



# Transition probabilities and Franck-Condon factors for the second negative band system of O<sub>2</sub><sup>+</sup>

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# TRANSITION PROBABILITIES AND FRANCK-CONDON FACTORS FOR THE SECOND NEGATIVE BAND SYSTEM OF $O_2^+$

J. L. Fox

Institute for Atmospheric Sciences and Department of Mechanical Engineering  
State University of New York at Stony Brook

A. Dalgarno

Harvard-Smithsonian Center for Astrophysics, Cambridge

**Abstract.** Transition probabilities for the second negative band system of  $O_2^+$  are computed using the dipole transition moment presented by Wetmore et al. [1984]. Vibrational levels  $v'' = 0 - 54$  of the  $X^2\Pi_g$  ground state and  $v' = 0 - 33$  of the excited  $A^2\Pi_u$  state are included. Franck-Condon factors for ionization-excitation of  $O_2$  ( $X^3\Sigma_g^-; v = 0 - 25$ ) to  $O_2^+(A^2\Pi_u; v' = 0 - 33)$  are also presented.

## 1. Introduction

The second negative band system of  $O_2^+$  arises from the transition  $A^2\Pi_u(v') \rightarrow X^2\Pi_g(v'')$ . The excited electronic state  $A^2\Pi_u$  can be populated by photoionization and electron impact ionization of  $O_2$  and by fluorescent scattering of radiation by  $O_2^+(X^2\Pi_g)$  in planetary and cometary atmospheres. The latter process is a source of excitation of high vibrational levels ( $v > 5 - 7$ ) of ground state  $O_2^+$  in the atmospheres of the terrestrial planets [Fox, 1985, 1986]. Recently, James et al. [1988] and Schappe et al. [1988] have investigated the production of the second negative band system by electron impact on  $O_2$ . They have presented cross sections for production of specific bands within the system and for the system as a whole. Analysis of the emission spectrum requires Franck-Condon factors for the excitation-ionization of ground state  $O_2$  to produce  $O_2^+(A^2\Pi_u)$  and radiative transition probabilities for individual bands of the second negative system. Since transition probabilities were not available, both James et al. and Schappe et al. used Franck-Condon factors to compute the ratios of band intensities, a practice which is valid only if the transition moment is constant with internuclear distance. In addition, in computing the Franck-Condon factors, James et al. used a Morse potential, which is less accurate for high vibrational levels than a Rydberg-Klein-Rees (RKR) potential.

Several years ago, in connection with studies of the vibrational distribution of  $O_2^+$  in the dayside ionospheres of the terrestrial planets [Fox, 1985; 1986], we computed transition probabilities of the second negative band sys-

tem, using the *ab initio* dipole transition moment of Wetmore et al. [1984]. Wetmore et al. [1984] presented absorption oscillator strengths for the bands involving the first eight vibrational levels of the ground and excited states, and lifetimes of the  $O_2^+(A^2\Pi_u)$  state for  $v' = 0 - 33$ . The computed lifetimes agreed very well with the available measured values [Jeunehomme, 1966; Erman and Larsson, 1977; Fink and Welge, 1968]. We present here transition probabilities for vibrational levels  $v'' = 0$  to 54 of the ground state  $O_2^+(X^2\Pi_g)$  and  $v' = 0$  to 33 of  $O_2^+(A^2\Pi_u)$ . We also present Franck-Condon factors for ionization-excitation of  $O_2(X^3\Sigma_g^-; v = 0 - 25)$  to produce  $O_2^+(A^2\Pi_u; v' = 0 - 33)$ , a wider range of vibrational quantum numbers than previously available [Nicholls, 1965; Krupenie, 1972]. Many vibrational quanta are potentially important, because the equilibrium internuclear distance of the  $O_2^+(A^2\Pi_u)$  potential curve is very different from those of the  $O_2(X^3\Sigma_g^-)$  and  $O_2^+(X^2\Pi_g)$  states. Hence a wide range of vibrational levels of the *A* state are populated in ionization or fluorescent scattering; the excited states then decay to an even wider range of vibrational levels of the ground state.

## 2. Calculations and Results

We have constructed vibrational wave functions for the  $O_2^+(X^2\Pi_g)$ ,  $O_2^+(A^2\Pi_u)$  and  $O_2(X^3\Sigma_g^-)$  states by numerical integration of the radial equation of nuclear motion [cf. Wetmore et al. 1984]. Our potential curves for  $O_2^+$  were adopted from the RKR values of Krupenie [1972] extended to larger internuclear distances using the asymptotic polarization term  $-\frac{1}{2}\alpha R^{-4}$ , where  $\alpha = 5.28a_0^3$  is the polarizability of atomic oxygen. The potential curves for the ground state of  $O_2$  were taken from Allison et al. [1982]. The Franck-Condon factors for ionization-excitation of  $O_2(X^3\Sigma_g^-; v = 0 - 25)$  to  $O_2^+(A^2\Pi_u; v' = 0 - 33)$  are presented in Tables 1a - 1c. Our values for ionization-excitation from  $O_2(X^3\Sigma_g^-; v = 0)$  agree well with those presented by James et al. [1988].

