Nanoshells as a high-pressure gauge analyzed to 200 GPa

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Nanoshells as a high-pressure gauge analyzed to 200 GPa

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In this article, we present calculations that indicate that nanoshells can be used as a high-pressure gauge in diamond anvil cells (DACs). Nanoparticles have important advantages in comparison with the currently used ruby fluorescence gauge. Because of their small dimensions, they can be spread uniformly over a diamond surface without bridging between the two diamond anvils. Furthermore, their properties are measured by broad-band optical transmission spectroscopy leading to a very large signal-to-noise ratio even in the multi-megabar pressure regime where ruby measurements become challenging. Finally, their resonant frequencies can be tuned to lie in a convenient part of the visible spectrum accessible to CCD detectors. Theoretical calculations for a nanoshell with a SiO2 core and a golden shell, using both the hybridization model and Mie theory, are presented here. The calculations for the nanoshell in vacuum predict that nanoshells can indeed have a measurable pressure-dependent optical response desirable for gauges. However, when the nanoshells are placed in commonly used DAC pressure media, resonance peak positions as a function of pressure are no longer single valued and depend on the pressure media, rendering them impractical as a pressure gauge. To overcome these problems, an alternative nanoparticle is studied: coating the nanoshell with an extra dielectric layer (SiO2) provides an easy way to shield the pressure gauge from the influence of the medium, leaving the compression of the particle as a result of the pressure as the main effect on the spectrum. We have analyzed the response to pressure up to 200 GPa. We conclude that a coated nanoshell could provide a new gauge for high-pressure measurements that has advantages over current methods. © 2011 American Institute of Physics. [doi:10.1063/1.3665649]

I. INTRODUCTION

Recently, nanoshells1 have received a lot of attention because they possess interesting optical properties. Consisting of a dielectric core surrounded by a metallic shell, nanoshells allow surface plasmon polaritons to exist at the interfaces between the layers, resulting in a spectrum with very pronounced absorption and extinction peaks. The position and broadness of these resonance peaks depend on the size, shape, and materials of the particles and on the surrounding medium. This versatility and sensitivity make nanoshells excellent probes in different fields, ranging from cancer ablation2 and biosensors3 to surface-enhanced Raman spectroscopy applications4 and plasmonics.5 In this paper, we investigate the usefulness of nanoshells in the field of high-pressure physics, and more precisely diamond anvil cell (DAC) pressure measurements.6 The first theoretical calculations for a spherically symmetric SiO2-gold nanoshell under pressure (up to 200 GPa) are presented, indicating clear measurable absorption peaks. The main idea behind the use of nanoshells as a pressure gauge is that the size of the nanoshell and the permittivity of the SiO2 core and of the medium will change under pressure resulting in a shift of the resonance frequencies. The goal of this paper is to calculate the optical transmission as a function of wavelength for a spatial distribution of noninteracting monodisperse nanoshells.

At the moment, there are several pressure gauges used in high-pressure physics. We briefly discuss them and conclude with the advantages of the nanoshell gauge in comparison with the established methods. The prime and venerable pressure gauge is the shift of the peak of the ruby fluorescence spectrum with pressure,7,8 excited by laser pumping. In this case, micron-sized ruby grains are embedded in the pressurization medium. Several problems can arise above a certain pressure:9,10 at pressures above 100 GPa, diamond fluorescence can become intense and mask the ruby line; ruby grains can be blown away during loading or masked during pressurization; above a few hundred GPa, the standard method of pumping the ruby with a green or blue laser line becomes ineffectual as the laser light is absorbed by the diamond anvils. Although some of these problems can be overcome,11,12 ruby becomes challenging to use at very high pressure. For cases where the ruby is lost or cannot be observed, researchers have used the phonon Raman spectrum of the diamond from the high-pressure culet or stressed region of the diamond. This is less precise and has some dependence on the diamond geometry.13 Another method is to embed a grain of diamond in the pressurization medium, but this also has challenges and limitations.14 An important gauge is the x-ray spectrum of metal markers embedded in the pressurization medium, but this is only useful at synchrotrons. Finally, we mention that many of the pressure gauges have problems at high temperatures. The advantages of the nanoshells, which come dispersed in a volatile fluid, is that they can be painted onto the diamond culet in a thin invisible

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(to the eye) layer so they will not blow out and they cover the entire culet flat so they cannot easily be masked; they should maintain their sensitivity to the highest pressures. Optical spectroscopy is easy to implement with a large signal-to-noise ratio, compared to fluorescence or Raman scattering, and will not be masked by fluorescence from the diamonds. We believe that nanoshells will maintain their sensitivity at high temperatures, but this requires further study.

