Linear Stability and Instability Patterns in Ion-Sputtered Silicon

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Accessibility
Linear Stability and Instability Patterns in Ion-Sputtered Silicon

Charbel S. Madi, H. Bola George, and Michael J. Aziz

Harvard School of Engineering and Applied Sciences, Cambridge MA 02138

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We study the patterns formed on Ar$^+$ ion sputtered Si surfaces at room temperature as a function of the control parameters ion energy and incidence angle. We observe the sensitivity of pattern formation to artifacts such as surface contamination and report the procedures we developed to control them. We identify regions in control parameters space where holes, parallel mode ripples and perpendicular mode ripples form, and identify a region where the flat surface is stable. In the vicinity of the boundaries between the stable and pattern forming regions, called bifurcations, we follow the time dependence from exponential amplification to saturation and examine the amplification rate and the wavelength in the exponential amplification regime. The resulting power laws are consistent with the theory of nonequilibrium pattern formation for a Type I (constant-wavelength) bifurcation at low angles and for a Type II (diverging wavelength) bifurcation at high angles. We discuss the failure of all sputter rippling models to adequately describe these aspects of the simplest experimental system studied, consisting of an elemental, isotropic amorphous surface in the simplest evolution regime of linear stability.
I. INTRODUCTION

Uniform ion beam sputter erosion often causes a spontaneously-arising pattern of corrugations, holes or dots [1]. Periodic self-organized patterns with spacing as small as 7 nm [2] have stimulated interest in this method as a means of sub-lithographic nanofabrication [3]. We are studying spontaneous pattern formation in uniform noble-ion irradiation of silicon. Due to its simplicity, this system is a very promising one for using experiment as a rigorous test of theory: it is a monatomic system amenable to molecular dynamics (MD) simulation and its surfaces are amorphous under ion bombardment, thereby minimizing potentially confounding effects of disproportionation and crystallographic singularities. If theory and experiment cannot agree in such a prototypical simple system as this, where can they possibly agree? And if we can't make them agree even in the linear regime of exponential amplification, how much confidence can we have in the results of explorations of patterns evolving from nonlinear terms as they are added to the wrong linear partial differential equation (PDE)?

In the linear stability theory of Bradley and Harper [4] (BH) the pattern originates from different wavenumber dependences of the destabilizing (roughening) effect in which the erosion rate is enhanced at regions of high concave curvature, and the stabilizing (smoothening) effect of surface diffusion. Whereas BH theory explains several experimental observations, significant contradictions are evident. Several of these are attributable [1] to crystallographic effects missing from BH, but the most serious ones are those occurring on amorphous surfaces, for which BH was designed. One particularly important prediction of BH is that a flat surface is unstable to perpendicular mode ripples (wave vector perpendicular to ion beam) under uniform ion irradiation at any incidence angle. Another is that the dominant instability undergoes a "ripple rotation" from parallel mode (wave vector parallel to the projected ion beam) near normal incidence to
perpendicular mode near grazing incidence. The trend that emerges from a number of studies on amorphous surfaces such as quartz glass [5] and room-temperature silicon [6-9] is ripple rotation at high angles (which is qualitatively consistent with BH) but a transition to a stable flat surface at low or intermediate angles (which is inconsistent with BH). It is possible that because the sputter yield is highest near the angles where ripple rotation is observed, the erosive component (perhaps adequately modeled by the Gaussian ellipsoids in BH, discussed below) of the surface response dominates over the component from local mass redistribution [6,10,11]. In making this comparison with experiment, two caveats should be kept in mind. First, these experimental studies are often of saturated structures after high fluence, and their relation to the dominant linear instability is not always clear. And second, the difficulty of concluding that a flat surface enjoys stability is that care must be taken to distinguish experimentally between truly stable flat surfaces and surfaces that are undergoing amplification of an instability at rates too low to be measured.

