bigeleisen and Wolfsberg, 1958). Furthermore, these enzymes tightly share active site structures (Oliveira et al., 2008b; Parey et al., 2013).

**Analytical Methods and Data Handling**

**Quantification of Dissolved Species**

To quantify sulfite and bisulfite concentration in solution we adapted a protocol to quantify SO2 dissolved in water (Grant, 1947), referred to as the “Fuschin” assay from here forward. Our protocol is specific to the in vitro DsrAB assay conditions. It was determined that matrix matching between samples and standards and the exclusion of oxygen is critical to a successful and reliable assay. Furthermore, we determined trithionate, thiosulfate, sulfate, and zinc sulfide solids do not interact with this color-reactent in the assay. The Fuschin assay is useful over a range of 0–40 nanomoles of sulfite in the final assay volume of 1 mL. Standards of sodium sulfite (Na2SO3 anhydrous, analytical grade) were prepared immediately before the assay is performed in deoxygenated water (boiled and degassed with N2) or KPi buffer. The reaction mixture is composed of 0.04% w/v Pararosaniline HCl (analytical grade) in 10% H2SO4 (analytical grade) v/v, prepared stored in an aluminum-foil wrapped tube or amber-glass bottle at 4°C, and 3.7% formaldehyde (HCHO) prepared fresh each day by diluting 37% (stock) formaldehyde 1:10 water. The reaction is performed on the bench working under N2 flow, or in an anaerobic chamber. A detailed step-by-step protocol is available in Leavitt (2014).

Trithionate and thiosulfate were measured by a modified cyanolysis protocol (Sörbo, 1957; Kelly et al., 1969; Kelly and Wood, 1994). We primarily employed the method of Kelly and Wood (1994) modified in the following manner: the reaction volumes were reduced to 10 rather than 25 mLs (still in volumetric flasks) and we used nitric rather than perchloric acid. Nitric acid was used in the original version of this method (Sörbo, 1957), allowing us to avoid the significant hazards of working with significant volumes of perchloric acid. Samples were added to the reaction buffer to fit within the range of ferric thiocyanate standards (prepared from potassium thiocyanate as a simple standard and thiosulfate as a reaction standard) from 5 to 25 µM (final concentration in the 10 mL reaction), as well as “blanks” prepared from the in vitro assay reaction buffer (50 mM potassium phosphate buffer at pH 7). This is typically 400 µL of in vitro solution added to the 10 mL cyanolysis reaction, in duplicate per method (2X thiosulfate determinations and 2X trithionate determinations). A detailed step-by-step protocol is available in Leavitt (2014).

For sulfide quantifications, we preserved samples in zinc acetate (2% w/v) from each closed system reaction, using a modified Cline method (Cline, 1969). Analytical grade sodium sulfide (>98.9% Na2S9H2O) was used as the standard, and prepared in deoxygenated (boiled and N2-sparged) in vitro reaction buffer, by precipitating the sulfide with excess zinc acetate (anhydrous), mimicking our sampling protocol. A detailed step-by-step protocol is available in Leavitt (2014). In all samples no sulfide was detected above the determined detection limit of 6.25 µM. From the literature reports where membrane fractions were omitted (Drake and Akagi, 1978), signifying a lack of DsrC re-cycling mechanism (Oliveira et al., 2008b; Bradley et al., 2011), we expected little to no sulfide. This is further supported by the closure of S mass balance at each time-point from each experiment, within analytical error (see main text). Blanks were prepared identically to those in the cyanolysis protocol.
Sample Preparation for S Isotope Analysis