The article is organized as follows. In Sec. II, we first review existing theories that can be used to calculate the spectrum and resonance frequencies of a nanoshell. Next, the pressure dependency is taken into account. In Sec. III, the results of the calculations are shown for the nanoshell geometry. To overcome some of the problems seen with nanoshells, the coated nanoshell is introduced in Sec. IV. Section V contains the conclusions.

II. THEORY

The optical properties of nanoshells are usually described by either Mie theory or the hybridization model. The hybridization model, developed by Prodan and co-workers,15 offers a fast-to-evaluate analytical form for the resonance frequencies, but it is only valid for small particles (smaller than ca. a tenth of the wavelength). Mie theory16 is valid for all particle sizes, but this method is far more time consuming for calculating the peak positions, because it does not allow for a closed-form analytical formula for the position of the resonance peak. These resonance-peak positions have to be numerically derived from the absorption or extinction spectrum.

In this section, both theories will be reviewed. The pressure dependency is taken into account in the last part of this section.

A. Hybridization theory

Hybridization theory is a phenomenological approach in which the nanoshell is modeled as a combination of a cavity and a metallic sphere. First, the sphere and cavity are studied separately. The free electrons of the sphere are described as an incompressible fluid excited by plasmons and the dielectric function is assumed to be that of a Drude metal:

$$\varepsilon_s(\omega) = \varepsilon_b - \frac{\omega_{\text{pl}}^2}{\omega^2},$$  (1)

where $\varepsilon_b$ indicates the background permittivity and $\omega_{\text{pl}}$ the bulk plasma frequency of the metal.

In a second step, the resonance frequencies of the cavity and the sphere are hybridized because of the coupling between the cavity and the sphere modes, very similar to the hybridization of molecular orbitals. This results in a closed formula for the resonance frequencies:19

$$\omega_{L,c}^2 = \frac{\omega_{\text{pl}}^2}{\beta} \left( (L + 1)^2 \varepsilon_m + 2L(L + 1) \varepsilon_b + L^2 \varepsilon_c \right)$$
$$+ L(L + 1) \left( \varepsilon_m - 2\varepsilon_b + \varepsilon_c \right) x^{2L+1}$$
$$\pm \left\{ \left[ L^2 \varepsilon_c - (L + 1)^2 \varepsilon_m + L(L + 1) \left( \varepsilon_m - \varepsilon_c \right) x^{2L+1} \right]^2 - 4L(L + 1) \left[ (L + 1) \varepsilon_m + L\varepsilon_c \right] x^{2L+1} \right\}^{1/2},$$  (2)

with:

$$\beta = 2\left\{ \left[ (L + 1) \varepsilon_b + L\varepsilon_c \right] \left[ (L + 1) \varepsilon_m + L\varepsilon_b \right] + L(L + 1) \left( \varepsilon_b - \varepsilon_c \right) \left( \varepsilon_m - \varepsilon_b \right) x^{2L+1} \right\},$$  (3)

where $\varepsilon_c$, $\varepsilon_b$, and $\varepsilon_m$ are the permittivities of the core, the background of the shell (see formula (1)), and the medium, respectively, and $L$ is the orbital quantum number and $x = R_c / R_s$ is the ratio between the core $(R_c)$ and shell $(R_s)$ radii.

B. Mie theory

Mie theory is used to solve the Maxwell equations in systems with spherical symmetry.16 It allows the calculation of the absorbed, scattered, and total cross section for an incident beam of radiation as a function of frequency. The nanoshell is modeled as two concentric spheres. For this case, the results originally derived by Mie for a single spherical interface were worked out by Aden and Kerker.20 The coated nanoshell, which will be introduced later, is modeled by three concentric spheres. Extending Mie theory to three concentric spheres, although not available in the literature, does not provide any new problems in comparison with the two-concentric-sphere case solved by Aden and Kerker. The final expressions for the electromagnetic fields in and around the coated nanoshell, as well as the scattering and absorption cross section, are given in the Appendix. From the resulting total cross section, the resonance frequencies can be determined numerically.