Transition probabilities and band origins of the second negative system are given in Tables 2a - 2e for  $O_2^+(A^2\Pi_u, v' = 0 - 33)$  and  $O_2^+(X^2\Pi_g, v'' = 0 - 54)$ . Vibrational levels of the *X* state with  $v'' \geq 30$  lie above the lowest vibrational level of the *A* state, so some of the high vibrational levels of the *X* state decay radiatively to vibrational levels of the *A* state. The "reverse"  $X \rightarrow A$

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TABLE 1a. Franck-Condon Factors for Ionization of  $O_2(X^3\Sigma_g^-; v'' = 0-10)$  to  $O_2^+(A^2\Pi_u; v')$ 

$v'$	$v''$										
	0	1	2	3	4	5	6	7	8	9	10
0	3.058(-3)	2.087(-2)	6.692(-2)	1.344(-1)	1.900(-1)	2.016(-1)	1.674(-1)	1.117(-1)	6.107(-2)	2.778(-2)	1.062(-2)
1	1.291(-2)	6.225(-2)	1.253(-1)	1.295(-1)	5.880(-2)	1.670(-3)	2.929(-2)	1.064(-1)	1.541(-1)	1.420(-1)	9.572(-2)
2	2.994(-2)	9.849(-2)	1.108(-1)	3.397(-2)	3.490(-3)	6.622(-2)	9.167(-2)	3.378(-2)	6.845(-4)	5.173(-2)	1.228(-1)
3	5.071(-2)	1.084(-1)	5.246(-2)	6.114(-4)	5.785(-2)	6.538(-2)	5.169(-3)	2.669(-2)	8.182(-2)	5.235(-2)	1.651(-3)
4	7.032(-2)	9.103(-2)	8.519(-3)	3.121(-2)	6.362(-2)	5.861(-3)	2.837(-2)	6.533(-2)	1.432(-2)	1.325(-2)	7.128(-2)
5	8.489(-2)	5.968(-2)	1.400(-3)	5.759(-2)	2.210(-2)	1.215(-2)	5.691(-2)	1.122(-2)	1.865(-2)	6.072(-2)	1.702(-2)
6	9.260(-2)	2.923(-2)	1.864(-2)	5.033(-2)	6.671(-5)	4.365(-2)	2.341(-2)	8.473(-3)	5.152(-2)	1.097(-2)	1.737(-2)
7	9.356(-2)	8.749(-3)	3.863(-2)	2.484(-2)	1.225(-2)	4.216(-2)	3.341(-5)	3.978(-2)	1.927(-2)	9.868(-3)	4.793(-2)
8	8.904(-2)	4.194(-4)	4.806(-2)	4.809(-3)	3.237(-2)	1.728(-2)	1.423(-2)	3.508(-2)	3.231(-4)	3.957(-2)	1.282(-2)
9	8.075(-2)	1.844(-3)	4.485(-2)	3.029(-4)	3.859(-2)	9.443(-4)	3.283(-2)	9.288(-3)	1.959(-2)	2.697(-2)	2.758(-3)
10	7.022(-2)	8.815(-3)	3.356(-2)	7.765(-3)	2.935(-2)	3.803(-3)	3.154(-2)	2.259(-4)	3.303(-2)	2.801(-3)	2.581(-2)
11	5.888(-2)	1.723(-2)	2.036(-2)	1.851(-2)	1.473(-2)	1.579(-2)	1.655(-2)	1.059(-2)	2.267(-2)	3.792(-3)	2.979(-2)
12	4.824(-2)	2.441(-2)	9.733(-3)	2.610(-2)	3.990(-3)	2.455(-2)	3.691(-3)	2.224(-2)	6.376(-3)	1.806(-2)	1.290(-2)
13	3.894(-2)	2.926(-2)	3.170(-3)	2.850(-2)	6.031(-5)	2.554(-2)	3.644(-5)	2.430(-2)	3.757(-6)	2.427(-2)	7.691(-4)
