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Within-Host Selection Is Limited by an Effective Population of *Streptococcus pneumoniae* during Nasopharyngeal Colonization

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*Streptococcus pneumoniae* (pneumococcus) is a significant pathogen that frequently colonizes the human nasopharynx. Environmental factors, including antimicrobial use and host immunity, exert selection on members of the nasopharyngeal population, and the dynamics of selection are influenced by the effective population size of the selected population, about which little is known. We measured here the variance effective population size ($N_e$) of pneumococcus in a mouse colonization model by monitoring the frequency change of two cocolonizing, competitively neutral pneumococcal strains over time. The point estimate of $N_e$ during nasal carriage in 16 BALB/c mice was 133 (95% confidence interval [CI] = 11 to 203). In contrast, the lower-bound census population exhibited a mean of 5768 (95% CI = 2,515 to 9,021). Therefore, pneumococcal $N_e$ during nasal carriage is substantially smaller than the census population. The $N_e$ during day 1 to day 4 of colonization was comparable to the $N_e$ during day 4 to day 8. Similarly, a low $N_e$ was also evident for the colonization of pneumococcus in BALB/c mice exposed to cholera toxin 4 weeks prior to challenge and in another mouse strain (DO11.10 RAG$^{-/-}$). We developed a mathematical model of pneumococcal colonization composed of two subpopulations with differential contribution to future generations. By stochastic simulation, this model can reproduce the pattern of observed pneumococcal $N_e$ and predicts that the selection coefficients may be difficult to measure *in vivo*. We hypothesized that such a small $N_e$ may reduce the effectiveness of within host selection for pneumococcus.

Studies of within-host competition between bacteria typically measure selection by the mean change in the logarithm of the ratio of a favored to a disfavored allele (1–4), sometimes called a “competitive index.” In animal experiments, there is often substantial variation in the competition outcome among animal subjects (1–4), which necessitates the use of a large number of animals to ensure reproducible results (5). Understanding the source of this variation is important for a number of purposes, including sample size calculations in experimental design and results interpretation. For example, modern methods for identifying genes important for fitness in certain environments, such as transposon mutagenesis screens, rely on the ability of many members of a large inoculum to establish infection, so that variations in mutant frequency may be attributed to selection rather than chance. From the opposite perspective, predictions of quantitative models of selection within a host for immune escape or emergence of resistant variants depend not only on the strength of selection but also on the number of pathogen individuals available for selection (3, 6, 7).

The variation in competitive index in experiments is rarely commented on, as if the presence of noise in results was an inevitable consequence of animal experiments. Stochasticity introduced by population bottlenecks and by small effective population size can also contribute to the observed variation. Since the first transposon mutagenesis study that relied on interpretation of allele frequency change to infer fitness effects of gene knockouts (8), this has been an important issue that needs to be accounted for implicitly or explicitly (9). In population genetics, stochasticity in the fate of alleles under selection (as well as that of neutral alleles) is explained by the concept of effective population size, which intuitively is related to the number of individuals in each generation who contribute to the next (10), making allowance for the fact that contributions may be uneven for many reasons. More precisely, the effective size of a population ($N_e$) is defined by the value that produces an observed distribution of changes in the frequencies of unselected alleles due to stochasticity in the reproduction of a finite population and can be estimated from this distribution, with a larger $N_e$ corresponding to smaller stochastic fluctuations (10). $N_e$ is an important parameter in understanding the dynamics of population diversity since it controls, among other genetic processes, the effectiveness of selection relative to genetic drift. A small $N_e$ increases the relative weight of genetic drift over selection in determining allele frequency, so that the difference between the chance of fixing a favorable mutation and the chance of fixing a neutral mutation in the population is reduced (10). Because bacterial pathogens usually show large census populations (i.e., the number of CFU per host), many experiments have been performed with the assumption that the median or mean change in frequency of one variant compared to another is a good representation of the selective value of those variants *in vivo* (1, 2, 11–15), although researchers may make allowance for the noise involved when small numbers of each variant are present in a small population, such as in transposon-mutant screens (13). Although little is known about the actual $N_e$ of bacterial populations within individual hosts, it is possible that $N_e$ is smaller than the census population because of the observed subpopulation
structure (16), which may lead to heterogeneity in the reproductive potential of members of the population. We therefore hypothesize that limited effective population sizes contribute to the variability of competition outcome when the sizes are small enough to make even a fully neutral marker drift significantly.

Streptococcus pneumoniae (pneumococcus) is an important pathogen that frequently colonizes the human nasopharynx. Although nasopharyngeal colonization is usually asymptomatic, it is a critical step prior to invasive infections (17, 18). The nasopharyngeal carriage population serves as a reservoir of bacteria that may be transmitted to other hosts. In humans, an average carrier harbors at least 10^7 to 10^8 pneumococci (19), and the duration of colonization ranges from 1 week to several months (19). More importantly, most transmission of pneumococci occurs from healthy carriers, making the nasopharyngeal colonization a key stage in the evolution and ecology of these organisms. The effect of selection pressures imposed by host immunity, competition with other microflora, and antimicrobial treatment will depend on the effective population size. This is both because a small Ne limits the amount of genetic variation (i.e., mutations and recombination events) available for selection and because, in simple population-genetic models, selection can be effective only if the product of the selection coefficient and Ne is substantially greater than 1; otherwise, selection will typically be overwhelmed by genetic drift. An understanding of within host Ne would be valuable in understanding the population dynamics of pneumococcus in vivo.