For this method, the input parameters are again the sizes and permittivities of the shells. In analogy with the hybridization model, we used the Drude dielectric function in Mie theory to describe the permittivity of the metal shell.

C. Pressure dependency: Equation of state

Applying a pressure $P$ to a nanoshell will lead to a change of the volume of the core $V_c(P)$ and the shell $V_s(P)$. These changes can be calculated using the Vinet equation of state (EOS) (Ref. 21):

$$P = 3K_0 \left( \frac{V}{V_0} \right)^{2/3} \exp \left\{ \frac{3}{2} (K_1 - 1) \left[ 1 - \left( \frac{V}{V_0} \right)^{1/3} \right] \right\},$$  (4)

which gives the relation between the pressure $P$ and the relative volume change $V/V_0$ with respect to a reference volume $V_0$ of a material at a certain temperature. Here $K_0$ and $K_1$ are material constants for which the values used in this article are presented in Table I. Using the Vinet EOS, one can calculate the size change of the nanoshell under pressure where $V_0$ has been taken as the original volume at zero pressure. Under pressure, the nanoshell will be compressed resulting in a different core and shell radius and a different bulk plasma frequency. These changes can be calculated from:

$$R_c(P) = R_c(0) \left( \frac{V_c(P)}{V_c(0)} \right)^{1/3},$$  (5)
The pressure dependency of the radii is shown in Fig. 1 for a nanoshell with \( R_s = 60 \) nm and \( R_c = 75 \) nm. When the nanoshell is compressed, the electron density will increase and so will the plasma frequency, Eq. (7). This will also influence the permittivity of the metal because the plasma frequency is an essential part of the Drude dielectric function (see Eq. (1)).

The pressure and frequency dependency of the permittivity of SiO\(_2\) in the megabar regime remains, to the best of our knowledge, unknown. However, it is possible to estimate the pressure dependency from the Vinet EOS using the Clausius-Mossotti relation:

\[
\varepsilon(\omega, P) = \frac{\varepsilon(\omega, 0) - 1}{\varepsilon(\omega, 0) + 2} \left( \frac{V_c(P)}{V_c(0)} \right),
\]

where \( V(P)/V_0 \) can be calculated from the Vinet EOS, Eq. (4), and \( \varepsilon(\omega, 0) \) represents the relative permittivity at zero pressure. The pressure dependency of the permittivity of SiO\(_2\), and some other possible medium materials, is shown in Fig. 2. Notice that there is no phase change in the SiO\(_2\) curve. In nature, SiO\(_2\) is in a crystalline phase at zero pressure and will switch to the amorphous phase at about 90 GPa. However, it has been reported\(^{26}\) that the fabrication method of the SiO\(_2\) particles results in cores that are in the amorphous state also at zero pressure.

### III. RESULTS FOR A NANOSHELL

Figure 3 shows the relative cross section of the considered nanoshell placed in vacuum as calculated with Mie theory. The relative cross section is the total optical cross section divided by \( \pi R_s^2 \), the area of the projection of the nanoshell on a plane perpendicular to the incoming radiation. From this figure, one can clearly see a substantial blueshift when 200 GPa pressure is applied. Another important observation concerns the width of the peak. This is important for increasing the precision in an experimental measurement, because sharper peaks allow for a more accurate determination of the peak position. However, sharp resonance lines may elude experimental detection if they do not carry enough spectral weight. In Fig. 3, one can see that the dipole

![Figure 1](image1.png)

**FIG. 1.** (Color online) The behavior of the sizes of the nanoshell under pressure. The top panel presents the radii of the core and shell as a function of pressure. Notice that the golden shell will be compressed more than the core until about 150 GPa where the core/shell ratio reaches a maximum. The bottom panel shows this ratio \( R_s/R_c \), which is an important parameter for the optical response. The radii of the nanoshells in this article correspond to the size of commercially available nanoshells.

![Figure 2](image2.png)

**FIG. 2.** (Color online) The pressure-dependent permittivity of different materials. The permittivity of SiO\(_2\) was calculated from the Vinet EOS and the Clausius-Mossotti relation. The other permittivities are based on the literature.\(^{27}\)

### TABLE I. The material properties used in the pressure calculations of the nanoshell. Parameters \( K_0 \) and \( K_3 \) are valid up to 580 GPa for gold and 150 GPa for amorphous silicon according to, respectively, Refs. 24 and 22. The last column indicates the relative permittivity at ambient pressure. The permittivity indicated for gold is the bulk permittivity \( \varepsilon_b \) as defined in Eq. (1).