14	3.103(-2)	3.155(-2)	3.465(-4)	2.643(-2)	1.494(-3)	2.052(-2)	3.618(-3)	1.800(-2)	3.894(-3)	1.859(-2)	2.514(-3)
15	2.461(-2)	3.180(-2)	1.677(-4)	2.188(-2)	5.441(-3)	1.338(-2)	9.482(-3)	9.455(-3)	1.094(-2)	8.826(-3)	1.052(-2)
16	1.944(-2)	3.051(-2)	1.453(-3)	1.654(-2)	9.533(-3)	7.007(-3)	1.396(-2)	3.089(-3)	1.549(-2)	1.968(-3)	1.596(-2)
17	1.537(-2)	2.830(-2)	3.283(-3)	1.160(-2)	1.251(-2)	2.721(-3)	1.574(-2)	2.672(-4)	1.601(-2)	2.729(-6)	1.604(-2)
18	1.217(-2)	2.562(-2)	5.068(-3)	7.586(-3)	1.399(-2)	5.658(-4)	1.512(-2)	2.776(-4)	1.356(-2)	1.490(-3)	1.241(-2)
19	9.660(-3)	2.275(-2)	6.496(-3)	4.622(-3)	1.415(-2)	8.599(-9)	1.302(-2)	1.770(-3)	9.876(-3)	4.200(-3)	7.732(-3)
20	7.697(-3)	1.993(-2)	7.456(-3)	2.605(-3)	1.337(-2)	3.647(-4)	1.035(-2)	3.602(-3)	6.321(-3)	6.556(-3)	3.849(-3)
21	6.158(-3)	1.727(-2)	7.953(-3)	1.333(-3)	1.203(-2)	1.118(-3)	7.729(-3)	5.103(-3)	3.556(-3)	7.896(-3)	1.400(-3)
22	4.941(-3)	1.484(-2)	8.043(-3)	5.954(-4)	1.045(-2)	1.903(-3)	5.490(-3)	6.012(-3)	1.716(-3)	8.196(-3)	2.590(-4)
23	3.973(-3)	1.263(-2)	7.808(-3)	2.125(-4)	8.835(-3)	2.527(-3)	3.739(-3)	6.327(-3)	6.649(-4)	7.727(-3)	1.219(-6)
24	3.198(-3)	1.067(-2)	7.333(-3)	4.675(-5)	7.317(-3)	2.916(-3)	2.457(-3)	6.174(-3)	1.694(-4)	6.820(-3)	1.991(-4)
25	2.572(-3)	8.944(-3)	6.696(-3)	8.700(-7)	5.962(-3)	3.070(-3)	1.567(-3)	5.705(-3)	9.462(-6)	5.743(-3)	5.420(-4)
26	2.064(-3)	7.424(-3)	5.961(-3)	1.147(-5)	4.793(-3)	3.024(-3)	9.738(-4)	5.058(-3)	1.831(-5)	4.672(-3)	8.512(-4)
27	1.648(-3)	6.096(-3)	5.180(-3)	4.056(-5)	3.806(-3)	2.827(-3)	5.925(-4)	4.337(-3)	8.813(-5)	3.702(-3)	1.049(-3)
28	1.305(-3)	4.942(-3)	4.395(-3)	6.791(-5)	2.987(-3)	2.530(-3)	3.549(-4)	3.615(-3)	1.592(-4)	2.875(-3)	1.122(-3)
29	1.023(-3)	3.946(-3)	3.640(-3)	5.500(-5)	2.316(-3)	2.179(-3)	2.105(-4)	2.938(-3)	2.056(-3)	2.195(-3)	1.090(-3)
30	7.917(-4)	3.099(-3)	2.941(-3)	9.030(-5)	1.771(-3)	1.812(-3)	1.245(-4)	2.331(-3)	2.216(-4)	1.652(-3)	9.854(-4)
31	6.033(-4)	2.389(-3)	2.318(-3)	8.597(-5)	1.336(-3)	1.458(-3)	7.400(-5)	1.808(-3)	2.125(-4)	1.226(-3)	8.409(-4)
32	4.522(-4)	1.807(-3)	1.783(-3)	7.549(-5)	9.922(-4)	1.139(-3)	4.446(-5)	1.371(-3)	1.873(-4)	8.975(-4)	6.843(-4)
33	3.331(-4)	1.339(-3)	1.338(-3)	6.224(-5)	7.253(-4)	8.643(-4)	2.712(-5)	1.018(-3)	1.547(-4)	6.483(-4)	5.347(-4)