We assessed here how much stochastic effects influence the outcome of animal experiments by measuring the Ne of pneumococcus in a mouse colonization model and modeling its effects on within-host selection. We found that Ne was substantially smaller than the carriage population size. It appeared that Ne did not change over time during colonization. Simulation studies suggested that such a small Ne could reduce the efficiency of within-host selection for favored variants.

MATERIALS AND METHODS

Strains and animals. The OVA and AVO stains were serotype 6B pneumococcal strain 603 derivatives that were described previously (3). Briefly, these were derivatives of clinical strain 603 with either OVA323-339 peptide (ISQAVHAAHAEINEAGR) fused with two pneumococcal proteins: pneumococcal surface protein A (PspA) and pneumolysin (Ply). Wild-type BALB/c (BALB/c) mice and BALB/c DO11.10 RAG\(^{-/-}\) (DO11.10) mice were obtained from the Jackson ImmunoResearch Laboratories, Bar Harbor, ME. All mice were female, 9 to 10 weeks old at the start of experiments, and kept in a BL2 facility. Some mice were intranasally administered 1 μl of phosphate-buffered saline containing approximately 5 x 10^8 CFU of each strain. Nasal wash samples were collected up to 8 days after challenge according to a method described previously (3). Aliquots of each sample were titered to determine the CFU density in sample. The remaining samples were cultured overnight on blood agar plates supplemented with gentamicin to a final concentration of 2.5 mg/liter, and all bacterial growth was harvested for genomic DNA extraction.

Genomic DNA was purified from cultures of samples collected from animals using a DNeasy blood and tissue kit (Qiagen, Valencia, CA). OVA strain- and AVO strain-specific primer sets were designed based on the nucleotide sequence difference in the psaA locus between the two strains. The quantity of strain-specific genomic DNA in a sample was determined by real-time PCR as described previously (3). The AVO/OVA ratio for each sample was calculated by using the absolute amount of OVA DNA and AVO DNA in the sample. The CFU counts for AVO and OVA bacteria in a sample were estimated from the total CFU and the AVO/OVA ratio (Table 1).

Bacterial growth curve. AVO and OVA strains were streaked onto blood agar plates and cultured at 37°C in a 5% CO\(_2\) overnight. Four colonies from each strain were subcultured in Todd-Hewitt medium with 0.5% yeast extract (THY; Becton Dickinson, Sparks, MD) until the optical density at 620 nm (OD\(_{620}\)) reached ~0.4 and then diluted into THY medium at a starting culture OD\(_{620}\) of ~0.005. Growth was monitored in sterile flat-bottom 96-well microtiter plates (Nunc, Denmark) containing 200 μl of culture in each well every 30 min using a VERSAmax microplate reader (Molecular Devices, Sunnyvale, CA) over 6 h. The growth curves were fitted to an exponential growth equation, and the doubling time was estimated using Prism software (GraphPad Software, Inc., La Jolla, CA).

Estimation of variance effective population (Ne). MLNE software (20, 21) was used to estimate the maximum-likelihood Ne and its 95% confidence interval (CI). Essentially, the software uses the probability of observing the CFU count data (Table 1) in a sample at a given time as a function of the CFU count data in a previous sample, the number of generations during the sampling period, and the (harmonic) mean effective size (N\(_e\)) of the population (22). The estimation procedure in MLNE function further accounted for the probability of observing the CFU count data in a sample given a true ratio between the two strains in the underlying population and thus explicitly accounted for sampling error caused by examining the allelic composition of a finite number of bacterial CFU. When the CFU count data in all time points are given, the software will maximize the likelihood of the data by varying the Ne. We assumed that Ne was the same for each mouse, and the frequency of AVO and OVA bacteria in different mice at each time point in a single experiment could be treated as if they were alleles at independently assorting loci. The likelihood maximized by the software in this way corresponds to