In this work we concern ourselves with the prediction of BH that a flat, uniformly irradiated surface is always unstable, and compare it to experimental ranges of two control parameters -- incident angles $\theta$ and ion beam energies $E$ -- where the surface is stable. We take care to identify and confine our attention to the "linear regime" of exponential amplification at early time and low fluence. Sharp boundaries between stable and unstable regimes in control parameter space are known as bifurcations. Nonequilibrium pattern formation theory predicts that near bifurcations pattern features are universal, depending only on general characteristics of the dynamics, such as its symmetries, degree of criticality (i.e. whether the amplitude vanishes continuously or discontinuously), and whether the characteristic length scale vanishes, diverges or remains finite at bifurcation [12]. We carried out a careful characterization of patterns around bifurcation points by varying both incidence angle and ion beam energy in room temperature Si bombardment [13].
We found that this monatomic, isotropic system exhibits two different types of supercritical bifurcations as incidence angle and ion energy are varied: At low $\theta$, a bifurcation of type I, characterized by constant wavelength and, at high $\theta$, another bifurcation, of type II, characterized by diverging wavelength [12]. Supplemented by analysis of evolving patterns near and away from bifurcations, this observation leads us to conclude that no existing theory is adequate for this monatomic, isotropic system, even at early times when nonlinear terms may be neglected.

This paper is organized as follows: In Sec. II, the experimental details are discussed. The experimental results, Sec. III contain two sections. The sensitivity of pattern formation to artifacts such as metal incorporation coming from the ion gun and sample surroundings together with the procedures developed to control the surface contamination are presented in Sec. III A. In Sec. III B, we compile our results into a phase diagram of pattern vs. the control parameters $E$ and $\theta$ which is characterized by supercritical bifurcations of Type I (constant-wavelength) and Type II (diverging-wavelength). In Sec. IV, we discuss the various possible scenarios that can account for the observed empirical results. The dependence of the amplification rate and wavelength on the control parameters is consistent with the theory of pattern formation outside of equilibrium. Finally, the conclusions are presented in Sec. V.

II. EXPERIMENT

We performed argon ion ($\text{Ar}^+$) irradiation experiments on 1 cm$^2$ Si(001) square samples (p type, $1 \sim 10 \ \Omega\cdot\text{cm}$) in an ultra-high vacuum chamber (base pressure $7 \times 10^{-11}$ torr at room temperature) with the projected ion beam direction along the [110] crystallographic direction. The argon ions were generated using a 3-cm RF source with graphite accelerating grids [14]. The ion flux from the source was 0.57 mA cm$^{-2}$ in the plane perpendicular to the ion beam. The beam
divergence was roughly 4.5° and the distance to the target was approximately 15 cm. To vary the incidence angle samples were fixed, using melted indium, onto graphite wedges of various angles which were shielded everywhere from the ion beam by Si wafer shields. Thus, only silicon was exposed to the direct ion beam and contamination-induced dynamics is suppressed [15]. Energy Dispersive X-ray Spectroscopy (EDXS), X-Ray Photoelectron Spectrometry (XPS) and a Scanning Tunneling Electron Microscopy (STEM) map scan were employed to assess the surface impurity coverage of some of the Si samples after the completion of ion sputtering. The only elements that were evident were Si, O, Ar and C, and the O and C signals from the ion beam sputtered samples were indistinguishable from those from a Si wafer taken directly out of the box.

III. RESULTS

A. Effect of surface contaminants on ion sputter erosion surface morphology

During the course of these studies we noticed that pattern formation on Ar⁺ ion sputtered Si surfaces at room temperature is extremely sensitive to the experimental configuration. Important factors include the manner in which the Si samples are fixed to the substrate holder within the vacuum chamber, the grid material, and the alignment of the grids within the ion gun.

In many ion beam sources such as ours, the screen grid (the first grid traversed by the ions) determines the ultimate kinetic energy and the accelerating grid (the second grid traversed) determines the divergence of the extracted ions. Ziberi et al. [16] have reported the sensitivity of pattern formation to the voltage of the accelerating grid at constant kinetic energy. They interpret this observation as a sensitivity to beam divergence; in principle the fundamental sensitivity is presumably to the "convergence" — i.e. the distribution of incoming angles at a point on the
sample surface — which is related to, but can be different from, the divergence. We recently noticed a sensitivity to the mechanical alignment of the grid openings themselves as an apparent shift in the boundary between "holes" and "perpendicular mode ripples" in the phase diagram of Fig. 5. At 250 eV, 5° from normal incidence, 20 minutes exposure, before the graphite grids were realigned we observed holes and dots whereas after realignment we observed perpendicular mode ripples under nominally identical conditions. Consequently, in Fig. 5, for which all the data reported were taken prior to grid realignment, we have placed the boundary between holes and perpendicular mode ripples to lie at 5°, reflecting an uncertainty in boundary position associated with grid alignment. In fact, there may be no sharp boundary, but rather a continuum of morphologies between "holes" and "perpendicular mode ripples": the topographic pattern at 10° in Fig. 2(b) may be interpreted as "holes" that are stretched along the direction of the projected ion beam.