Read 3.058(-3) as  $3.058 \times 10^{-3}$ .

TABLE 1b. Franck-Condon Factors for Ionization of  $O_2(X^3\Sigma_g^-; v'' = 11-21)$  to  $O_2^+(A^2\Pi_u; v')$ 

$v'$	$v''$											
	11	12	13	14	15	16	17	18	19	20	21	
0	3.438(-3)	9.476(-4)	2.229(-4)	4.479(-5)	7.679(-6)	1.118(-6)	1.378(-7)	1.420(-8)	1.199(-9)	8.528(-11)	4.381(-12)	
1	5.020(-2)	2.119(-2)	7.343(-3)	2.115(-3)	5.100(-4)	1.032(-4)	1.751(-5)	2.481(-6)	2.917(-7)	2.786(-8)	2.180(-9)	
2	1.424(-1)	1.098(-1)	6.264(-2)	2.788(-2)	9.966(-3)	2.906(-3)	6.979(-4)	1.384(-4)	2.262(-5)	3.034(-6)	3.280(-7)	
3	2.973(-2)	1.030(-1)	1.374(-1)	1.138(-1)	6.747(-2)	3.055(-2)	1.092(-2)	3.136(-3)	7.308(-4)	1.383(-4)	2.120(-5)	
4	5.735(-2)	4.217(-3)	2.258(-2)	9.485(-2)	1.338(-1)	1.130(-1)	6.708(-2)	2.996(-2)	1.043(-2)	2.878(-3)	6.338(-4)	
5	9.973(-3)	6.637(-2)	5.592(-2)	4.134(-3)	2.284(-2)	9.507(-2)	1.322(-1)	1.093(-1)	6.298(-2)	2.703(-2)	8.937(-3)	
6	5.711(-2)	1.483(-2)	1.130(-2)	6.578(-2)	5.081(-2)	2.165(-3)	2.834(-2)	1.011(-1)	1.317(-1)	1.031(-1)	5.610(-2)	
7	7.541(-3)	2.058(-2)	5.387(-2)	9.950(-3)	1.606(-2)	6.721(-2)	4.263(-2)	2.269(-4)	3.893(-2)	1.110(-1)	1.304(-1)	
8	1.436(-2)	4.417(-2)	3.260(-3)	2.684(-2)	4.928(-2)	4.444(-3)	2.425(-2)	6.821(-2)	3.168(-2)	8.008(-4)	5.491(-2)	
9	3.923(-2)	6.131(-3)	2.119(-2)	3.844(-2)	3.255(-4)	3.483(-2)	4.195(-2)	5.703(-4)	3.551(-2)	6.619(-2)	1.905(-2)	
10	1.756(-2)	8.151(-3)	3.633(-2)	1.297(-3)	2.888(-2)	2.997(-2)	7.314(-4)	4.235(-2)	3.158(-2)	6.872(-4)	4.803(-2)	
11	2.500(-5)	2.999(-2)	8.640(-2)	1.551(-2)	3.012(-2)	9.363(-5)	3.503(-2)	1.984(-2)	5.327(-3)	4.684(-2)	1.977(-2)	
12	1.043(-2)	2.304(-2)	1.717(-3)	3.045(-2)	2.439(-3)	2.281(-2)	2.179(-2)	2.928(-3)	3.788(-2)	1.039(-2)	1.333(-2)	
13	2.306(-2)	4.846(-3)	1.739(-2)	1.473(-2)	6.728(-3)	2.723(-2)	2.649(-5)	2.821(-2)	1.315(-2)	8.884(-3)	3.694(-2)	
14	2.116(-2)	4.894(-4)	2.362(-2)	5.742(-4)	2.208(-2)	7.259(-3)	1.298(-2)	2.137(-2)	1.328(-3)	3.042(-2)	5.994(-3)	
15	1.069(-2)	8.213(-3)	1.482(-2)	4.116(-3)	2.031(-2)	3.309(-4)	2.356(-2)	2.247(-3)	1.858(-2)	1.461(-2)	5.310(-3)	
16	2.263(-3)	1.561(-2)	4.033(-3)	1.361(-2)	8.147(-3)	9.080(-3)	1.503(-2)	2.907(-3)	2.209(-2)	1.200(-4)	2.227(-2)	
17	3.230(-5)	1.656(-2)	7.085(-6)	1.714(-2)	5.593(-4)	1.663(-2)	3.235(-3)	1.337(-2)	9.638(-3)	6.748(-3)	1.871(-2)	
18	2.283(-3)	1.244(-2)	2.187(-3)	1.361(-2)	1.233(-3)	1.552(-2)	1.259(-4)	1.707(-2)	6.510(-4)	1.608(-2)	5.246(-3)	
19	5.780(-3)	6.976(-3)	6.335(-3)	7.498(-3)	5.752(-3)	9.315(-3)	3.985(-3)	1.234(-2)	1.528(-3)	1.570(-2)	3.514(-6)	
20	8.355(-3)	2.766(-3)	9.292(-3)	2.655(-3)	9.460(-3)	3.468(-3)	8.678(-3)	5.491(-3)	6.697(-3)	8.982(-3)	3.596(-3)	
21	9.324(-3)	5.651(-4)	1.010(-2)	3.437(-4)	1.057(-2)	4.734(-4)	1.073(-2)	1.125(-3)	1.028(-2)	2.824(-3)	8.671(-3)	
22	8.928(-3)	1.188(-7)	9.199(-3)	7.624(-5)	9.498(-3)	8.835(-5)	9.981(-3)	4.759(-6)	1.054(-2)	1.666(-4)	1.073(-2)	
23	7.723(-3)	3.564(-4)	7.436(-3)	8.460(-4)	7.368(-3)	1.060(-3)	7.722(-3)	8.634(-4)	8.543(-3)	3.788(-4)	9.631(-3)	
24	6.224(-3)	1.024(-3)	5.516(-3)	1.832(-3)	5.125(-3)	2.289(-3)	5.212(-3)	2.263(-3)	5.856(-3)	1.768(-3)	7.031(-3)	
25	4.769(-3)	1.631(-3)	3.836(-3)	2.589(-3)	3.268(-3)	3.188(-3)	3.143(-3)	3.354(-3)	3.506(-3)	3.086(-3)	4.391(-3)	
26	3.522(-3)	2.020(-3)	2.539(-3)	2.976(-3)	1.935(-3)	3.594(-3)	1.710(-3)	3.869(-3)	1.854(-3)	3.823(-3)	2.397(-3)	
27	2.535(-3)	2.165(-3)	1.619(-3)	3.021(-3)	1.074(-3)	3.572(-3)	8.390(-4)	3.867(-3)	8.617(-4)	3.956(-3)	1.146(-3)	
28	1.792(-3)	2.109(-3)	1.005(-3)	2.819(-3)	5.611(-4)	3.265(-3)	3.667(-4)	3.524(-3)	3.428(-4)	3.666(-3)	4.708(-4)	
29	1.253(-3)	1.916(-3)	6.130(-4)	2.475(-3)	2.773(-4)	2.810(-3)	1.386(-4)	3.012(-3)	1.089(-4)	3.156(-3)	1.575(-4)	
30	8.699(-4)	1.649(-3)	3.710(-4)	2.070(-3)	1.302(-4)	2.310(-3)	4.229(-5)	2.455(-3)	2.267(-5)	2.577(-3)	3.681(-5)	
31	6.016(-4)	1.356(-3)	2.246(-4)	1.665(-3)	5.846(-5)	1.831(-3)	8.635(-6)	1.929(-3)	1.047(-6)	2.023(-3)	3.113(-6)	
32	4.152(-4)	1.073(-3)	1.371(-4)	1.296(-3)	2.529(-5)	1.407(-3)	4.562(-7)	1.471(-3)	1.554(-6)	1.539(-3)	7.709(-7)	
33	2.558(-4)	8.220(-4)	8.478(-5)	9.791(-4)	1.067(-5)	1.053(-3)	4.203(-7)	1.094(-3)	6.087(-6)	1.142(-3)	5.430(-6)	

TABLE 1c. Franck-Condon Factors for Ionization of  $O_2(X^3\Sigma_g^-; v'' = 22-25)$  to  $O_2^+(A^2\Pi_u; v')$ 