<table>
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<tr>
<th>Mouse</th>
<th>CFU count</th>
</tr>
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<tbody>
<tr>
<td></td>
<td>Day 1</td>
</tr>
<tr>
<td>AVO/ OVA</td>
<td></td>
</tr>
<tr>
<td>1-1</td>
<td>1,510</td>
</tr>
<tr>
<td>1-2</td>
<td>8</td>
</tr>
<tr>
<td>1-3</td>
<td>200</td>
</tr>
<tr>
<td>1-4</td>
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</tr>
<tr>
<td>2-3</td>
<td>22</td>
</tr>
<tr>
<td>3-1</td>
<td>57</td>
</tr>
<tr>
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<tr>
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<td>283</td>
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<tr>
<td>4-1</td>
<td>31</td>
</tr>
<tr>
<td>4-2</td>
<td>848</td>
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<tr>
<td>4-3</td>
<td>1,775</td>
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<tr>
<td>4-4</td>
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<table>
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<th>Day 4</th>
<th>Day 8</th>
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<td>1,510</td>
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<td>4,413</td>
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<td>1,775</td>
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<td>247</td>
</tr>
<tr>
<td>4-4</td>
<td>95</td>
<td>197</td>
<td>7</td>
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the assumption that \( N_e \) was the same in each mouse, so each mouse contributes independent data to the estimation of that single quantity. To estimate the pneumococcal \( N_e \) during colonization in BALB/c mice, the CFU count data on days 1, 4, and 8 were used. To estimate the average pneumococcal \( N_e \) during colonization in DO11.10 RAG\(^{-/-}\) mice, the CFU count data on days 1, 3, and 7 were used. Allele frequency change from the time of inoculation (day 0) to day 1 was not considered in \( N_e \) estimation to minimize the effect of colonization bottleneck. Any mouse with missing data on any of the three sampling time points was also excluded from analysis. The input data for MLNE were prepared according to software instructions with each mouse replicate being treated as an independent locus. The number of pneumococcal generations between two sampling time points was calculated by dividing the length of time between two samplings by the average life span of pneumococcus. We used (cells doubling time)/ln(2) as the average life span according to a simple exponential-growth/exponential-death model at its equilibrium. Due to the haploidy of pneumococcal genome, the \( N_e \) and 95% CI estimated by the MLNE software (designed for diploids) were scaled up by a factor of 2 (Jinliang Wang, unpublished data), a scaling that we validated by preliminary simulation (data not shown).

**Simulation of pneumococcal colonization population.** A simple model of heterogeneity in bacterial reproduction that could generate a small effective population size is one similar to that described by Balaban et al. (23) for “type 1 persisters.” This model represents the pneumococcal colonization population as composed of two subpopulations, \( P_1 \) and \( P_2 \). \( P_1 \) is a small subpopulation that actively replicates, while \( P_2 \) represents a large subpopulation where most bacterial death/removal occurs. Each subpopulation is composed of two strains, \( A \) and \( O \), that satisfy \( P_1 = A_1 + O_1 \) and \( P_2 = A_2 + O_2 \). The dynamics of \( A_1, O_1, A_2, \) and \( O_2 \) is described by equations 1 to 4:

\[
\frac{dA_1}{dt} = \mu A_1 - \frac{\mu A_1 (A_1 + O_1)}{K_1} - d_A A_1
\]

(1)

\[
\frac{dO_1}{dt} = \mu O_1 - \frac{\mu O_1 (A_1 + O_1)}{K_1} - d_O O_1
\]

(2)

\[
\frac{dA_2}{dt} = \frac{\mu A_2 (A_1 + O_1)}{K_1} + \mu A_2 \left( 1 - \frac{A_2 + O_2}{K_2} \right) - d_A A_2
\]

(3)

\[
\frac{dO_2}{dt} = \frac{\mu O_2 (A_1 + O_1)}{K_1} + \mu O_2 \left( 1 - \frac{A_2 + O_2}{K_2} \right) - d_O O_2
\]

(4)

For competitively neutral strains to achieve stable carriage, we assumed that \( d_A = d_O = d \) and that \( \mu > d \). Essentially, strains in \( P_1 \) follow exponential growth and clearance, with the probability of the descendant cell’s remaining in \( P_1 \) decreasing with the number of cells in \( P_1 \); otherwise, it migrates to \( P_2 \) (equations 5 and 6), with the migration modeled as a separate event. Strains in \( P_2 \) grow logistically and are also subjected to exponential clearance.

\[
\frac{dP_1}{dt} = \mu P_1 - \frac{\mu P_1^2}{K_1} - d_P P_1
\]

(5)

\[
\frac{dP_2}{dt} = \frac{\mu P_2^2}{K_1} + \mu P_2 \left( 1 - \frac{P_2}{K_2} \right) - d_P P_2
\]

(6)

Equation 5 combines equations 1 and 2; equation 6 combines equations 3 and 4. The stable equilibrium subpopulation size of \( P_1 \) and \( P_2 \) is given by:

\[
P_1^* = A_1^* + O_1^* = \frac{\mu - d}{\mu} K_1
\]

(7)

\[
P_2^* = A_2^* + O_2^* = \frac{(\mu - d)(1 + \sqrt{1 + 4\mu K_2})}{2\mu}
\]

(8)

Note that when growth is blocked (\( \mu = 0 \)), the total population (\( P_1 + P_2 \)) follows an exponential decay: \( dP_1 + P_2/dt = -d(P_1 + P_2) \). In this situation, the half-life (\( \ln(2)/d \)) of pneumococcus during mouse nasal colonization has been estimated to be 161 min (13). Unless otherwise specified, the clearance rate \( d = 0.0043 \min^{-1} \) (\( \ln(2)/161 \min^{-1} \)) and the maximum growth rate \( \mu = 0.0231 \min^{-1} \) were used. Varied \( K_1 \) and \( K_2 \) values were used as indicated.