Ion bombardment of Si samples fixed in the vacuum chamber using Mo clips that are directly exposed to the ion beam resulted in an array of dots inhomogeneously distributed on the sample surface, no matter whether graphite (C) or molybdenum (Mo) grids were used. High densities of dots developed immediately adjacent to the clips forming a ripple-like structure, with a gradual transition to an isotropic distribution of dots ~1 mm from the clips, as shown in Fig. 1. In contrast, fixing the substrate to the holder using melted indium (with no indium exposed to the ion beam) and without using any clips resulted in a featureless steady-state surface under otherwise identical irradiation conditions using graphite grids. Hence, it appears likely that trace metal contamination from the Mo grids and clips is directly responsible for the dot pattern formation, which extends over the entire 1 × 1 cm² Si surface. Similar observations of the sensitivity of pattern formation to surface metal content were reported by Ozaydin et al. [15],
who used Mo clips to fix their samples and reported XPS measurements indicating Mo
concentrations of 5-15%; and by Sanchez-Garcia et al. [17], who measured by Rutherford
Backscattering Spectrometry (RBS) about 5% of Mo and Fe combined in their samples arising
from the Mo clips and the cold cathode ion source, respectively. We examined some of our
irradiated silicon surfaces for surface contamination using RBS and XPS. For a series of
specimens that were directly contacted by silicon clamps, which themselves were held down by
Mo clips, and with no direct line of sight from any of the irradiated Mo clip or graphite sample
holder material to the sample surface, RBS measurements indicated a Mo surface coverage of 1-
9 × 10^{14} \text{ cm}^{-2} on specimens irradiated using Mo grids at 150 to 500 eV for 30 minutes at 10^{\circ}
from normal incidence. Ion bombardment of a Mo-clipped silicon sample (with Si clamps) at
250 eV and 10^{\circ} to a fluence of 4-8 × 10^{18} \text{ cm}^{-2} using C grids resulted in a distribution of dots
superimposed on a ripple-like structure (e.g., Fig. 4(a)). XPS measurements on specimens
irradiated with 4.2 × 10^{18} \text{ cm}^{-2} at 10^{\circ} and 250 eV revealed an apparent (not well-calibrated)
atomic Mo concentration of about 2 % when Mo clips and Si clamps had been used with either
Mo or C grids. In contrast, when using graphite grids and no clips, a ripple-like structure with no
dots formed, there was no XPS signal from any metal, and the apparent concentration of carbon
in the processed Si sample was indistinguishable from that in a new Si wafer taken directly out
of the box. RBS is insensitive to C on Si and the sensitivity of XPS to carbon is less than that to
molybdenum, and we are unable to put a reliable upper limit on the carbon coverage of our
samples. However, we attribute the observed difference — between dots using Mo grids and Mo
clips, and a featureless surface using graphite grids with no clips — to a trace metal
contamination effect. In order to eliminate metal contamination we settled on graphite grids and
clip-free indium soldering to a graphite substrate entirely shielded by silicon, as reported above,
and for each kinetic energy we chose the voltage of the accelerating grid so as to minimize the beam divergence.

**B. Type I (constant wavelength) and Type II (diverging wavelength) bifurcations**

Patterns for $\theta < 25^\circ$ ($\theta > 45^\circ$) were first observed at a fluence of $\sim 2 \times 10^{18} \ (1 \times 10^{17}) \text{ cm}^2$. The surface should become amorphous very quickly, after a fluence of the order $10^{14} \text{ ions cm}^{-2}$ [18]. A $\sim 3$-nm amorphous surface layer was observed in cross-sectional TEM of samples irradiated at 250 eV and fluences exceeding $10^{17} \text{ cm}^2$ at angles exhibiting both instability and stability. In a control experiment at 250 eV and $10^\circ$, no difference was found between pattern development on a crystalline Si wafer and on a wafer pre-amorphized with an 80 keV Si$^+$ implant to a dose of $10^{16} \text{ cm}^2$ that resulted in an initial amorphous layer thickness of 192 nm.