<table>
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<tr>
<th>Material</th>
<th>( K_0 ) (GPa)</th>
<th>( K_3 ) (GPa)</th>
<th>( \varepsilon )</th>
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<td>Amorphous SiO(_2)</td>
<td>329 (Ref. 22)</td>
<td>4.1 (Ref. 22)</td>
<td>2.0449 (Ref. 23)</td>
</tr>
<tr>
<td>Au</td>
<td>167 (Ref. 24)</td>
<td>5.94 (Ref. 24)</td>
<td>6.9 (Ref. 25)</td>
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where \( V_c(P) \) and \( V_s(P) \) are the volumes of the core and the shell, respectively, \( n \) is the bulk electron concentration, \( e \) is the electron charge, \( \varepsilon_0 \) is the permittivity of vacuum, and \( m \) is the electron mass. The pressure dependency of the radii is shown in Fig. 1 for a nanoshell with \( R_s = 60 \) nm and \( R_c = 75 \) nm. When the nanoshell is compressed, the electron density will increase and so will the plasma frequency, Eq. (7). This will also influence the permittivity of the metal because the plasma frequency is an essential part of the Drude dielectric function (see Eq. (1)).

The pressure and frequency dependency of the permittivity of SiO\(_2\) in the megabar regime remains, to the best of our knowledge, unknown. However, it is possible to estimate the pressure dependency from the Vinet EOS using the Clausius-Mossotti relation:\(^{17}\)

\[
\varepsilon(\omega, P) = \frac{\varepsilon(\omega, 0) - 1}{\varepsilon(\omega, 0) + 2} \left( \frac{V_c(P)}{V_c(0)} \right),
\]

where \( V(P)/V_0 \) can be calculated from the Vinet EOS, Eq. (4), and \( \varepsilon(\omega, 0) \) represents the relative permittivity at zero pressure. The pressure dependency of the permittivity of SiO\(_2\), and some other possible medium materials, is shown in Fig. 2. Notice that there is no phase change in the SiO\(_2\) curve. In nature, SiO\(_2\) is in a crystalline phase at zero pressure and will switch to the amorphous phase at about 90 GPa. However, it has been reported\(^{26}\) that the fabrication method of the SiO\(_2\) particles results in cores that are in the amorphous state also at zero pressure.
peak (the rightmost peak) is a broad, clear, and rather symmetric peak, whereas the quadrupole peak is much sharper and a good candidate for these kinds of experiments. Numerically, however, it is easier to track the broad dipole peak; thus, all results presented here will be with regard to the dipole peak. It is seen that although the quantitative results differ for all peaks, the qualitative results presented here hold true for all resonance peaks.

In Fig. 4, the position of the dipole resonance peak is shown as a function of pressure for a nanoshell in a medium with $\varepsilon = 1$ constant. The filled squares are calculated using Mie theory and a subsequent numerical determination of the peak maximum. The results from the hybridization theory are presented by the open circles. It is clear that the two theories diverge from each other only at higher pressures. The inset is also an indication of the resolution that can be useful because both theories agree well on the amount the resonance peak shifts. The inset is also an indication of the resolution that could be achieved. For this example nanoshell, the dipole resonance peak shifts over 75 nm when 200 GPa pressure is applied [for rubies, this would be 51.1 nm (Refs. 9 and 10)].

To determine the usefulness of nanoshells as a pressure gauge, calibration would need to be done for every pressure medium separately. The nanoshell’s optical response depends on the dielectric function of the surrounding medium in which it is placed, and, as such, both the position of the resonance peaks and their pressure-induced shift will differ for different pressure media. The original data used for the calculation of the dielectric function are shown in Table II. In Fig. 5, one can see the pressure dependency of the position of the dipole resonance peak for different pressure media: helium, hydrogen, and neon. The behavior of the medium under pressure clearly has a large influence on the optical response of the nanoshell. For these media, the blueshift that occurs in vacuum has turned into a redshift as pressure is increased. From a certain pressure and onward, there will be almost no shift of the resonance peak, rendering the nanoshells ineffectual as pressure gauges in that region. Although it is possible to calculate the optical response of nanoshells for much higher pressures, the results are not presented here because they are based on extrapolation of data from a limited pressure region and, as such, are considered unreliable.