All S-bearing samples for S-isotope analyses (ultimately as SF₆ and/or SO₂) were removed from the in vitro reaction solution (50 mM potassium phosphate) following a sequential precipitation protocol, inspired by that of Smock et al. (1998). Our protocol reflects our specific experimental setup and the pools we aimed to isolate and purify: sulfite (and any trace sulfate), sulfonate, and reduced product S. Samples of the residual reactant (sulfite) and pooled products (reduced product S and sulfonate S) were removed from the in vitro reaction mixture by sequential precipitation and filtration or centrifugation to isolate solid-phases Ag₂Sₐ (reduced product), BaSO₄ₐ (sulfite), BaSO₄₀ (sulfonate) by the extraction scheme modified from our recent work (Leavitt et al., 2014) and detailed elsewhere (Leavitt, 2014). Samples were captured as BaSO₄ₐ, BaSO₄₀, or Ag₂Sₐ, respectively. Sub-samples of the reduced product Ag₂S were directly fluorinated (after the below washing steps were carried out to ensure clean Ag₂Sₐ), or in the case of the sulfonate S-pool, collected from the AVS residue and converted from BaSO₄ to Ag₂S by the method by Thode (Thode et al., 1961), according to the protocol we recently published (Leavitt et al., 2013). Novel to this study: all sulfite samples (reacted as BaSO₄ₐ) were oxidized with peroxide prior to “Thode”-reduction (detailed protocols for these methods are available in Leavitt, 2014). All samples entering the elemental analyzer isotope ratio mass spectrometer (EA-IRMS), and combusted to and analyzed as SO₂, were prepared as dry BaSO₄ₐ, BaSO₄₀, or Ag₂Sₐ. All samples for quadruple S isotope analysis enter the fluorination line as pure dry Ag₂Sₐ.

Major S-isotope (³⁴S/³²S) Ratios Measurements

Continuous flow isotope ratio mass spectrometric (CF-IRMS) measurements of the three S-bearing pools of interest, sulfite, sulfonate and reduced product S, were performed as follows: 0.4 mg (±0.05 mg) BaSO₄, BaSO₄₀, or Ag₂S were converted to SO₂ by combustion at 1040°C in the presence of excess V₂O₅ (Elementary Analyzer, Costech ECS 4010) and analyzed by continuous flow isotope ratio mass spectrometry (SD = ±0.3‰; Thermo-Finnegan DELTA V Plus). All samples yielded clean chromatography and most m/z 66 amplitudes (corresponding primarily to the (¹⁶O³⁴S⁶O) ionization product) within the range of in-run standards (IAEA: S1, S2, and S3 for Ag₂S or SO₅, SO₆, and NBS-127 for BaSO₄ and BaSO₃). Some sulfite precipitates (BaSO₄ₐ), though not any of the sulfate or sulfide precipitates (BaSO₄ₐ sulfonate or Ag₂Sₐ reduced product) produced atypical weight to m/z 66 response to what we regularly note with lab standards of BaSO₄ or BaSO₄₀ – specifically the signal was less than predicted, likely due to occlusion of phosphates (from the in vitro reaction buffer) in the barium sulfite matrix. As a result, we use the m/z 66 to BaSO₃ weight ratio (mg of BaSO₃ per unit area of the m/z 66 peak) to calculate the desired sample weight to achieve standard signal size, re-weighed and re-combusted/measured the requisite samples, and in all cases achieved m/z 66 peak areas in the range of our IAEA BaSO₄ and in-house BaSO₃ standards. Each standard is measured at least 4x in-run and each sample 2-3x (when sufficient sample is available). This simplifies the scale-conversion calculation for taking samples referenced in-run to in-house standard tank gas (HAR1_SO₂) and ultimately to the international reference frame (V-CDT).