After irradiation, AFM images were obtained from a Digital Instruments Nanoscope D3100 AFM in tapping mode. In Fig. 2 we show topographs of surfaces irradiated at room temperature by 250 eV Ar$^+$ at various incidence angles. Notably, at incidence angles near $35^\circ$ the flat surface is stable under uniform ion sputter erosion. In Fig. 3 we show topographs of surfaces irradiated at room temperature at $10^\circ$ from normal incidence with Ar$^+$ of varying kinetic energy. To further investigate the relative stability of the flat surface and the patterned surface, we started with a saturated rippled structure formed using $8 \times 10^{18} \text{ Ar}^+ \text{ cm}^2$, 250 eV irradiation at $\theta = 10^\circ$ and observed decay at all wavevectors upon further irradiation at 500 eV with the same dose, as shown in Fig. 4 [19]. This observation proves that the flat surface is truly stable, rather than unstable with an amplification rate too low to be detected.

In Fig. 5 we compile our observations into a phase diagram of pattern formed (or lack thereof) in the linear regime vs. control parameter. Whereas at low $\theta$ we observe perpendicular mode ripples (wave vector perpendicular to the projected ion beam direction), at the high $\theta$ transition
to instability we see parallel mode ripples (wave vector parallel to the projected ion beam). Finally, at sufficiently high $\theta$ we observe perpendicular mode again. Several observations are qualitatively consistent with the phase diagram for 500-2000 eV Xe$^+$ irradiation of Si presented by Zibiri in his thesis [8], namely: an isotropic array of holes at normal incidence; a transition from holes to perpendicular mode ripples to flatness with increasing angle, and a transition from holes or perpendicular mode ripples to flatness with increasing energy at low angles. Other transitions, at higher energy or angle, appear to be sensitive to the particular system being studied.

We next focus on the bifurcation from a rippling instability to a stable flat surface as the control parameter ($\theta$ or $E$) traverses a critical value. To characterize this transition, we measured the RMS roughness and wavelength of the evolving pattern as the control parameter approaches the bifurcation point. In Fig. 6 we report the dependence of wavelength on $\theta$ and $E$ as the bifurcation points are traversed. Two key features are apparent. As the low angle transition is approached in either $\theta$ or $E$, the wavelength remains practically constant [20]. At the high angle transition, the wavelength grows rapidly, apparently indicating divergence [21].

With Figs. 7 and 8 we focus on the pattern amplification near the bifurcation points. Fig. 7a shows the RMS roughness vs. time during irradiation at several angles near the high-$\theta$ bifurcation. We take this as a proxy for the amplification rate at the most unstable wave vector, which is readily predicted by most theories. We do this because we did not find an objective way of quantifying the amplification rate at the most unstable wave vector under the conditions of this study. We believe this is justified because, according to Parseval's theorem, the RMS roughness is the sum of the contributions from all the wave vectors in reciprocal space, and normally (with an exception noted below) we expect the Fourier components at and around the most unstable wave vector to dominate all contributions. We observe saturation of the roughness after just a few
minutes. Many studies have reported patterns observed well into the saturation regime, where nonlinear effects may be important. In order to safely neglect nonlinear effects, our measurements are restricted to the pre-saturation regime of exponential amplification, permitting us to directly test linear stability theories. Note that the roughness at $\theta = 50^\circ$ initially decreases before beginning a slow rise. Our interpretation is that, out of the box, the silicon wafer's roughness spectrum is not well matched to that amplified by the ion beam and that an initial transient period occurs wherein the "wrong" Fourier components decay, eventually revealing the exponential amplification of the "right" Fourier components. Fig 7b shows that the amplification rate varies quadratically with deviation from the high-$\theta$ bifurcation point. Fig. 7c shows that the wavelength varies as the inverse square root of the misorientation. The power laws for the lines superposed on data are those expected for an infinite-wavelength bifurcation [12].