IV. RESULTS FOR A COATED NANOSHELL

As was seen in the previous section, the simple nanoshell geometry is not ideal for high-pressure experiments. The peak shift is affected by the pressure medium so calibration will be necessary for each nanoshell and medium. A possible solution would be to shield the nanoparticle from...
the effects of the medium, therefore allowing the shift of the resonance peak to be influenced only by the compression of the nanoparticle. The absence of these problems when the nanoshell is placed in vacuum indicates that shielding the particle could indeed result in the desired effect.

Shielding the nanoparticle from the environments means creating a barrier between the golden shell and the dielectric medium. This barrier should also be a dielectric. If not, another set of surface plasmon polaritons would arise on the interface between the outer layer and the environment, counteracting the intent of the extra layer. In this article, the extra coating is achieved by adding an extra SiO$_2$ layer to the model and extending Mie theory to three concentric spheres. Henceforth, we shall indicate this type of “nanomatryushka” as “coated nanoshell.” The main question to be answered is how thick this coating should be to effectively shield the nanoshell from the pressure effects on the dielectric function of the environment. Figure 6 presents the dipole peak position for several coating thicknesses of the coated nanoshell as calculated by Mie theory. For reasons of comparison, the core and the thickness of the golden shell are kept the same as for the nanoshell discussed before. Furthermore, we have only studied the coated nanoshell in a helium environment because this is a commonly used quasi-hydrostatic pressure medium in DAC experiments. In neon, the results will be almost the same because the dielectric functions of helium and neon are similar. For hydrogen, the counteracting effect is not present, therefore the results with nanoshells are adequate and no further improvements are necessary.

In this article, we do not compare the calculations for the coated nanoshell with calculations using the hybridization model. The expansion of the hybridization theory for multiple-layered nanoshells is available in the literature, but it is not considered here because of the expected deviations, because the diameters of the coated nanoshell particles are two or three times larger than the nanoshell particles, and thus the electrostatic approximation is certainly not valid.

It can be seen from Fig. 6 that, for thin coatings, the redshift caused by the effect of the medium is still visible. At a certain pressure, the peak position will reach a maximum and from there on the peak will undergo a blueshift, which is caused by the compression of the nanoshell, similar to the results in vacuum (Fig. 4). This maximum is indicated by the

![FIG. 5. (Color online) The position of the dipole peak as calculated with Mie theory for various pressure media: helium (circles), hydrogen (diamonds), and neon (triangles). In all figures, the vacuum position is indicated in black for reference and the phase transition from liquid to solid is indicated. The plots only show the pressures for which experimental data is available. For completeness, the original data are presented in Table II together with the pressure range in which they are valid.](image)

![FIG. 6. (Color online) The dipole peak position as a function of pressure for the coated nanoshell with a 60-nm SiO$_2$ core, a 15-nm-thick golden shell, and for different thicknesses of the outer SiO$_2$ coating. For small coatings, the redshift caused by the medium is still clearly visible, whereas for thick coatings this effect seems to disappear. The crosses indicate the pressure at which the wavelength peak position is maximal and where the redshift turns into a blueshift.](image)
crosses and can be used as a measure for the pressure up to which the medium affects the optical response of the nanoparticle. It is clear that for thicker coatings, the maximum shifts to lower pressures suggesting that the influence of the medium indeed diminishes and thus that the coating effectively shields the nanoparticle. Unfortunately, the redshift never disappears completely, meaning that the influence of the medium cannot be fully shielded by the dielectric layer. However, it is possible to position the maximum into a pressure region where it can do no harm for the pressure measurements.

Obviously, the thickness of the coating has to be adjusted to the needs of the experiments. A thicker coating will provide better shielding, but bigger particles take up more space and risk interacting with each other because of being in close proximity of one another. However, because the coated nanoshell is much larger than the nanoshell, the absolute cross section is larger, meaning that a smaller density is sufficient while still gaining the same response.

The derivative of the curves on Fig. 6 give a direct indication of the sensitivity achievable with the coated nanoshell structures. On average, the sensitivity for the coated nanoshell with a 110-nm-thick coating (upper curve on Fig. 6) is approximately 0.90 nm/GPa. The resolution for rubies in the same pressure regime (0-20 GPa) is approximately 0.36 nm/GPa (Ref. 9) and for a nanoshell in vacuum, as was shown in Fig. 4, this would be 0.94 nm/GPa. From this, we can conclude that the theory predicts a better resolution for nanoshells than for rubies in the pressure regime under consideration.