Our simulation was a stochastic version of the model described by equations 1 to 4. To generate simulation data of allele frequency, we used the “ssa.adaptivetau” package in R (24), which implements an adaptive tau leaping to approximate the trajectory of a continuous-time stochastic process. The instantaneous transition rate for each transition and its effects are given in Table 2.

**Table 2** Transition rates for simulation of the colonization population

<table>
<thead>
<tr>
<th>Event</th>
<th>Effects ((A_1, O_1, A_2, O_2))</th>
<th>Transition rate (0)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Birth</td>
<td>(A_1) 1, 0, 0, 0</td>
<td>(\mu A_1)</td>
</tr>
<tr>
<td></td>
<td>(O_1) 0, 1, 0, 0</td>
<td>(\mu O_1)</td>
</tr>
<tr>
<td>Migration</td>
<td>(A_1) -1, 0, 1, 0</td>
<td>(\mu A_1 (A_1 + O_1)/K_1)</td>
</tr>
<tr>
<td></td>
<td>(O_1) 0, -1, 0, 1</td>
<td>(\mu O_1 (A_1 + O_1)/K_1)</td>
</tr>
<tr>
<td>Clearance</td>
<td>(A_1) -1, 0, 0, 0</td>
<td>(d_A A_1)</td>
</tr>
<tr>
<td></td>
<td>(O_1) 0, 1, 0, 0</td>
<td>(d_O O_1)</td>
</tr>
<tr>
<td>Birth</td>
<td>(A_2) 0, 0, 1, 0</td>
<td>(\max[0, \mu A_2 [1 - (A_2 + O_2)/K_2]])</td>
</tr>
<tr>
<td></td>
<td>(O_2) 0, 0, 0, 1</td>
<td>(\max[0, \mu O_2 [1 - (A_2 + O_2)/K_2]])</td>
</tr>
<tr>
<td>Death</td>
<td>(A_2) 0, 0, -1, 0</td>
<td>(-\min[0, \mu A_2 [1 - (A_2 + O_2)/K_2]])</td>
</tr>
<tr>
<td></td>
<td>(O_2) 0, 0, 0, -1</td>
<td>(-\min[0, \mu O_2 [1 - (A_2 + O_2)/K_2]])</td>
</tr>
</tbody>
</table>

*Max, function that returns the largest value of the input values; min, function that returns the smallest value of the input values.

To initialize the simulation, \( A_1 + O_1 \) and \( A_2 + O_2 \) were first set to their equilibrium size (\( P_1^* \) and \( P_2^* \)) in equations 7 and 8, respectively. To mimic the allele frequency distribution on day 1 of colonization, a value of \( \log_{10}(a) \) was randomly drawn from a normal distribution estimated from the BALB/c colonization experiment (equation 9), where \( a \) is the ratio between the two strains in each subpopulation (\( a = A_1/O_1 = 1.2 \)). The specific initial state \((A_1, O_1, A_2, O_2)\) was then calculated according to the value of \( a \) and equations 10 to 13.

\[
\log_{10} a \sim N(0, 0.23^2)
\]

(9)

On day 1:

\[
A_1 = P_1^* \frac{a}{1 + a}
\]

(10)

\[
O_1 = P_1^* \frac{1}{1 + a}
\]

(11)

\[
A_2 = P_2^* \frac{a}{1 - a}
\]

(12)

\[
O_2 = P_2^* \frac{1}{1 - a}
\]

(13)

After initialization, the model was first simulated forward for \( t = 4,320 \min \) (3 days) by using the “ssa.adaptivetau” function in the “adaptivetau” R package (24). The values of \( A_1, O_1, A_2, \) and \( O_2 \) at the end of the \( t = 4,320 \min \) were recorded as the day 4 output. Continuing from this state, the model
was subsequently simulated forward for another 5,760 min (4 days), and the end values of \(A_1, O_1, A_2,\) and \(O_2\) were recorded as the day 8 output.

The \(N_e\) of the simulated population was estimated by the MLNE software using a method similar to what is described in this previous section. Briefly, the values of \(A_1\) and \(O_1\) on days 1, 4, and 8 of simulation were used as allele count data in the input file of the MLNE software. Twenty replicate simulations were performed for any given set of parameters (\(\mu, d, K_1,\) and \(K_2\)). The values of \(A_1\) or \(O_1\) on days 1, 4, and 8 in each replicate simulation were used as allele counts from an independent locus in the input file of the MLNE software. As for the experimental data, the \(N_e\) and 95% CI estimated by the MLNE software were scaled up by a factor of 2. To estimate the \(N_e\) of the simulated population between days 1 and 4, the pneumococcal colonization model was modified to incorporate selection were used to estimate the \(N_e\) of the simulated population between days 4 and 8.