Fig. 8a shows the RMS roughness vs. time during irradiation at several angles near the low-$\theta$ bifurcation. We observe qualitatively similar amplification behavior as in the high-$\theta$ bifurcation (Fig. 7a) and offer the same interpretation, although the amplification rate here is slower and the initial transient lasts much longer and is observed over a wider range of angles. Figs. 8(b-c) show that the amplification rate varies linearly with control parameter near the low-$\theta$ bifurcation point. The linear power law for the lines superposed on the data in Fig 8(b-c) is that expected for a finite-wavelength (Fig. 6(a-b)) bifurcation [12].

The continuously vanishing amplification rate with control parameter indicates that all observed bifurcation points are supercritical. In the vicinity of supercritical bifurcations, pattern formation can be described by universal equations whose form depends only on general symmetries of the underlying dynamics and on the growth rate of the most unstable modes [12]. Hence any theoretical description of the patterns must agree with the global sequence of the experimen-
tally identified bifurcations: finite-wavelength at low angles and diverging-wavelength at high angles.

IV. DISCUSSION

Theories of sputter erosion predict a partial differential equation (PDE) for the evolution of a surface height profile \( h(x; y; t) \). By assuming that the average response of the surface to the impact of a single ion is characterized by a cavity derived from Sigmund's Gaussian ellipsoid collision cascade model [22], BH derived the following PDE:

\[
\frac{\partial h}{\partial t} = -I + \left\{ S_x \frac{\partial^2 h}{\partial x^2} + S_y \frac{\partial^2 h}{\partial y^2} - B \nabla^4 \right\} h ,
\]

where \( I(\theta) \) is the vertical erosion rate of a flat surface, \( S_x(\theta) \) and \( S_y(\theta) \) are its curvature coefficients, and \( B \) is a material parameter describing relaxation and containing the surface free energy and either the surface diffusivity or the viscosity of the ion-stimulated layer. A negative value of \( S_x \) or \( S_y \) leads to instability. BH showed that the Gaussian ellipsoid response implies \( S_y < 0 \) for all \( \theta \) and \( E \), i.e. a flat surface is unstable for some wavevector perpendicular to the ion beam. Regions of stability of a flat surface in our study, as well as several previous experimental studies of amorphous systems covering a sufficient range of incident angles to test this prediction, show it to be incorrect.

Modifications to the BH model have been proposed that allow stability for some range of incidence angles. Davidovitch et al. [11] considered a modification of BH that results in replacing the BH curvature coefficients \( S_x; S_y \) by effective coefficients \( S_x^{\text{eff}} \), \( S_y^{\text{eff}} \), whose control parameter dependence contains regimes where both coefficients are positive, implying stability of flat sur-
faces. These can arise either from response functions to ion impact with shapes different than Gaussian ellipsoids, or from ion-induced surface currents at the impact site as envisaged by Carter and Vishnyakov [6,10]. With ion-induced surface currents as the only modification to BH theory, $S_{x}^{\text{eff}}$ and $S_{y}^{\text{eff}}$ can both be positive at low angles (i.e. stability, as we observe), with a sign change in $S_{z}^{\text{eff}}$ occurring at intermediate angles [11] causing a parallel-mode instability. For these models the pattern wavelength diverges at the bifurcation point [11]. This is a potential explanation of our observations at the high-θ bifurcation point at both high and low Ar$^{+}$ ion energy (Fig. 5) but cannot explain the behavior we observe at the low-θ bifurcation identified at low ion Ar$^{+}$ energy. Therefore the patterns formed at low angles and low ion energies must be caused primarily by a mechanism qualitatively different than those considered so far.

Davidovitch et al. have argued that there are at least two ways for a bifurcation to occur with finite wavevector $\mathbf{q}$ (i.e. non-diverging wavelength) [11], such as we observe at low angle. Both of the ways identified so far involve non-local processes, requiring the introduction of integral operators whose range is much larger than the pattern wavelength. One way is by including the Facsko damping term $-K\left(h - \bar{h}\right)$, where $K$ is a positive constant [23,24], and the average height $\bar{h}$ appears for consistency with translational invariance; this adds a constant term $-Kq^{0}$ to the linear dispersion relation. We note that the Facsko term was offered as a proxy for a model of redeposition but has not been derived from more fundamental principles. It is intriguing to note that Brown and Erlebacher found just such a $-Kq^{0}$ term when they measured the dispersion relation over a range of wavenumber with positive amplification rate and fit it to a constant plus the BH dispersion relation (Fig. 9 of [25]). It is not possible to rule out effects of singular crystallo-
graphic energetics or kinetics because this measurement was performed on Si(111) at 733 °C, at which temperature the surface is almost certainly crystalline.