Multiple S-isotope (³³S/³²S, ³⁴S/³²S, ³⁶S/³²S) Ratio Measurements

Dual-inlet (DI-IRMS) measurements of all four stable S isotopes (³²S, ³³S, ³⁴S, ³⁶S) from the three S-bearing pools of interest, sulfite, sulfonate and reduced product S, were performed as previously described (Leavitt et al., 2013, 2014). Briefly, all samples for quadruple S-isotope analysis, prepared dry and clean Ag₂S (described above), were fluorinated under 10X excess F₂ to produce SF₆, which is then purified cryogenically (distilled at −107°C) and chromatographically (on a 6 molecular sieve 5 Å inline with a 6’ HaySepQ 1/8”-stainless steel column, detected by TCD). Purified SF₆ was measured as SF₆′ (m/z of 127, 128, 129, and 131) on a Thermo-Finnegan Scientific MAT 253 (SD: δ³⁴S ±0.2, Δ³³S ±0.006‰, Δ³⁶S ±0.15‰). All isotope ratios are reported in parts per thousand (‰) as experimentally prepared sulfates and sulfides measured. Long-term running averages and standard deviations are calculated from measures of IAEA standards: S1, S2, S3 for sulfides or NBS-127, SO5, SO6 for sulfates. Isotope calculations and notation are detailed in the text. Standard deviations for each value is estimated as reported previously (Johnston et al., 2007) with previous inaccuracies in the transcription corrected here.

Scale-Compression Correction Calculations for Small S Samples

Experiments with A. fulgidus yielded small amounts of product (0.35 to 0.01 mg), which required additional data handling during isotope analysis. Given the small size of these samples, we ran each sample only once and bracketed the samples (n = 2) with a series of standards: IAEA S1, S2 and S3 (n = 16, 14, and 14, respectively) run over a size series that captured the sample sizes, all by CF-IRMS only. As expected, we observed that the measured isotopic composition of the standards varied non-linearly as a function of signal intensity (monitored as peak integrated areas and peak intensities on m/z 64 and 66 for SO₂ and 48 and 50 for SO⁺). The size dependence on the isotopic composition (handled as ⁵⁰R and ⁶⁰R, which are the 50/48 and 66/64, respectively) scale compression is calculated as a proportional change. For SO (correction factor in Figure A3) it scales as: 

\[
\frac{R_{\text{predicted}} - R_{\text{measured}}}{R_{\text{predicted}}} = \frac{50}{50}
\]

We focus on SO here as these samples yielded sharper chromatography on slightly different sized signals (due to resistor differences between SO and SO₂ cups – 3 × 10¹⁰ Ω and 1 × 10¹⁰ Ω respectively). Thus, using the three IAEA standards, we developed a correction whereby we solve (in the standards) for the non-linear features of the data as it relates to signal intensity (here monitored as the peak integrated area on mass 48 – ³²SO). This is shown in Figure A3. After this correction is applied to ⁵⁰R measured, SO data is converted to an SO₂ scale (see Figure A3), which is a linear transfer function again derived from IAEA standard data. The final correction places all the data (now on a SO₂ scale against in-house reference SO₂ tank gas) to the V-CDT scale. To review, we perform the following steps (1) correcting the ⁵⁰R on SO for sample size, (2)
convert $^{50}$R to $^{64}$R (against tank gas), and finally (3) convert all data to a VCDT scale.

The largest source of error in this treatment is associated with the sample size correction. As such, we propagate the error associated with the fit in Figure A3 to determine the uncertainty in the final isotope value. As expected, for small samples this error is quite large (Figure A2), with the value decreasing in absolute magnitude as signal intensity (peak integrated area) increases. We also compare these error estimates to the calculated shot noise for this measurement (pink line in Figure A3d). As is presented below, our regressed error is in excess of the shot noise limit. Similarly, the error on the population of standards that were used in deriving this fit is 1% ($n = 44$).

The Closed-System Distillation Model for a More Complex Network

There exists the possible mixing of multiple fractionation factors later in the experiment ($f < 0.85$). The approach outlined in the main text yielded results in which the observed fractionation factor between sulfite and reduced pools appeared to change as a function of $f$, when $f < 0.85$—that is, later in the reaction, when back-reactions are more likely (Figure A4). One explanation for this apparent behavior is that the reduced pool is not the product of a single set of reactions but of multiple reactions. The most plausible explanation for this is that some fraction of the reduced pool is derived from the sulfonate pool rather than being derived solely from sulfite, particularly later in the in vitro experiment (i.e., at values of $f < 0.85$). Previous work (Drake and Akagi, 1977, 1978; Parey et al., 2010) has demonstrated that DsrAB is capable of reducing trithionate to thiosulfate, and thiosulfate to sulfite and sulfate, which was confirmed with the D. vulgaris enzyme.