**Simulation of within-host selection in the colonizing population.**

To examine the influence of \(N_e\) on the efficiency of within host selection, the pneumococcal colonization model was modified to incorporate selection mediated by different clearance rates for a wild-type strain (O) and a mutant strain (A) (i.e., \(d_A \neq d_O\)); otherwise, the equations are the same as equations 1 to 4 and Table 2. The parameters used in the simulation were \(\mu = 0.0231 \text{ min}^{-1}, d_A = 0.0043 \text{ min}^{-1}, K_1 = 400,\) and \(K_2 = 40,000,\) which corresponded to an estimated \(N_e\) of 181 according to previous simulations. Varied \(d_A\) values were used as indicated.

To initialize the simulation, \(A_1 + O_1, A_2 + O_2\) were first set to the carrying capacities (400 and 40,000, respectively). The specific values of \(A_1, O_1, A_2,\) and \(O_2\) were then set to satisfy that \(A_1/O_1 = A_2/O_2 = a,\) where \(a\) is a given initial ratio between mutant and wild-type alleles. After initiation, the model was first simulated forward for \(t = 5,760\) min (4 days). The value of \(A_1, O_1, A_2,\) and \(O_2\) at the end of the \(t = 5,760\) min was recorded as the day 4 output. Continuing from this state, the model was subsequently simulated forward for another 5,760 min (4 days), and the end value of \(A_1, O_1, A_2,\) and \(O_2\) was recorded as the day 8 output. The \(A_1\) and \(O_2\) outputs on days 4 and 8 of simulation were used to calculate the mutant allele frequency \([A_1/(A_1 + O_1)]\). Twenty replicate simulations were performed. The average census population size \((A_1 + O_1)\) during the simulation was approximately 33,000.

**Simulation of within-host selection by an ideal population model.**

The ideal population is a single population with a wild-type strain (O) and a mutant strain (A) undergoing selection mediated by different clearance rates (equations 14 and 15). The parameters used in simulation were \(\mu = 0.0231 \text{ min}^{-1}, d_A = 0.0043 \text{ min}^{-1},\) and \(K = 40,000.\) Varied \(d_A\) values were used as indicated.

The following equations express the ideal population model:

\[
\frac{dA}{dt} = \mu A \left(1 - \frac{A + O}{K}\right) - d_A A
\]

\[
\frac{dO}{dt} = \mu O \left(1 - \frac{A + O}{K}\right) - d_O O
\]

Simulation data of allele frequency were generated by using the "adaptive" package in R (24), and the instantaneous transition rates are listed in Table 3. To initialize the simulation, \(A + O\) was first set to the carrying capacity (400). The specific values of \(A\) and \(O\) were then set to satisfy that \(A/O = a,\) where \(a\) is a given initial ratio between mutant and wild-type alleles. After initiation, the model was first simulated forward for \(t = 5,760\) min (4 days). The value of \(A\) or \(O\) at the end of the \(t = 5,760\) min was recorded as the day 4 output. Continuing from this state, the model was subsequently simulated forward for another 5,760 min (4 days) and the end value of \(A\) or \(O\) was recorded as the day 8 output. The \(A\) and \(O\) outputs on days 4 and 8 of simulation were used to calculate the mutant allele frequency \([A/(A + O)]\). Twenty replicate simulations were performed. The average census population size \((A + O)\) during simulation was approximately 32,000.

**RESULTS**

Pneumococcal variants showed genetic drift during nasal colonization. To investigate the effective population size of pneumococcus during nasal carriage, we used two competitively neutral strains, the AVO strain and the OVA strain, which have been described previously (3). The two strains showed similar in vitro growth rates in THY medium (Fig. 1A). The average doubling time of the AVO strain (62 min, 95% CI = 55 to 70) was not significantly different from that of the OVA strain (65 min, 95% CI = 57 to 76) (Fig. 1A, Student t test, \(P = 0.82\)).

To quantify genetic drift in vivo, 20 BALB/c mice were intranasally challenged by a 1:1 mixture of the AVO and OVA strains. We measured the total CFU and the AVO/OVA ratio in the nasal washes as described in Materials and Methods. The mean \(\log_{10}(\text{AVO/OVA})\) values were 0.067 (\(n = 20,\) standard deviation [SD] = 0.23), 0.014 (\(n = 16,\) SD = 0.76), and 0.070 (\(n = 19,\) SD = 1.04) on days 1, 4, and 8, respectively (Fig. 1B). None of the mean \(\log_{10}(\text{AVO/OVA})\) values were significantly different from the input \(\log_{10}(\text{AVO/OVA})\) (\(P > 0.05,\) one sample t test). In contrast, the variance of \(\log_{10}(\text{AVO/OVA})\) showed a significant increase over time (Fig. 1B, Levene’s test for equal variance, \(P = 0.034\)). Furthermore, no significant correlation between change in AVO/OVA from day 0 to day 1 and change from day 4 to day 8 was observed (Fig. 1C, \(n = 16,\) rho = 0.20, \(P = 0.45\)). In similar colonization experiments carried out in BALB/c mice exposed to immunization adjuvant (cholera toxin) 4 weeks prior to challenge, no correlation between change in AVO/OVA from day 0 to day 1 and change from day 4 to day 8 was observed either (Fig. 1D, \(n = 9,\) rho = -0.38, \(P = 0.31\)). The lack of consistent AVO/OVA ratio change in an individual mouse argued against selection for heritable fitness differences acquired by a subpopulation of one of the strains during nasal colonization.

