Stochasticity in the symmetric division of plant cells: when the exceptions are the rule

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Long before most of the molecular aspects of cell division were uncovered, L. V. Heilbrunn remarked that: “it is easier to make a new theory of cell division than to test an old one” and promised his readers to limit his treatment of cell division to “the factual facts regarding the physical changes which take place during mitosis” (Heilbrunn, 1928). Heilbrunn’s own work was inspired by Plateau’s observations on soap films, along with the properties of soap films. Heilbrunn’s findings were published both in French and German, and they earned him the title of a “cell wall, at the moment of its formation, tends to assume the form which a weightless liquid film would assume under the same conditions” (Errera, 1886, 1888). Errera draws several conclusions from his new principle, most importantly that division planes ought to be surfaces of constant mean curvature and that the division plane is not a natural consequence of his theory. However, one conclusion that Errera appears to avoid is that the dividing wall, being subjected to the same surface tension as soap films, will invariably assume the configuration of minimal surface area. Errera’s omission is in sharp contrast with statements made at the same time by Berthold (1886) who insisted on the minimization of area. One finds an explanation for the deliberately broad definition adopted by Errera in the work of one of his student, de Wildeman (1893). de Wildeman follows Errera’s soap film analogy but now recognizes the possibility of multiple division planes for a given cellular morphology. He says: “When new walls, under the influence of their own tension, are fashioned into surface of constant or zero mean curvature; they represent minimal surfaces. But it is a relative minimum rather than an absolute minimum, as clearly indicated by Plateau. It is therefore not necessary that all new walls in a cell occupy, of all the possible positions, the one of least area” (p. 9). Later in his monograph, de Wildeman returns to this theme—“the dividing wall possesses a fairly large leeway in adopting its form. In fact, it will find itself in a stable equilibrium as long as its surface is a relative area minimum, its mean curvature is constant and it attaches itself to the surrounding wall at right
angle…” (p. 76). The quadrant cell, a favorite of Berthold (1886), illustrates well the different relative area minima that are possible within a cell and thus the “fairly large leeway” a cell possesses in selecting a division plane (Figures 1A–F). It is striking that Errera and de Wildeman recognized the co-existence of multiple division planes for a given cell geometry and therefore excluded in very explicit terms a deterministic interpretation of their division rule. This subtle view of plant cell division, however, was not meant to persist very long.

THE PRINCIPLE OF MINIMAL AREA

Ironically, the nuanced version of Errera’s rule seems to have been lost because of a desire to check its predictive power. To be tested, Errera’s rule had to move beyond the level of a soap film analogy to a fully operational definition giving explicit predictions for specified cellular geometries. Thus, Berthold’s principle of minimal area came to be the incarnation of Errera’s rule whenever predictions had to be made. This tension is clearly seen in D’Arcy Thompson’s book “On Growth and Form” (Thompson, 1917). Thompson first states Errera’s rule following precisely the soap film analogy used by Errera himself (p. 306) but as he prepares to calculate the division plane of an idealized quadrant cell, he promptly equates Errera’s rule to Berthold’s minimal area principle: “the incipient partition-wall of a dividing cell tends to be such that its area is the least possible by which the given space-content can be enclosed.” (p. 348). Following Thompson’s work, the great majority of references to Errera’s rule are cast in terms of an absolute area minimum; while the 1886 formulation and its nuanced interpretation were revisited only on a handful of occasions in the twentieth century. Wardlaw must be credited for the final and clearest statement of the spirit of Errera’s rule, which appeared in a book commemorating the centennial of Leo Errera’s birth:

“In essence, Errera was calling attention to fundamental physiological and physical relationship, the relationship so aptly described in the title of his classical paper—a fundamental condition of equilibrium in living cells. In this general approach we are reminded of the writings of Plateau, from which Errera’s idea was derived; for Plateau stated quite clearly that a surface of minimal area was to be understood as a relative minimum, determined as it would be by all the material agencies. If, therefore, we accept Errera’s Law in its general aspect (as he himself clearly intended), recognizing that in different biological circumstances other factors will inevitably become incident and may affect the pattern of wall formation to a greater or less extent, then the value of the Law, far from being diminished by seeming exceptions, is enhanced by them” (Wardlaw, 1960).

It is probably fair to say that Wardlaw’s lucid reflections, just as those of Errera and de Wildeman, left no mark on the field of cell biology until stochasticity forced itself into experiments.

REVISITING STOCHASTICITY

The first inkling of the importance of stochasticity in cell division came from studies of the morphogenetic transitions in fern protonemata; most prominently the analysis by Cooke and Paolillo of division plane selection in the apical cell of protonemata (Cooke and Paolillo, 1980, see also Miller, 1980). Cooke and Paolillo’s data show that the transverse and longitudinal division planes co-exist for a broad range of cell geometries but are expressed in different proportions depending on the aspect ratio of the apical cell. Thirty years later, Dupuy et al. (2010) obtained similar results for the marginal cells of Coleochaete.