$v'$	$v''$			
	22	23	24	25
0	1.734(-13)	1.402(-14)	1.358(-15)	1.458(-15)
1	1.301(-10)	5.255(-12)	3.902(-13)	2.301(-14)
2	2.842(-8)	1.915(-9)	8.125(-11)	5.250(-12)
3	2.597(-6)	2.497(-7)	1.865(-8)	9.033(-10)
4	1.114(-4)	1.547(-5)	1.660(-6)	1.365(-7)
5	2.308(-3)	4.675(-4)	7.378(-5)	8.873(-6)
6	2.258(-2)	6.909(-3)	1.624(-3)	2.926(-4)
7	9.406(-2)	4.720(-2)	1.737(-2)	4.786(-3)
8	1.224(-1)	1.266(-1)	8.221(-2)	3.720(-2)
9	6.715(-3)	7.602(-2)	1.330(-1)	1.193(-1)
10	5.900(-2)	7.356(-3)	2.053(-2)	1.016(-1)
11	6.192(-3)	5.850(-2)	4.635(-2)	4.604(-4)
12	4.703(-2)	9.229(-3)	1.657(-2)	6.410(-2)
13	3.429(-3)	2.321(-2)	4.265(-2)	1.985(-3)
14	1.634(-2)	3.251(-2)	1.707(-4)	3.272(-2)
15	2.951(-2)	1.487(-3)	2.373(-2)	2.542(-2)
16	8.420(-3)	1.061(-2)	2.612(-2)	1.064(-7)
17	4.815(-4)	2.378(-2)	3.776(-3)	1.602(-2)
18	1.057(-2)	1.456(-2)	2.530(-3)	2.333(-2)
19	1.708(-2)	2.260(-3)	1.369(-2)	1.046(-2)
20	1.343(-2)	6.014(-4)	1.683(-2)	6.189(-4)
21	6.132(-3)	5.578(-3)	1.097(-2)	1.808(-3)
22	1.245(-3)	9.781(-3)	4.001(-3)	7.144(-3)
23	6.771(-6)	1.044(-2)	4.421(-4)	1.021(-2)
24	9.526(-4)	8.500(-3)	1.820(-4)	9.795(-3)
25	2.404(-3)	5.760(-3)	1.414(-3)	7.443(-3)
26	3.440(-3)	3.381(-3)	2.696(-3)	4.808(-3)
27	3.830(-3)	1.747(-3)	3.422(-3)	2.736(-3)
28	3.697(-3)	7.957(-4)	3.551(-3)	1.396(-3)
29	3.259(-3)	3.133(-4)	3.269(-3)	6.430(-4)
30	2.698(-3)	1.015(-4)	2.780(-3)	2.668(-4)
31	2.134(-3)	2.358(-5)	2.238(-3)	9.849(-5)
32	1.631(-3)	2.278(-6)	1.731(-3)	3.133(-5)
33	1.213(-3)	2.267(-7)	1.296(-3)	7.972(-6)

transitions are indicated by negative band origins and transition probabilities. For strong bands with fairly low vibrational quantum number, intensity ratios computed with our transition probabilities agree to within a few percent with those computed with the Franck-Condon factors of James et al. [1988] and Schappe et al. [1988]. Significant differences arise for weaker bands and higher vibrational levels.

TABLE 2a. Transition Probabilities ( $s^{-1}$ ) (Upper Entry) and Band Origins (nm) (Lower Entry) of the Second Negative Band System of  $O_2^+(A; v' \rightarrow X; v'' = 0-10)$ 

$v'$	$v''$										
	0	1	2	3	4	5	6	7	8	9	10
0	7.400(0) 249.56	1.238(2) 261.80	9.789(2) 275.05	4.867(3) 289.43	1.707(4) 305.11	4.487(4) 322.24	9.179(4) 341.03	1.497(5) 361.74	1.990(5) 384.70	2.210(5) 410.25	2.069(5) 438.67
1	6.164(1) 244.25	8.958(2) 255.96	6.021(3) 268.61	2.474(4) 282.32	6.913(4) 297.21	1.376(5) 313.44	1.979(5) 331.19	2.017(5) 350.69	1.353(5) 372.23	4.590(4) 396.10	5.126(2) 422.53
2	2.736(2) 239.32	3.453(3) 250.55	1.967(4) 262.66	6.621(4) 275.75	1.444(5) 289.94	2.077(5) 305.36	1.879(5) 322.19	8.728(4) 340.61	5.956(3) 360.89	2.124(4) 383.29	8.561(4) 407.99
3	8.608(2) 234.73	9.436(3) 245.53	4.535(4) 257.14	1.236(5) 269.68	2.042(5) 283.23	1.961(5) 297.94	8.541(4) 313.93	1.885(3) 331.40	3.827(4) 350.56	9.808(4) 371.65	6.650(4) 394.83
4	2.155(3) 230.46	2.051(4) 240.86	8.279(4) 252.03	1.800(5) 264.05	2.154(5) 277.04	1.180(5) 291.09	7.607(3) 306.34	3.332(4) 322.95	1.001(5) 341.12	5.931(4) 361.06	4.857(2) 382.89
5	4.570(3) 226.48	3.774(4) 236.51	1.272(5) 247.28	2.161(5) 258.84	1.743(5) 271.31	3.624(4) 284.77	1.249(4) 299.35	9.408(4) 315.19	7.345(4) 332.47	2.056(3) 351.39	3.712(4) 372.04
6	8.528(3) 222.78	6.108(4) 232.47	1.707(5) 242.86	2.203(5) 254.01	1.052(5) 266.00	4.608(2) 278.93	6.506(4) 292.90	9.753(4) 308.05	1.449(4) 324.54	2.205(4) 342.54	7.010(4) 362.13
7	1.436(4) 219.31	8.918(4) 228.71	2.049(5) 238.75	1.930(5) 249.52	4.114(4) 261.08	1.700(4) 273.53	1.029(5) 286.95	5.055(4) 301.47	3.050(3) 317.25	6.470(4) 334.43	3.748(4) 353.08