We can constrain the magnitudes of the fractionation factor related to the conversion of the sulfonate to reduced S through the following steps. First, utilizing the framework given above to solve for $\alpha_{\text{red}}$ for the time points where $f$ is nearest to 1. As these measurements are obtained at the lowest concentrations of product, we assume that this result gives an estimate for $\alpha_{\text{red}}$ that reflects the production of reduced S from sulfite only, with minimal input of reduced S derived from sulfonate. Second, we write an equation for $R_{\text{red}}$ as a function of $\alpha_{\text{red}}$, $R_{\text{SO}_3}$, and $R_{\text{ox}}$:

$$ R_{\text{red}} = X_{\text{SO}_3}\alpha_{\text{red}}R_{\text{SO}_3} + (1 - X_{\text{SO}_3})\alpha_{\text{unk}}R_{\text{ox}} $$

where $X_{\text{SO}_3}$ is the fraction of $R_{\text{red}}$ generated directly from sulfite and $\alpha_{\text{unk}}$ is the unknown fractionation factor between $R_{\text{ox}}$ and $R_{\text{red}}$. This equation is then rewritten and solved for $\alpha_{\text{unk}}$ as a function of the other parameters over a range of values of $X_{\text{SO}_3}$ (0.01–0.99). This does not yield a unique solution for the unknown fractionation, but constrains its value given the relative importance of the contribution to the reduced sulfur pool of both sulfonate and sulfite. We assume that the relative contribution of the secondary reaction is invariant over the course of the reaction, thereby manifesting as no change in $f$.

Error Propagation Calculation for the Closed System Model Estimates

The error associated with calculations of $\delta^{33}\lambda$ (approximately the slope of a $\delta^{33}$S vs. $\delta^{34}$S line) is highly sensitive to the length of the line (total $\delta^{34}$S range, $\delta^{34}$,$\delta^{33}$) and modestly related to the residual around a mass-dependent theoretical prediction (the standard deviation on $\Delta^{33}$S is often used here (Farquhar et al., 2003; Johnston et al., 2007). To approximate the standard deviation ($\sigma$) associated with our $\delta^{33}\lambda$ calculation, we propagate our measurement errors ($\delta^{34}$S, concentration, etc.). We keep with the presumption that mass-dependence will dictate the $\delta^{33}$S, once the new $\delta^{34}$S is calculated. This stems from the fact that the error in $\delta^{34}$S and $\delta^{33}$S are highly correlated, meaning that the error in $\delta^{33}$S is significantly smaller (0.008%o) than that for $\delta^{33}$S (0.1%o). As our fractionation factor model is based on a closed-system distillation equation (see above), we perform an error propagation on an equation of the form: $R_f = (R_0) (\eta^{\alpha-1})$, where we are most interested in accounting for the analytical errors on the isotope measurement ($\sigma_R$, 0.2%/1000) and the uncertainty on $f$. The second term is critical here as we are independently determining $f$ from concentration measurements in the experiment, with a standard deviation on sulfite concentration measurements of 3%. We use this value moving forward as a metric of $\sigma_f$. To simplify the presentation, we set $X = (\alpha - 1)$ and $Z = f$. Following typical error propagation for power law and multiplicative relations (Bevington and Robinson, 2003 p. 43–46), we find:

$$ \sigma_Z/Z = \sqrt{(X\sigma_f/f)^2} $$

which then can substitute into the final form of:

$$ \sigma_R/\delta = \sqrt{(\sigma_Z/Z)^2 + (\sigma_{R_0}/R_0)^2} $$

The $\eta\sigma_{Rf}$ is then converted into %o units (through multiplying by 1000) so that it can be inserted into the updated (Johnston et al., 2007) error equation for $\delta^{33}\lambda$, presented here:

$$ \sigma_{\delta^{33}\lambda} = \sqrt{\sigma_{\Delta^{33}\lambda}^2 * (\frac{\partial \lambda}{\partial \Delta^{33}\lambda})^2 + \sigma_{\delta^{34}\lambda}^2 * (\frac{\partial \lambda}{\partial \delta^{34}\lambda})^2} $$

which can be broken down into:

$$ \frac{\partial \lambda}{\partial \Delta^{33}\lambda} = \left\{ \frac{1}{\ln (\frac{\delta^{34}\lambda}{1000} + 1)} * \frac{1}{\Delta^{33}\lambda + \frac{\delta^{34}\lambda}{1000} + 1} \right\} * \frac{1}{1000} $$

and

$$ \frac{\partial \lambda}{\partial \delta^{34}\lambda} = \left\{ \frac{1}{\ln (\frac{\delta^{34}\lambda}{1000} + 1)} * \frac{1}{{\Delta^{33}\lambda + \frac{\delta^{34}\lambda}{1000} + 1}} \right\} * \lambda_{RFL} \left( \frac{\delta^{34}\lambda}{1000} + 1 \right) ^ {\lambda_{RFL} - 1} * \frac{1}{1000} $$
As noted above, the error on lambda $\sigma_{\lambda}$ is dependent on the $\delta^{34}\text{S}$ and $\Delta^{33}\text{S}$. The subscript RFL represents the reference fractionation line, which for $^{33}\lambda$ is 0.515, and for $^{36}\lambda$ is 1.90. Data for $\delta^{36}\text{S}$ are not discussed in the text, as they yield the same conclusions as $\delta^{33}\text{S}$, but are included here in Dataframe S1 (https://github.com/bradleylab/DsrAB_enzyme_models).

In total, this leaves our error estimate a function of the following five variables: $^{34}\epsilon$, $\sigma_{R}$, $f$, $\sigma_{f}$, and $\alpha$. The final error is not an evenly weighted sum of these variables, and in the case presented here, most heavily influenced by the error in concentration data ($\sigma_{f}$). A sensitivity analysis (Figure A6) on this exercise demonstrates that the errors in $f$ far outweigh the analytical uncertainty in a measurement of $R$, and dominate the magnitude of the final $\sigma_{Rf}$.

Data Compilations and Statistical Analysis

Compilation and Statistical Analysis of Pure-Culture MSR Fractions

To place our DsrAB enzyme-specific fractionation factor in context with the previous 65 years of pure-culture experimental work, we compile all available observations from studies using axenic cultures of MSR (Figure 4), in the following experimental systems: batch (closed-system, in vivo, whole-cell), chemostat (open-system, in vivo, whole-cell), resting (closed-system, in vivo, whole-cell, not growing), cell-free (closed-system, ex vivo crude cell extracts, not growing). From these four types of experiments we further subdivide experiments into where sulfate was reduced to sulfide or sulfite was reduced to sulfide. We count each experimental determination ($^{34}\epsilon_{r-p}$) and compile them all in the supplemental data files (http://dx.doi.org/10.6084/m9.figshare.1436115), from experiments where less than 10% of the reactant $S$-species was consumed. Herein we calculate and present column statistics (box-whisker plots in Figure 4) using Prism5c (GraphPad, San Diego, CA). The key finding here is that the majority of the means from each set of experiments is significantly less than the previous estimates for the fractionation factor associated with DsrAB (25 to 53%, Harrison and Thode, 1957; Rees, 1973; Farquhar et al., 2003; Brunner and Bernasconi, 2005; Johnston et al., 2007), and that the mean values from all 650+ experimental determinations, regardless of experiment type or whether it was a sulfate-sulfide or sulfate-sulfite experiments, the mean for $^{34}\epsilon_{r-p}$ falls at 17.9% (median at 16.1%), with the 25th and 75th percentiles falling at 10% and 22.5%, respectively (Figure 5)—these are all well within the maximum fractionation accounted for by the sum of our DsrAB value (15.3%) and our literature derived range for sulfate reduction to sulfite (4 to 15%), for a total of 19.3 to 30.3% (see main text).