V. DISCUSSION AND CONCLUSIONS

In this article, we have carried out a theoretical analysis of nanoshells, which can be designed so that they have absorption peaks in the IR-visible part of the optical spectrum because of scattering or absorption by localized surface plasmon polaritons. Calculations indicate that, for nanoshells in vacuum, these peaks have a substantial shift with pressure making them suitable as a pressure gauge for high-pressure research. A useful pressure gauge should have a calibration (peak wavelength versus pressure) independent of the pressurization medium. We found that for a simple nanoshell consisting of a SiO₂ core and a gold shell, the calibration differed with the pressurization medium; moreover it was double valued and had a region of zero slope. The latter problem was resolved by coating the nanoshell with a SiO₂ cladding, resulting in a robust sensitive pressure gauge. The proposed nanoshell gauge has advantages in comparison with well-established pressure gauges: they will not easily blow out during loading of a DAC, they cannot easily be masked by fluorescence from the diamonds, they have large signal-to-noise ratio in comparison to fluorescence and Raman Scattering, and, because of their small dimensions, they will not be stressed by bridging between the diamonds at very high pressure when the gasket thins. All of these putative advantages must be confirmed by experiment.

A possible implementation of the coated nanoshell would be to distribute them inside the DAC cell together with the ruby on the diamond culet. For low pressures, both gauges can be used and the coated nanoshell can be calibrated by using the extensive knowledge of the behavior of ruby under pressure. A possible challenge is the application of nanoshells to the surface of a diamond culet. Coated nanoshells can be acquired at high concentration (2 × 10⁹/µm³), from Nanospectra Biosciences, Inc., in a liquid solution. A droplet can be placed on the culet and allowed to evaporate to produce a coverage bonded to the surface by van der Waals forces. Preliminary measurements show that to avoid clustering and segregation, it may prove useful to functionalize the diamond surface with a film of poly-4-vinylpyridine (pvp), which has dense sites that localize the nanoparticles. For high pressures, the ruby measurement would be difficult or would no longer be possible. The spectra of the coated nanoshells, however, will still be measurable because these measurements are based on absorption and transmission. In this way, nanoshells could be easily used and effectively extend pressure measurements to ultrahigh pressures.

ACKNOWLEDGMENTS

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APPENDIX: ABSORPTION AND SCATTERING OF AN ELECTROMAGNETIC WAVE BY THREE CONCENTRIC SPHERES

The coated nanoshell was modeled using Mie theory for three concentric spheres. These spheres divide the space into four regions: the core of the nanoparticle, two shells, and the medium in which the nanoparticle is immersed, respectively numbered 1-4, as shown in Fig. 7. The radii of the three spheres are indicated with a, b, and c, from inner to outer. Using the notations of Bohren and Huffman, the incoming plane wave can be expanded in vector spherical harmonics:
\[ E_{4,i} = \sum_{n=1}^{\infty} E_n (\mathbf{M}_{o1n}^{(1)} - i \mathbf{N}_{o1n}^{(1)}), \]  
(A1)

\[ H_{4,i} = -\frac{k_0}{\omega \mu_4} \sum_{n=1}^{\infty} E_n (\mathbf{M}_{o1n}^{(1)} + i \mathbf{N}_{o1n}^{(1)}), \]  
(A2)

with:

\[ E_n = E_0 n^\ast \frac{2n+1}{n(n+1)}. \]  
(A3)

The vector spherical harmonics can be written as:

\[ \mathbf{M}_{o1n}^{(i)} = -z_n^{(i)}(kr) \pi_n(\cos \theta) \sin \varphi \bar{e}_\theta - z_n^{(i)}(kr) \tau_n(\cos \theta) \cos \varphi \bar{e}_\varphi, \]  
(A4)

\[ \mathbf{M}_{o1n}^{(i)} = z_n^{(i)}(kr) \pi_n(\cos \theta) \cos \varphi \bar{e}_\varphi - z_n^{(i)}(kr) \tau_n(\cos \theta) \sin \varphi \bar{e}_\theta, \]  
(A5)