8	2.222( 4) 216.09	1.196( 5) 225.20	2.235( 5) 234.93	1.448( 5) 245.35	5.139( 3) 256.52	5.924( 4) 268.52	9.689( 4) 281.45	7.834( 3) 295.41	3.722( 4) 310.54	6.367( 4) 326.98	2.108( 3) 344.78
9	3.196( 4) 213.08	1.490( 5) 221.93	2.237( 5) 231.38	9.063( 4) 241.48	2.755( 3) 252.29	9.469( 4) 263.89	5.952( 4) 276.36	2.804( 3) 289.81	6.821( 4) 304.36	2.812( 4) 320.13	1.042( 4) 337.18
10	4.300( 4) 210.28	1.736( 5) 218.89	2.064( 5) 228.08	4.401( 4) 237.89	2.467( 4) 248.37	1.046( 5) 259.61	2.051( 4) 271.67	2.789( 4) 284.65	6.616( 4) 298.68	2.000( 3) 313.85	3.946( 4) 330.22
11	5.428( 4) 207.69	1.901( 5) 216.09	1.759( 5) 225.04	1.354( 4) 234.58	5.473( 4) 244.77	8.897( 4) 255.68	1.142( 3) 267.37	5.586( 4) 279.93	3.943( 4) 293.48	5.461( 3) 308.13	5.104( 4) 323.89
12	6.507( 4) 205.31	1.981( 5) 213.52	1.400( 5) 222.25	8.530( 2) 231.56	7.940( 4) 241.48	6.054( 4) 252.09	4.220( 3) 263.44	6.752( 4) 275.64	1.250( 4) 288.76	2.589( 4) 302.93	3.802( 4) 318.15
13	7.479( 4) 203.13	1.985( 5) 211.17	1.044( 5) 219.70	2.207( 3) 228.79	9.224( 4) 238.47	3.227( 4) 248.81	2.041( 4) 259.87	6.065( 4) 271.72	3.973( 2) 284.47	4.301( 4) 298.21	1.662( 4) 312.94
14	8.263( 4) 201.14	1.917( 5) 209.01	7.284( 4) 217.37	1.203( 4) 226.26	9.246( 4) 235.73	1.193( 4) 245.82	3.843( 4) 256.61	4.291( 4) 268.16	3.754( 3) 280.57	4.662( 4) 293.93	2.533( 3) 308.24
15	8.854( 4) 199.32	1.803( 5) 207.05	4.746( 4) 215.25	2.510( 4) 223.96	8.352( 4) 233.23	1.815( 3) 243.11	5.102( 4) 253.65	2.394( 4) 264.94	1.527( 4) 277.04	3.847( 4) 290.05	5.540( 2) 303.98
16	9.216( 4) 197.66	1.653( 5) 205.26	2.852( 4) 213.31	3.755( 4) 221.87	6.938( 4) 230.96	2.505( 2) 240.65	5.564( 4) 250.98	9.657( 3) 262.02	2.713( 4) 273.85	2.517( 4) 286.56	6.892( 3) 300.14
17	9.371( 4) 196.16	1.488( 5) 203.63	1.551( 4) 211.56	4.729( 4) 219.97	5.386( 4) 228.91	4.081( 3) 238.42	5.337( 4) 248.55	1.987( 3) 259.38	3.478( 4) 270.97	1.283( 4) 283.40	1.552( 4) 296.68
18	9.331( 4) 194.79	1.319( 5) 202.17	7.314( 3) 209.98	5.348( 4) 218.26	3.940( 4) 227.06	1.023( 4) 236.41	4.665( 4) 246.37	5.961( 0) 257.00	3.707( 4) 268.38	4.520( 3) 280.57	2.216( 4) 293.58
19	9.112( 4) 193.57	1.152( 5) 200.85	2.710( 3) 208.55	5.615( 4) 216.72	2.727( 4) 225.39	1.642( 4) 234.60	3.792( 4) 244.41	1.679( 3) 254.87	3.495( 4) 266.05	6.301( 2) 278.03	2.512( 4) 290.80
20	8.748( 4) 192.46	9.960( 4) 199.66	5.805( 2) 207.27	5.590( 4) 215.34	1.790( 4) 223.90	2.137( 4) 232.99	2.910( 4) 242.66	4.995( 3) 252.96	3.020( 4) 263.98	1.116( 2) 275.76	2.472( 4) 288.32
21	8.269( 4) 191.48	8.533( 4) 198.60	1.740( 0) 206.13	5.348( 4) 214.11	1.113( 4) 222.57	2.457( 4) 231.55	2.128( 4) 241.09	8.483( 3) 251.26	2.444( 4) 262.13	1.511( 3) 273.74	2.206( 4) 286.12
22	7.695( 4) 190.61	7.249( 4) 197.66	2.788( 2) 205.12	4.956( 4) 213.02	6.515( 3) 221.39	2.598( 4) 230.27	1.493( 4) 239.71	1.129( 4) 249.76	1.878( 4) 260.49	3.591( 3) 271.96	1.833( 4) 284.17
23	7.052( 4) 189.84	6.109( 4) 196.83	9.265( 2) 204.23	4.475( 4) 212.06	3.554( 3) 220.35	2.588( 4) 229.15	1.009( 4) 238.49	1.307( 4) 248.44	1.384( 4) 259.06	5.536( 3) 270.40	1.443( 4) 282.46
24	6.364( 4) 189.16	5.108( 4) 196.11	1.633( 3) 203.45	3.953( 4) 211.22	1.775( 3) 219.44	2.462( 4) 228.17	6.603( 3) 237.43	1.381( 4) 247.29	9.868( 3) 257.80	6.937( 3) 269.03	1.090( 4) 280.97
25	5.653( 4) 188.58	4.238( 4) 195.48	2.218( 3) 202.77	3.426( 4) 210.49	7.860( 2) 218.66	2.258( 4) 227.32	4.196( 3) 236.51	1.365( 4) 246.29	6.856( 3) 256.72	7.671( 3) 267.85	7.983( 3) 279.69
26	4.938( 4) 188.08	3.485( 4) 194.94	2.599( 3) 202.20	2.917( 4) 209.87	2.886( 2) 217.99	2.009( 4) 226.59	2.599( 3) 235.73	1.284( 4) 245.44	4.667( 3) 255.79	7.790( 3) 266.85	5.708( 3) 278.59
27	4.236( 4) 187.66	2.837( 4) 194.49	2.757( 3) 201.71	2.441( 4) 209.34	7.431( 1) 217.42	1.738( 4) 225.98	1.575( 3) 235.06	1.158( 4) 244.72	3.131( 3) 255.01	7.422( 3) 265.99	4.013( 3) 277.66
28	3.563( 4) 187.30	2.282( 4) 194.11	2.714( 3) 201.30	2.006( 4) 208.90	6.457( 0) 216.94	1.467( 4) 225.46	9.378( 2) 234.51	1.007( 4) 244.12	2.080( 3) 254.36	6.721( 3) 265.29	2.789( 3) 276.89