Literature Estimates of Fractionation during Sulfate Activation to Sulfite

The upstream kinetic isotope fractionation, the result of enzyme mediated sulfate/sulfite exchange in cell-free extract experiments, is between 4 and 15% (compilation files: http://dx.doi.org/10.6084/m9.figshare.1436115). The mean of these experiments is $^{34}\epsilon_{\text{SO}_4/\text{SO}_3} = 9.5\%$, $\text{Ci}_{35}\% = 7.2$ to 11.9%, with and $n = 12$ (column statistics are also permanently available at: http://dx.doi.org/10.6084/m9.figshare.1436115) (Ford, 1957; Harrison and Thode, 1958; Kaplan and Rittenberg, 1964; Kemp and Thode, 1968). Deconvoluting this aggregated fractionation factor ($^{34}\epsilon_{\text{SO}_4/\text{SO}_3}$ in vitro) is a target for future pure enzyme experiments focusing on the constituent steps (enzyme specific $^{34}\epsilon$), as well as the minor isotope fractionations associate with each (i.e., $^{33}\lambda$'s).

These values represent the fractionation across the sum of the steps incorporating sulfite activation to APS and its concomitant reduction to sulfite (Figure 1). It is important to note that these values were determined using crude-cell extracts, rather than purified enzymes, and not measured over a range of reaction progress (as in Figure 2). Further, available data do not allow for the evaluation of mass balance closure, as we have done here for DsrAB. Given our present understanding of the enzymes involved in this process (Bradley et al., 2011; Pereira et al., 2011), sulfate transport into the cytoplasm followed by activation to APS (Sat) are not likely to directly impact $S$-isotope compositions, whereas the reduction of APS (APSr) most likely does, due to the breaking of a S-O bond. The sum of transport, Sat and APSr fractionations sit immediately upstream of the DsrAB. Both of these constraints ($^{34}\epsilon_{\text{SO}_4/\text{SO}_3}$ and $^{34}\epsilon_{\text{DsrAB}}$) are interpreted in the context of the MSR data compiled from the literature, which includes lab experiments, natural waters and sediments, as discussed in the main text (Figure 5).

Statistical Analysis of Laboratory Chemostat and Marine Sediment Fractions

To apply the compiled sedimentary sulfate reduction rates from Goldhaber and Kaplan (1975), we re-plot their log-scale values to a linear scaling (Figure 5) and apply the same non-linear regression one-phase decay model ($Y = (Y_0-\text{Plateau}) e^{-KX} + \text{Plateau}$) from our recent work on fractionation—rate relationships in MSR (Leavitt et al., 2013), minimizing variance to arrive at the following parameters: $Y_0 = 73\%$, plateau = 17.3%, and a decay-constant ($K$) of 6.4 (Figure 5). For the chemostat (open-system) MSR data in the study where we derived this regression model (Leavitt et al., 2013), we re-scale the cell-specific MSR rates to basic volumetric fluxes by multiplying out the number of cells at each sampling point, using the chemostat values from our recent study (Leavitt et al., 2013). Applying the same one-phase decay model and minimize variance, we calculate the following parameters: $Y_0 = 56.5\%$, plateau = 17.3%, and a decay-constant ($K$) of 0.054.
All regressions were calculated using Prism5c (GraphPad, San Diego, CA).

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SUPPLEMENTARY MATERIAL

The Supplementary Material for this article can be found online at: http://journal.frontiersin.org/article/10.3389/fmicb.2015.01392

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Miller, M. F. (2002). Isotopic fractionation and the quantification of 17 O anomalies in the oxygen three-isotope system: an appraisal and geochemical


Conflict of Interest Statement: The authors declare that the research was conducted in the absence of any commercial or financial relationships that could be construed as a potential conflict of interest.