**Estimation of effective population size.** Based on the temporal change of AVO strain frequency in each mouse, we estimated \(N_e\) by using the MLNE software (25), which implements a maximum-likelihood method and accounts for sampling error. An in vivo doubling time of 161 min (13) was assumed to estimate the number of generations between two sampling points. In BALB/c mice, the effective population of pneumococcus showed a point estimate of 133 with 95% CI of 11 to 203 (Fig. 2A). In comparison, the CFU recovered on day 8 showed a mean of 5,768 with a 95% CI of 57 to 76.
confidenve interval of 2,515 to 9,021 (Fig. 2A). Since CFU recovered on day 8 represents only a fraction of the carriage population, we concluded that the Ne of pneumococcus is much smaller than the carriage population during nasal colonization.

A number of in vitro studies indicated that the doubling time of pneumococcus could be much shorter than 161 min (13, 26). We therefore tested whether a shorter generation time could explain the discrepancy between carriage population and effective popu-

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FIG 1 AVO and OVA are neutral alleles and show genetic drift during nasal carriage. (A) The AVO and OVA strains were cultured in THY medium at 37°C, and the increase in OD_{620} was measured every 30 min. The curve was fitted to an exponential growth to estimate the average doubling time. (B) Twenty BALB/c mice were intranasally challenged by a 1:1 mixture of the AVO and OVA strains (day 0). The AVO/OVA ratio in mouse nasal wash was measured on days 1, 4, and 8. Each dashed line connects points for the same mouse over time. (C) Scatter plots to examine correlation between the change in AVO/OVA from day 0 to day 1 and the change in AVO/OVA from day 4 to day 8 in BALB/c mice. (D) Scatter plots to examine correlation between the change in AVO/OVA from day 0 to day 1 and the change in AVO/OVA from day 4 to day 8 in BALB/c mice who had been treated with cholera toxin (CT) 4 weeks prior to challenge.

FIG 2 Effective population of pneumococcus in BALB/c mice. (A) The estimated Ne in BALB/c mice (□) was lower than the CFU recovered on day 8 (■). (B) A range of in vivo generation time was assumed, and the estimated Ne values (left panel) were compared to the CFU recovered on day 8 (right panel). (C) The Ne for different time intervals was estimated by only using the strain frequency data during the time period specified. Error bars represent the 95% CI.
luation. A range of generation times was assumed and the corresponding effective population size was calculated (Fig. 2B). As expected, effective population size increased when generation time became shorter (Fig. 2B). However, the effective population size was still substantially smaller than the CFU recovered even an unrealistically short generation time (20 min) was assumed (Fig. 2B). Thus, a short generation time in vivo was unlikely to be the major explanation for the small N_e.

We next examined whether there is temporal change in pneumococcal N_e during colonization. The average N_e from day 1 to day 4 (days 1 to 4) was calculated by using the AVO allele frequency change between day 1 and day 4. The same strategy was used to estimate average N_e during days 4 to 8. As shown in Fig. 2C, the estimation of N_e for days 1 to 4 (point estimate, 132; 95% CI = 7 to 250) was very similar to the estimation of N_e for days 4 to 8 (point estimate, 132; 95% CI = 11 to 250). The N_e estimated for the two time intervals were much lower than the CFU recovered on day 8, a finding consistent with the overall N_e.

Finally, the effective population size of pneumococcus during nasal carriage in varied experimental conditions, as well as in a different mouse type, was investigated. Cholera toxin (CT) is a commonly used adjuvant in immunization experiments, and here we examined its effect on N_e in BALB/c mice. In BALB/c mice exposed to CT (BALB/c + CT), the effective population of pneumococcus showed point estimate of 64 (95% CI = 6 to 65) (Fig. 3A, n = 8). Similar to what was observed in naive BALB/c mice, the N_e was substantially smaller than the CFU recovered on day 8 (mean, 14,641; 95% CI = 3,620 to 25,655) (Fig. 3A). The estimation of N_e for days 1 to 4 (point estimate, 62; 95% CI = 3 to 111) was similar to the estimation of N_e for days 4 to 8 (point estimate, 69; 95% CI = 4 to 75) (Fig. 3B). It appeared that exposure to CT reduced pneumococcal N_e in BALB/c mice.