TABLE 2a. (continued)

$v'$	$v''$										
	0	1	2	3	4	5	6	7	8	9	10
29	2.933( 4) 187.01	1.810( 4) 193.80	2.513( 3) 200.97	1.618( 4) 208.54	2.672( 0) 216.56	1.207( 4) 225.05	5.523( 2) 234.05	8.484( 3) 243.63	1.375( 3) 253.83	5.829( 3) 264.71	1.924( 3) 276.26
30	2.361( 4) 186.78	1.413( 4) 193.55	2.209( 3) 200.70	1.280( 4) 208.25	1.831( 1) 216.24	9.692( 3) 224.71	3.238( 2) 233.69	6.933( 3) 243.23	9.082( 2) 253.40	4.867( 3) 264.24	1.322( 3) 275.75
31	1.856( 4) 186.60	1.084( 4) 193.35	1.855( 3) 200.48	9.916( 3) 208.02	3.297( 1) 216.00	7.597( 3) 224.44	1.905( 2) 233.40	5.506( 3) 242.92	6.013( 2) 253.06	3.926( 3) 263.87	9.073( 2) 275.35
32	1.425( 4) 186.46	8.168( 3) 193.20	1.495( 3) 200.32	7.525( 3) 207.85	4.017( 1) 215.81	5.815( 3) 224.24	1.132( 2) 233.18	4.255( 3) 242.68	3.998( 2) 252.80	3.069( 3) 263.59	6.223( 2) 275.04
33	1.069( 4) 186.35	6.038( 3) 193.09	1.162( 3) 200.20	5.593( 3) 207.71	4.017( 1) 215.66	4.349( 3) 224.09	6.835( 1) 233.01	3.205( 3) 242.50	2.669( 2) 252.61	2.331( 3) 263.38	4.265( 2) 274.81

TABLE 2b. Transition Probabilities ( $s^{-1}$ ) (Upper Entry) and Band Origins (nm) (Lower Entry) of the Second Negative Band System of  $O_2^+(A; v' \rightarrow X; v'' = 11 - 21)$ 

$v'$	$v''$										
	11	12	13	14	15	16	17	18	19	20	21
0	1.578(5) 470.40	9.855(4) 506.49	5.397(4) 547.59	2.463(4) 594.15	9.084(3) 648.20	2.693(3) 710.50	5.916(2) 783.98	1.048(2) 870.78	1.488(1) 976.00	1.303(0) 1104.22	3.903(-2) 1266.05
1	2.518(4) 451.89	8.078(4) 485.09	1.168(5) 522.66	1.081(5) 564.92	7.217(4) 613.56	3.700(4) 669.10	1.400(4) 733.87	4.005(3) 809.39	8.197(2) 899.53	1.266(2) 1007.35	1.407(1) 1140.31
2	9.454(4) 435.29	3.858(4) 466.01	3.956(2) 500.58	2.384(4) 539.21	7.269(4) 583.36	9.214(4) 633.34	6.991(4) 691.08	3.650(4) 757.65	1.311(4) 836.07	3.371(3) 928.43	6.018(2) 1040.23
3	4.607(3) 420.35	1.990(4) 448.93	6.693(4) 480.93	5.296(4) 516.47	6.899(3) 556.83	9.905(3) 602.20	5.556(4) 654.16	8.001(4) 713.50	6.087(4) 782.64	2.929(4) 863.00	9.273(3) 958.78
4	3.763(4) 406.85	6.720(4) 433.56	2.180(4) 463.33	3.130(3) 496.24	4.425(4) 533.38	4.794(4) 574.87	7.118(3) 622.03	1.004(4) 675.45	5.505(4) 737.10	7.238(4) 807.95	4.867(4) 891.31
5	6.715(4) 394.61	1.342(4) 419.69	1.114(4) 447.53	5.104(4) 478.15	2.442(4) 512.54	1.258(3) 550.73	3.709(4) 593.87	3.811(4) 642.38	2.336(3) 697.88	1.848(4) 761.08	6.197(4) 834.60
6	1.881(4) 383.48	1.001(4) 407.13	5.162(4) 433.27	1.882(4) 461.91	5.380(3) 493.93	4.092(4) 529.30	1.782(4) 569.03	3.410(3) 613.41	3.787(4) 663.82	2.459(4) 720.74	2.779(2) 786.35
7	2.549(3) 373.34	4.893(4) 395.72	2.489(4) 420.37	3.617(3) 447.28	3.973(4) 477.24	1.447(4) 510.17	6.993(3) 546.98	3.563(4) 587.87	7.569(3) 634.01	1.131(4) 685.74	3.738(4) 744.87
8	3.618(4) 364.08	3.974(4) 385.33	5.682(1) 408.67	3.549(4) 434.05	2.024(4) 462.21	4.075(3) 493.04	3.335(4) 527.34	6.064(3) 565.23	1.395(4) 607.76	2.793(4) 655.14	2.287(2) 708.90
9	5.290(4) 355.62	6.388(3) 375.86	2.229(4) 398.03	3.276(4) 422.08	9.478(1) 448.65	3.018(4) 477.64	1.122(4) 509.76	8.977(3) 545.09	2.634(4) 584.54	1.487(2) 628.23	2.351(4) 677.50
10	3.143(4)	3.631(3)	4.055(4)	5.647(3)	1.888(4)	2.295(4)	1.675(3)	2.702(4)	2.411(3)	1.732(4)	1.388(4)