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FIGURE A1 | Activity assays with *D. vulgaris* DsrAB. The difference between initial and final concentration of sulfite after 2 h was used to calculate the rate. The Michaelis-Menten equation ($Y = \frac{V_{\text{max}} X}{K_M + X}$) was solved for experimental $K_M$ and $V_{\text{max}}$ under our conditions. The analytical error is less than the size of the symbols ($2\sigma = 1 \mu$M). One unit (U) is defined as the quantity of enzyme that catalyzes the conversion of one micromol of substrate per minute. At both 10 and 15 mM initial sulfite we are assured to be well above the apparent DsrAB $K_M$ for sulfite. Reaction inhibition was not observed at sulfite concentrations as high as 50 mM (Wolfe et al., 1994; Soriano and Cowan, 1995).
Leavitt et al. Sulfur Isotope Effects of DsrAB

**FIGURE A2** | The major isotope ratios ($^{34}\text{S}$) reported relative to the composition of sulfite at $t_{0}$, for the *A. fulgidus* (closed symbols) and *D. vulgaris* (open symbols) experiments both as a function of reaction progress. The samples sets show a general consistency, particularly at the reduced S sites, despite the significant offset in temperature (20–30°C for *D. vulgaris* relative to 65°C for *A. fulgidus*), consistent with kinetic theory (Bigeleisen and Wolfsberg, 1958), where temperature should impart a minimal effect over this range. The asymmetric error bars on reduced S moieties are a function of the non-linear correction for small sample sizes available for isotope.

**FIGURE A3** | The size series correction calculated from IAEA standards ($n = 44$). (A) Shows the calculated residual around that fit, demonstrating a symmetric distribution that scales with peak area. This is an illustration of the goodness of the fit. (C) The regression used to convert SO data to an SO$_2$ scale. (D) The calculated shot noise for SO as a function of signal intensity (peak height in mV). This precision limit is below that which we propagate through the correction, and is provided for reference here.
**FIGURE A4 | Reaction topology for closed-system models.** (A) The simple model for early in the experiments ($f > 0.85$). (B) Shows a more complex reaction model that may be applicable later in the closed-system experiments ($f < 0.85$). Sulfite is present in light blue, reduced S is in red and the sulfonate moieties are in purple. Black (A,B) arrows represent the simple reduction of sulfite by DsrAB and then formation of thiosulfate and trithionate by combination of that partially reduced S with other sulfite molecules. The green arrows (B) represent the more complex scheme in which trithionate is then further reduced, releasing a sulfite and a thiosulfate.

**FIGURE A5 | The relationship between the magnitude of a secondary fractionation ($^{34}\alpha_{\text{secondary}}$) and the proportion of reduced sulfur deriving directly from sulfite reduction ($X_{SO_3}$).** The balance ($1 - X_{SO_3}$) is from the parallel reduction of bound sulfonate. Errors estimates are from the propagation calculation, incorporating both isotope and concentration analysis analytical errors (see below).

**FIGURE A6 | A series of frames (A–C) describing the origin and sensitivity of the controls on the resultant error in $\delta^{34}S$ and $\Delta^{33}S$, plotted in Figures A2, A3.** For this analysis, $^{34}\epsilon$ is set to 15.3/permil to be consistent with the reductive branch of the DsrAB experiments, the analytical precision of an isotope measurement is 0.2/permil in $\delta^{34}S$ and 0.008/permil in $\Delta^{33}S$, and $f$ is allowed to vary from 0.6 to 0.9 in 0.02 increments (noted by circles). This range in $f$ is chosen to reflect the experimental range, and the circle is filled where $f = 0.9$. In (A), the covariance of the relative error in $f$ ($\sigma_f/f$) is show to correlate with the error in the relative isotope ratio, $\sigma_R/R$. As the calculated error in the $R$ derived from the Rayleigh equation ($\sigma_R$) increases, the consequence is an increase in the error in $\Delta^{33}S$ (B). Finally, the relationship between the errors in both $f$ and $R$, as they contribute to the error on $\Delta^{33}S$, are presented in frame C. Frames B,C do not approach the origin as a result of $f$ not approaching the limits of 0 and 1, and also due to the multivariate nature of the propagation.