In DO11.10 RAG^-/- mice (which lack adaptive B cell and T cell immunity, except for CD4^+ T cells specific for a peptide of ovalbumin) exposed to CT (DO11.10 + CT), the effective population of pneumococcus showed point estimate of 87 (95% CI = 7 to 181) (Fig. 3C, n = 7). Again, the N_e was much smaller than the CFU recovered on day 8 (mean, 9,931; 95% CI = 4,155 to 15,708) (Fig. 3C). The estimation of N_e for days 1 to 3 (point estimate, 86; 95% CI = 5 to 245) was similar to the estimation of N_e for days 3 to 7 (point estimate, 87; 95% CI = 7 to 206) (Fig. 3D). Thus, the N_e of pneumococcus in DO11.10 RAG^-/- mice showed qualitatively similar patterns as in BALB/c mice.

A mathematical model reproduced the N_e patterns. The large discrepancy between N_e and carriage census population size would be most readily explained by heterogeneity in pneumococcal replication during nasopharyngeal colonization. Indeed, the nasal mucosa may support two populations of pneumococci, which can be primarily recovered from the outer surface and the nasal tissue, respectively (16). To examine whether the heterogeneous nasal environment can explain the observed N_e patterns, we modeled pneumococcal colonization by considering two subpopulations, P_1 and P_2, that are established 1 day after inoculation (Fig. 4A). Loosely based on the idea of the type I persisters described by Balaban et al. (23), we hypothesized that a small subpopulation of pneumococci (P_1), perhaps tissue associated (16), actively replicates, while a larger population that is in the nasopharyngeal lumen or mucosal surface (P_2) may or may not replicate but does not contribute to the future generations which are seeded by the P_1 population. Effectively, P_2 is the major site of bacterial death and removal. Note that this is a deliberate simplification, in the absence of detailed information concerning the heterogeneity in dynamics of the colonizing population over time.

We simulated this model, tracking OVA and AVO strains sep-


**Mathematical model of pneumococcal colonization dynamics.** (A) Differential equations describing the dynamics of two strains (A and O) in two subpopulations, \( P_1 \) and \( P_2 \). A stochastic version of this model was used in simulation. To initialize the simulation, \( P_1 \) and \( P_2 \) were set to their equilibrium size (\( P_1^* \) and \( P_2^* \), respectively), and the ratio between the two strains in each subpopulation was set to follow a log-normal distribution as estimated from the day 1 results of the BALB/c colonization experiment. After initiation, the model was simulated forward for a total of \( t = 10,080 \) min (7 days), and the counts of the two strains in each subpopulation on days 1, 4, and 8 were recorded as output. (B) Typical results from 20 simulations with the indicated parameter values. The log\(_{10}\) \((A_1/O_1)\) calculated from the simulation output is shown, and each dashed line connects data points from the same simulation. (C) Simulation of the model produced small \( N_e \) despite large census population size. The point estimate of \( N_e \) calculated from output of 20 simulations shown in panel B is shown, which is substantially smaller than the census population size \( P_1^* \) used in the simulation. Error bars indicate the 95\% CI. (D) Simulation of the model showed little temporal change in \( N_e \). \( N_e \) was calculated from output of 20 simulations shown in panel B and the \( N_e \) in different time intervals was estimated by only using the strain frequency data during the time period specified. Error bars indicate the 95\% CI. (E) Effects of \( P_1^* \) and \( P_2^* \) size on the estimated \( N_e \). Simulation was performed with varying \( K_1 \) and \( K_2 \) values such that the indicated \( P_1^* \) and \( P_2^* \) sizes were achieved. Twenty simulations were performed for each combination of \( P_1^* \) and \( P_2^* \), and the point estimate of \( N_e \) based on that 20 simulation output is shown. The shaded area represents where the simulated \( N_e \) values fall within the 95\% CI of \( N_e \) estimated from the BALB/c colonization experiment, and the census population size used in the simulation (\( P_2^* \)) is no smaller than the census population size observed in the BALB/c colonization experiment (95\% CI of mean CFU recovered, open bar).

Facilitated by the pneumococcal colonization model, we further investigated the pattern of allele frequency change in the colonizing population when the clearance rate of the A strain bacteria is different from that of the O strain bacteria, as might be the case of under selection for escape from strain-specific immune responses or antimicrobial agents. The results were compared to those from an ideal population in which the census size and effective size are nearly equal (Fig. 5). In both populations, the census size was approximately 30,000 during simulation. Selection would be expected to operate efficiently down to a selection coefficient of order \( \sim 10^{-4} \) if the effective population size were equal to the observed census size. The colonizing population was parameterized such that \( N_e = 183 \), a finding consistent with \( N_e \) estimated in the BALB/c mice. The initial mutant allele frequency was set as 0.5 (1:1 ratio to the wild-type allele), and the mutant allele frequency was monitored for up to 8 days. Clearance rate ratios ranging from 0.952 to 1.053 were used for both the colonizing population and the ideal population. The simulation results indicated that selection was less efficient in the colonizing population than in the ideal population (Fig. 5). For example, when the clearance rate of the
mutant allele was 0.990 that of the wild-type allele, mutant allele frequency increased above 0.5 in 13/20 simulations by day 4 in the colonizing population (Fig. 5A), while the mutant allele frequency increased above 0.5 in 20/20 simulations in the ideal population during the same period (Fig. 5C). By day 8, the mutant allele frequency showed a highly significant increase in the ideal population (mean increase $0.1274$, $n = 20$, $P = 0.0001$, one sample t test) (Fig. 5D). In the colonizing population, by contrast, the increase in mutant allele frequency was not statistically significant by day 8 (mean increase $0.038$, $n = 20$, $P = 0.57$, one sample Student t test) (Fig. 5B). Similar results were observed when the initial mutant allele frequency was set as 0.01 (see Fig. S1 in the supplemental material).