The other identified way to obtain a finite-wavelength bifurcation is by adding a $|q|^3$ term due to ion-induced stress in the ion-stimulated surface layer. This additional destabilizing term causes the Asaro-Tiller (AT) elastic energy-induced instability of solid surfaces [26, 27], and may become relevant if sufficient stress accumulates during the ion irradiation process [28, 29]. In this case the bifurcation occurs at finite $q$. The main problem with this mechanism is that preliminary in situ stress measurements [30] indicate stresses less than 200 MPa for which the standard ($S_{\text{eff}} = 0$) model [27] predicts an instability wavelength two orders of magnitude larger than that observed. Instabilities from a stress of this magnitude can work only if there is another (as yet unknown) mechanism for increasing its tenacity.

Another possible scenario, which we are currently investigating, is that the shape of the single-impact crater function varies from Sigmund’s Gaussian ellipsoid response so as to change the relative stability of perpendicular and parallel mode at low angle (so that $S_{\text{eff}} \leq S_{\text{eff}} \leq 0$), while reversing their stability $S_{x_{\text{eff}}} < S_{y_{\text{eff}}} < 0$) at higher angles. In this form, the model would still predict diverging wavelengths at the bifurcation points. An additional process such as one of the non-local ones discussed above would still have to be significant in the vicinity of the finite-wavelength (low-$\theta$) bifurcation.

V. CONCLUSIONS

We have examined stability and instability in the linear, exponential amplification regime for silicon surfaces. The phase diagram of pattern vs. the control parameters $E$ and $\theta$ exhibits regions of stability bordered by supercritical bifurcations of finite wavelength at low $\theta$ and diverging
wavelength at high $\theta$. The power laws observed for the amplification rate and the wavelength in the vicinity of these bifurcation points are consistent with those expected from the theory of non-equilibrium pattern formation. The BH theory is contradicted by the existence of the bifurcations as well as by the appearance, with increasing angle, of perpendicular mode before parallel mode ripples. The simplest modifications to the theory, such as the ion induced surface current mechanism envisioned by Carter and Vishnyakov, are insufficient to explain the finite-wavelength bifurcation at low $\theta$. It is surprising to find that even in the linear regime for isotropic, elemental systems, at least one and quite possibly two additional physical effects beyond those in BH are necessary to explain the observed experimental results. A better understanding of the role of stress in the amorphous layer, a physical process leading to a nonlocal damping term, and the characterization of actual crater functions in physical experiment or MD simulation should be considered high research priorities.

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References

[14] Veeco, Fort Collins, CO.


[20] We find the same qualitative behavior -- a transition to a flat surface between 280 and 300 °C -- as the temperature is raised at 10° off normal incidence with ion energy 250 eV. We do not dwell on this case, however, because complications may arise involving a potentially decreasing degree of amorphousness of the surface with increasing temperature. Likewise, Gago R, Vazquez L, Plantevin O, Sanchez-Garcia J A, Varela M, Ballesteros M C, Albella J M and Metzger T H 2006 Phys. Rev. B 73 155414 reported no divergence in the dot spacing of saturated Si structures at normal incidence as the transition to flatness is approached with increasing temperature.


Figure Captions

FIG. 1. Effect of Molybdenum (Mo) clips on surface morphology following irradiation with 250 eV Ar⁺, 30° off-normal incidence, and fluence of $6.4 \times 10^{18}$ Ar⁺ cm⁻² using graphite grids. (a)-(d) display scanning electron microscopy (SEM) images within 1 μm of the edge of the Mo clips, and 50 μm, 100 μm and 1000 μm away from the clips, respectively. The projected ion beam runs from the bottom of the page to the top. The clip edge is located just off the left edge in (a), running vertically. The SEM scan size is 1.5 μm × 1.125 μm.