By demonstrating broad transitions between different modes of cell division, these works paved the way for a
fully stochastic division rule in which two or more division planes, each representing a local area minimum, compete to express themselves in a given cell geometry. However, an important question remained: can a unique stochastic model explain the selection of a division plane in a broad range of plant systems? We set out to answer this question in 2007, after having rediscovered de Wildeman’s alternative division planes while preparing a figure for a review paper (Dumais, 2007). Our results showed that the competing division planes are observed according to a precise probability function and, more importantly, that this function is conserved across a wide sampling of plant systems (Besson and Dumais, 2011) (Figure 1G). Therefore, although it is impossible to predict the exact way a cell will divide, it is possible the compute precisely the possible division planes and their respective probability. Using this new information, we reformulated Errera’s rule as: symmetrically dividing plant cells select a division plane from a set of minimal area configurations according to an exponential probability distribution that increases inversely with the surface area of the configurations. This definition formalized the rule described by Errera and de Wildeman more than 100 years earlier.

THE ORIGIN AND ROLE OF STOCHASTICITY

This account of plant cell division has left out one important side of the story—the sustained effort to uncover the molecular underpinnings of mitosis. Two questions arise naturally if one accepts Errera’s rule for plant cell division. First, what components or properties of the cell division machinery allow the cell plate to behave like a soap film? Second, what is the molecular basis of the stochasticity observed at the cellular level? The first question was addressed by Lloyd, Venverloo and co-workers who provided evidence that tense cytoskeletal elements projecting from the nucleus and interacting with the pre-prophase band can explain many of the features associated with the positioning of the division plane (Venverloo and Libbenga, 1987; Lloyd, 1991). Based on this seminal work, we have argued that the stochasticity observed at the cell level is a reflection of the stochasticity inherent to the cytoskeletal dynamics supporting the selection of the division plane. In particular, we showed that the observed division planes correspond to the most probable distribution of tense microtubular strands competing over a fixed pool of tubulin (Besson and Dumais, 2011). Thus, the stochasticity observed at the cell level is only a reflection of the dynamic instability of microtubules that allows them to “sense” a cell’s geometry by exploring several configurations spanning the entire cell volume. Such conclusion forces us to shift perspective on the role of stochasticity in cell biology. Stochasticity does not always reflect a lack of regulation; it can also be the mechanism of regulation. Without dynamic remodeling of the cytoskeleton, cells could not sense their shape and therefore would be unable to align their division plane. Other examples of stochasticity playing a constructive role in biology have been demonstrated in the perception of weak signals by biological sensors (Wiesenfeld and Moss, 1995) and the “search and capture mechanism” allowing the spindle to attach to chromosomes (Holy and Leibler, 1994).

OVERCOMING STOCHASTICITY

If the underlying mechanism for the selection of a division plane is intrinsically stochastic, how can we explain the regularity of developmental events? To answer this question, it is important to realize first that stochasticity does not mean absence of control. In that respect, a notable consequence of the stochastic division rule expounded above can be deduced directly from the exponential law that governs it (Figure 1G). While isodiametric cells (small \( \delta_{ij} \) values) exert poor control over the selection of their division plane, highly elongated cells (large \( \delta_{ij} \) values) adopt reliably the division plane of absolute minimal area and, as a result, invariably cut their long axis. The stochastic division rule thus approximates a deterministic rule whenever a cell deviates strongly from an isodiametric shape. This fact alone can explain a broad range of stereotypical cellular patterns even if the underlying mechanism is stochastic (Besson and Dumais, 2011).

As noted soon after the publication of Errera’s paper, there are however several plant tissues where cell division deviates systematically from any division rule that one could formulate based on the behavior of soap films. Explicit examples are found in the division of cambial initials, the formation of stomatal complexes (Rasmussen et al., 2011) and early embryogenesis (Yoshida et al., 2014). All of these examples fit under the rubric of asymmetric cell division. Observations of asymmetric cell division suggest a level of control above a cell’s own geometry. What those controls are remains unclear although auxin signaling (Yoshida et al., 2014) and mechanical stress (Uytteewal et al., 2012; Louveau and Hamant, 2013) are promising candidates. Thus, the emerging picture for the control of plant cell division is one where a stochastic division mechanism governs a broad range of symmetric cell divisions based solely on cell geometry; while a deterministic division mechanism, presumably based on global cues rather than local cues, takes over when the fulfillment of a specific cellular pattern is a necessity.

CONCLUSION

This brief historical survey of the origin and evolution of division rules for plant cells highlights the difficulties in acknowledging stochasticity in biology. Fluctuations are an integral part of biology but are too often interpreted as masking underlying deterministic processes. As a result, the subtle division rule outlined by Errera was neglected for over one century because it implied stochasticity in the selection of a division plane. It is now clear that stochasticity can play a constructive role in the cell; either by supporting cytoskeletal dynamics (Holy and Leibler, 1994; Besson and Dumais, 2011) or allowing receptors to perceive faint signals (Wiesenfeld and Moss, 1995). We can expect many more examples to arise as cell biologists become more attuned to thinking in terms of stochasticity.

REFERENCES


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