DISCUSSION
In this study, we estimated the effective population size of Streptococcus pneumoniae in a mouse colonization model by following the frequency change of two cocolonizing, competitively neutral pneumococcal strains. Since only allele frequency data on or after day 1 were used in $N_e$ estimation, the effect of colonization bottleneck on frequency changes was minimized. In two mouse types, the $N_e$ during nasal carriage was much smaller than the lower bound of census population that is estimated by the number of CFU recovered. The number of CFU recovered in the present study was smaller than the colonization density reported in other studies (9, 27–29), because at no time point did we intend to remove and recover the whole colonizing population. We purposely retrieved only a small fraction of the total population during live sampling in order to keep the colonization minimally disturbed. Even at the terminal sample, we did not exhaustively wash the mouse’s upper respiratory tract but rather used a fixed recovery volume of 200 $\mu$L. Pneumococcal $N_e$ also showed little temporal variation during colonization. We hypothesized that such a small $N_e$ may reduce the effectiveness of within host selection for pneumococcus.

We constructed a mathematical model of colonization by considering two subpopulations of different growth dynamics that are established after a colonization bottleneck. In this model, a small, fast-replicating subpopulation generates most of the stochastic deviation in allele frequency that is then passed to a large subpopulation that is readily sampled but is not contributing much toward future generations. The model represents one, though not the only, biologically plausible mechanism that could generate such small effective population size. By simulation, we showed that this model could reproduce $N_e$ patterns that were consistent with what was observed in mice experiments over a wide range of parameter values. A small $N_e$ could be consistent with either a large or a small census population size (Fig. 4D), depending on the relative size of the two subpopulations. Thus, subpopulation structure, rather than the total population size, could be a critical determinant of $N_e$ during pneumococcal colonization.

Using stochastic simulation of the model, we also examined the effectiveness of within-host selection for a mutant allele. Compared to an ideal population, the colonizing population showed two features: (i) the increase in frequency of a favorable allele was more variable and (ii) a favorable allele was less likely to become...
fixed. These observations were consistent with strong genetic drift effects that interfered with the effectiveness of selection. In future investigations, it would be interesting to simultaneously estimate \( N_e \) and in vivo selection coefficient by using strains with medium and large fitness effects in competition experiments.

Our model certainly is not the only model that could produce the degree of stochastic variation observed. It is possible, for example, that there are more than two subpopulations with different contributions to successive generations. Alternatively, it is possible that the neutrally marked strains introduced in the experiment go on to mutate, and that some of these mutations (which occur at random with respect to the neutral marker) are advantageous in certain microanatomic sites within the nasopharynx. The consistency of results across experiments and the lack of positive correlation between frequency changes of neutral markers within a mouse over time make this selective explanation less likely. In any case, many models, including heterogeneous contributions to future generations or the presence of different selective microenvironments, which would produce random variation in neutral marker frequency as observed in our experiments, would also interfere with the action of selection to increase the frequency of, for example, a drug resistance mutation. It is for this reason that the concept of effective population size has been useful despite uncertainty about the precise mechanisms determining its value (10).

Studies of within-host competition between bacteria rarely comment on the aspects of stochasticity introduced by population bottlenecks and by a small effective population size. There are exceptions: transposon mutagenesis studies usually account for bottlenecks and by a small effective population size. There are comment on the aspects of stochasticity introduced by population (

The effect of small \( N_e \) is not limited to pneumococcal colonization. In a chicken model of colonization by Campylobacter, it was reported that the proportion of wild-type isogenic tagged strains present in chicken ceca after oral infection with a mixed population is not predictable from the inoculum (30). The unre-
dictability could be a result of both colonization bottleneck and a small \( N_e \) that increased the variability of the observed proportion. In addition, Grant et al. probed microbial population dynamics in vivo by simultaneously administering wild-type isogenic tagged strains of Salmonella enterica (33). By tracing the disappearance of strains through time, it was shown that independent bacterial subpopulations are established in different organs and that different bacterial populations mix between organs via the blood. Such population heterogeneity in vivo may also cause the effective pop-
ulation size of Salmonella enterica to be much smaller than the census population size and thus may influence the effectiveness of selection. Since the isogenic tagged strains allow tracking frequency change of multiple alleles simultaneously, data generated by this approach would be very informative to estimate the \( N_e \) of Salmonella enterica in vivo.

A small \( N_e \) could also affect the generation of new alleles. The probability that a neutral mutation occurs at a given position in an individual bacterium that is destined to contribute to future genera-

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