FIG. 2 (color online). Effect of incidence angle on surface morphology following irradiation with 250 eV Ar⁺ at room temperature. In all cases, the projected ion beam runs from the bottom of the page to the top. The AFM topograph scan size is 2 μm × 2 μm in (a)-(c) and 1 μm × 1 μm in (d)-(f). (a) 0°, $3.8 \times 10^{18}$ Ar⁺ cm⁻² (18 minutes), vertical range 3 nm. (b) 10°, 18 min., vertical range 3 nm. (c) 35°, 18 min., vertical range 3 nm. (d) 50°, $3.2 \times 10^{17}$ Ar⁺ cm⁻² (90 s.), vertical range 2 nm. (e) 70°, 90 s., vertical range 3.5 nm. (f) 80°, 90 s., vertical range 3.5 nm.

FIG. 3 (color online). Effect of ion energy on surface morphology following irradiation at 10° from normal incidence at room temperature. In all cases, the ion fluence is $3.8 \times 10^{18}$ Ar⁺ cm⁻² (18 minutes), the projected ion beam runs from the bottom of the page to the top, the AFM topograph scan size is 2 μm × 2 μm and the vertical range is 2 nm. The image in Fig. 2(b) may be considered to be the first image in this sequence.

FIG. 4 (color online). Top row: 5 μm x 5 μm AFM topographs of (a) a saturated rippled structure formed with 250 eV Ar⁺, 10° off-normal incidence, ambient temperature and ion fluence of 8 ×
10^{18} \text{ Ar}^+ \text{ cm}^{-2} (30 \text{ minutes at } 0.7 \text{ mA cm}^{-2}) \text{ and of (b) a stable flat surface obtained by irradiating sample in (a) with a fluence of } 8 \times 10^{18} \text{ Ar}^+ \text{ cm}^{-2} \text{ at 500 eV Ar}^+ \text{ and 10}^\circ \text{ off-normal incidence.}

The projected ion beam runs from the bottom of the page to the top and the vertical range is 7 nm in both images. Second row: Time sequence of 1-D circularly averaged power spectral densities (PSDs) resulting from ion bombarding sample starting with configuration shown in panel (a). The very high frequency peaks at $\sim \log_{10}[q(\mu\text{m}^{-1})] = 2.5$ are scanning artifacts from the AFM. Note that with increasing fluence both peaks centered at 125 $\mu\text{m}^{-1}$, corresponding to impurity-induced dots, and 56 $\mu\text{m}^{-1}$, corresponding to the saturated ripple structure, decay.

FIG. 5 (color online). Phase diagram for linear regime of pattern formation vs. control parameters $\theta$ and $E$. $\times$: flat; $+$: holes; circles: perpendicular mode ripples; squares: parallel mode ripples. Fluence is $3.8 \times 10^{18} \text{ Ar}^+ \text{ cm}^{-2}$ except for ripples at $\theta \geq 50^\circ$, where fluence is $3.2 \times 10^{17} \text{ Ar}^+ \text{ cm}^{-2}$.

FIG. 6 (color online). Ripple wavelength in the linear regime vs. (a) $\theta$ at $E = 250 \text{ eV}$; (b) $E$ at $\theta = 10^\circ$. Circles: perpendicular mode; squares: parallel mode.

FIG. 7 (color online). Behavior near bifurcation points for high-$\theta$ ripples at $E = 250 \text{ eV}$. (a) Pattern amplitude (reckoned as RMS surface roughness) vs. time. Squares: 65$^\circ$; $\times$: 60$^\circ$; $+$: 55$^\circ$; circles: 50$^\circ$. (b) Amplification rate vs. misorientation for high-$\theta$ bifurcation, showing quadratic dependence. (c) Wavelength vs. misorientation for high-$\theta$ bifurcation, showing inverse square root dependence.
FIG. 8 (color online). Behavior near bifurcation points for low-\(\theta\) ripples. (a) Pattern amplitude (reckoned as RMS surface roughness) vs. time, \(E = 250\) eV. Squares: 17.5\(^{\circ}\); +: 15\(^{\circ}\); \times: 12.5\(^{\circ}\); circles: 10\(^{\circ}\). (b) Amplification rate vs. misorientation, showing linear dependence, \(E = 250\) eV. (c) Amplification rate vs. \(E\) at \(\theta = 10^{\circ}\), showing linear dependence.
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