\[ N_{o1n}^{(i)} = \left( \frac{1}{kr} z_n^{(i)}(kr) n(n+1) \pi_n(\cos \theta) \sin \theta \cos \varphi \bar{e}_r + d z_n^{(i)}(kr) \right) \times \tau_n(\cos \theta) \cos \varphi \bar{e}_\theta - d z_n^{(i)}(kr) \pi_n(\cos \theta) \sin \varphi \bar{e}_\varphi, \]  
(A6)

\[ N_{o1n}^{(i)} = \left( \frac{1}{kr} z_n^{(i)}(kr) n(n+1) \pi_n(\cos \theta) \sin \theta \cos \varphi \bar{e}_r + d z_n^{(i)}(kr) \right) \times \tau_n(\cos \theta) \sin \varphi \bar{e}_\theta + d z_n^{(i)}(kr) \pi_n(\cos \theta) \cos \varphi \bar{e}_\varphi, \]  
(A7)

where \( P_n^m(x) \) are the associated Legendre polynomials:

\[ \pi_n(\cos \theta) = \frac{P_n^1(\cos \theta)}{\sin \theta}, \]  
(A8)

\[ \tau_n(\cos \theta) = \frac{d P_n^1(\cos \theta)}{d \theta}, \]  
(A9)

and the radial dependent functions:

\[ z_n^1(kr) = j_n(kr), \]  
(A10)

\[ z_n^2(kr) = y_n(kr), \]  
(A11)

\[ z_n^3(kr) = h_n^{(1)}(kr). \]  
(A12)

On the right-hand side one can see the well-known spherical Bessel, Neumann, and Hankel functions, respectively.

In region 4, there will also be a scattered wave, which can be described by:

\[ E_{4,s} = \sum_{n=1}^{\infty} E_n (-a_n \mathbf{M}_{o1n}^{(3)} + ib_n \mathbf{N}_{o1n}^{(3)}), \]  
(A13)

\[ H_{4,s} = \frac{k_0}{\omega \mu_4} \sum_{n=1}^{\infty} E_n (b_n \mathbf{M}_{o1n}^{(3)} + ia_n \mathbf{N}_{o1n}^{(3)}), \]  
(A14)

where \( a_n \) and \( b_n \) are coefficients to be determined from the boundary conditions. The total electromagnetic wave in region 4 is therefore given by the sum of the incoming and the scattered fields.

The electromagnetic fields in the other three regions are given by:

\[ \begin{align*}
E_3 &= \sum_{n=1}^{\infty} E_n \left(e_n^{(1)} \mathbf{M}_{o1n}^{(1)} + e_n^{(2)} \mathbf{M}_{o1n}^{(2)} - id_n^{(1)} \mathbf{N}_{o1n}^{(1)} - id_n^{(2)} \mathbf{N}_{o1n}^{(2)}\right), \\
H_3 &= -\frac{k_0}{\omega \mu_4} \sum_{n=1}^{\infty} E_n \left(d_n^{(1)} \mathbf{M}_{o1n}^{(1)} + d_n^{(2)} \mathbf{M}_{o1n}^{(2)} + ic_n^{(1)} \mathbf{N}_{o1n}^{(1)} + ic_n^{(2)} \mathbf{N}_{o1n}^{(2)}\right), \\
E_2 &= \sum_{n=1}^{\infty} E_n \left(f_n^{(1)} \mathbf{M}_{o1n}^{(1)} + f_n^{(2)} \mathbf{M}_{o1n}^{(2)} - if_n^{(1)} \mathbf{N}_{o1n}^{(1)} - if_n^{(2)} \mathbf{N}_{o1n}^{(2)}\right), \\
H_2 &= -\frac{k_0}{\omega \mu_4} \sum_{n=1}^{\infty} E_n \left(g_n^{(1)} \mathbf{M}_{o1n}^{(1)} + g_n^{(2)} \mathbf{M}_{o1n}^{(2)} + ig_n^{(1)} \mathbf{N}_{o1n}^{(1)} + ig_n^{(2)} \mathbf{N}_{o1n}^{(2)}\right), \\
\end{align*} \]  
(A15)

\[ \begin{align*}
\mathbf{E}_1 &= \sum_{n=1}^{\infty} E_n \left(g_n \mathbf{M}_{o1n}^{(1)} - i \delta_n \mathbf{N}_{o1n}^{(1)}\right), \\
\mathbf{H}_1 &= -\frac{k_0}{\omega \mu_4} \sum_{n=1}^{\infty} E_n \left(s_n \mathbf{M}_{o1n}^{(1)} + i \delta_n \mathbf{N}_{o1n}^{(1)}\right). \\
\end{align*} \]  
(A16)

Using the boundary conditions:

\[ \mathbf{E}_j \times \bar{\mathbf{e}}_r = \mathbf{E}_{j+1} \times \bar{\mathbf{e}}_r, \]  
(A18)

\[ \mathbf{H}_j \times \bar{\mathbf{e}}_r = \mathbf{H}_{j+1} \times \bar{\mathbf{e}}_r, \]  
(A19)

at each interface, where \( \bar{\mathbf{e}}_r \) indicates the radial unit vector which is perpendicular to the boundary, we obtain a system of 12 coupled equations to be solved. This system of equations can be split in two sets of six equations that we write in matrix form \( A \cdot x = b \) with, for the first set of equations,

\[ A_1 = \begin{bmatrix}
0 & 0 & 0 & j_n(k_2a) & y_n(k_2a) & -j_n(k_2a) \\
0 & 0 & 0 & d_j(k_2a) & d_y(k_2a) & -\frac{\mu_k j_1}{\mu_1 k_2} d_j(k_1a) \\
-\frac{k_4 \mu_5}{\mu_4 k_3} h_n^{(1)}(k_4c) & j_n(k_3c) & y_n(k_3c) & 0 & 0 & 0 \\
-\frac{k_4 \mu_5}{\mu_4 k_3} d_j(k_4c) & d_j(k_3c) & d_y(k_3c) & 0 & 0 & 0 \\
0 & j_n(k_3b) & y_n(k_3b) & -j_n(k_3b) & -y_n(k_3b) & 0 \\
0 & d_j(k_3b) & d_y(k_3b) & -d_j(k_3b) & -d_y(k_3b) & 0
\end{bmatrix} \]  
(A20)

and
And for the second set of equations:

\[ b_1 = \begin{bmatrix} 0 & 0 & j_n(k_4c) \\ k_4 \mu_3 j_n(k_4c) & \mu_3 k_4 \frac{d j_n(k_4c)}{d y} & 0 \\ 0 & 0 & 0 \end{bmatrix} , \quad x_1 = \begin{bmatrix} a_n \\ e_n^{(1)} \\ e_n^{(2)} \end{bmatrix} . \quad (A21) \]

\[ A_2 = \begin{bmatrix} d j_n(k_3c) & d j_n(k_3c) & d y_n(k_3c) \\ k_3 \mu_2 j_n(k_3c) & y_n(k_3c) & 0 \\ 0 & 0 & 0 \\ \frac{\mu_2 k_3}{\mu_1} j_n(k_3c) & \frac{\mu_2 k_3}{\mu_1} y_n(k_3c) & -j_n(k_3c) \end{bmatrix} , \quad (A22) \]

\[ b_2 = \begin{bmatrix} 0 & 0 & d j_n(k_4c) \\ k_4 \mu_2 j_n(k_4c) & \frac{d j_n(k_4c)}{d y} & 0 \\ 0 & 0 & 0 \end{bmatrix} , \quad x_2 = \begin{bmatrix} b_n \\ d_n^{(1)} \\ d_n^{(2)} \end{bmatrix} . \quad (A23) \]

These equations are solved by matrix inversion. Hence, the total solution in every region is known. The optical cross section can now be calculated by:

\[ Q_{\text{scat}} = \frac{2\pi}{k_4^2} \sum_{n=1}^{\infty} (2n+1) \left( |a_n|^2 + |b_n|^2 \right) , \quad (A24) \]

\[ Q_{\text{abs}} = \frac{2\pi}{k_4^2} \sum_{n=1}^{\infty} (2n+1) \left( |a_n|^2 + |b_n|^2 - \text{Re}(a_n + b_n) \right) , \quad (A25) \]

\[ Q_{\text{tot}} = \frac{2\pi}{k_4^2} \sum_{n=1}^{\infty} (2n+1) \text{Re}(a_n + b_n) , \quad (A26) \]

where \( a_n \) and \( b_n \) are the coefficients of the scattered wave as introduced in Eqs. (A13) and (A14). The wave vector \( k \) can be calculated from

\[ k_i^2 = \omega^2 \varepsilon_i \mu_i , \quad (A27) \]

with \( \varepsilon_i \) the permittivity and \( \mu_i \) the permeability of the \( i \)th region.

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