11	347.89	367.24	388.37	411.23	436.41	463.80	494.02	527.13	563.93	604.49	649.98
	5.363( 3)	2.574( 4)	2.654( 4)	2.737( 3)	3.145( 4)	2.021( 3)	2.011( 4)	1.174( 4)	7.352( 3)	1.954( 4)	5.950( 2)
	340.86	359.42	379.64	401.45	425.42	451.40	479.98	511.17	545.71	583.60	625.88
12	1.346( 3)	3.888( 4)	5.318( 3)	2.018( 4)	1.823( 4)	4.668( 3)	2.347( 4)	7.959( 0)	2.100( 4)	2.233( 3)	1.537( 4)
	334.51	352.36	371.78	392.67	415.57	440.33	467.48	497.02	529.61	565.23	604.80
13	1.505( 4)	3.150( 4)	6.639( 2)	2.995( 4)	2.487( 3)	1.913( 4)	9.115( 3)	9.269( 3)	1.388( 4)	3.424( 3)	1.619( 4)
	328.76	345.99	364.69	384.77	406.74	430.42	456.33	484.44	515.34	549.01	586.26
14	2.965( 4)	1.482( 4)	1.077( 4)	2.322( 4)	1.442( 3)	2.309( 4)	1.269( 2)	1.873( 4)	1.833( 3)	1.419( 4)	3.873( 3)
	323.57	340.24	358.31	377.68	398.82	421.56	446.39	473.25	502.70	534.68	569.95
15	3.474( 4)	2.734( 3)	2.221( 4)	1.009( 4)	1.064( 4)	1.483( 4)	4.036( 3)	1.582( 4)	1.290( 3)	1.502( 4)	3.647( 2)
	318.88	335.07	352.58	371.31	391.72	413.64	437.51	463.29	491.48	522.00	555.57
16	2.994( 4)	2.036( 2)	2.624( 4)	1.427( 3)	1.873( 4)	4.702( 3)	1.226( 4)	6.729( 3)	8.319( 3)	7.281( 3)	6.382( 3)
	314.66	330.41	347.42	365.60	385.37	406.57	429.61	454.43	481.52	510.78	542.88
17	2.031( 4)	4.657( 3)	2.258( 4)	4.246( 2)	2.012( 4)	1.246( 2)	1.627( 4)	7.339( 2)	1.323( 4)	9.994( 2)	1.144( 4)
	310.86	326.22	342.80	360.48	379.69	400.25	422.56	446.55	472.68	500.85	531.68
18	1.079( 4)	1.124( 4)	1.519( 4)	4.424( 3)	1.591( 4)	1.465( 3)	1.443( 4)	5.502( 2)	1.249( 4)	3.853( 2)	1.079( 4)
	307.46	322.48	338.66	355.91	374.62	394.62	416.29	439.55	464.85	492.07	521.79
19	4.102( 3)	1.638( 4)	7.961( 3)	9.473( 3)	9.733( 3)	5.500( 3)	9.506( 3)	3.785( 3)	8.254( 3)	3.381( 3)	6.624( 3)
	304.41	319.12	334.96	351.83	370.11	389.61	410.72	433.35	457.92	484.31	513.07
20	7.539( 2)	1.871( 4)	2.970( 3)	1.301( 4)	4.481( 3)	9.176( 3)	4.641( 3)	7.229( 3)	3.824( 3)	6.573( 3)	2.551( 3)
	301.69	316.14	331.68	348.21	366.10	385.17	405.79	427.87	451.80	477.46	505.40
21	1.227( 1)	1.842( 4)	5.276( 2)	1.426( 4)	1.308( 3)	1.105( 4)	1.460( 3)	9.125( 3)	1.014( 3)	8.114( 3)	3.761( 2)
	299.28	313.49	328.77	345.00	362.55	381.25	401.44	423.03	446.41	471.45	498.67
22	7.825( 2)	1.640( 4)	1.141( 1)	1.359( 4)	8.732( 1)	1.108( 4)	1.325( 2)	9.235( 3)	2.724( 1)	7.870( 3)	5.233( 1)
	297.15	311.16	326.20	342.17	359.43	377.80	397.62	418.79	441.69	466.19	492.79
23	2.120( 3)	1.359( 4)	5.700( 2)	1.176( 4)	1.488( 2)	9.839( 3)	1.029( 2)	8.119( 3)	2.565( 2)	6.527( 3)	7.528( 2)
	295.29	309.11	323.95	339.70	356.70	374.79	394.28	415.09	437.58	461.61	487.67
24	3.403( 3)	1.066( 4)	1.498( 3)	9.512( 3)	7.977( 2)	8.036( 3)	6.918( 2)	6.471( 3)	9.868( 2)	4.838( 3)	1.689( 3)
	293.66	307.33	321.99	337.55	354.33	372.17	391.39	411.88	434.02	457.65	483.25
25	4.321( 3)	8.045( 3)	2.353( 3)	7.316( 3)	1.539( 3)	6.176( 3)	1.393( 3)	4.801( 3)	1.718( 3)	3.290( 3)	2.408( 3)
	292.25	305.79	320.31	335.69	352.29	369.92	388.90	409.13	430.96	454.25	479.46
26	4.783( 3)	5.891( 3)	2.927( 3)	5.423( 3)	2.106( 3)	4.540( 3)	1.932( 3)	3.379( 3)	2.212( 3)	2.088( 3)	2.761( 3)
	291.05	304.48	318.86	334.11	350.55	368.00	386.78	406.78	428.35	451.35	476.24
27	4.826( 3)	4.222( 3)	3.174( 3)	3.915( 3)	2.407( 3)	3.233( 3)	2.215( 3)	2.287( 3)	2.414( 3)	1.252( 3)	2.782( 3)
	290.04	303.37	317.65	332.78	349.08	366.38	384.99	404.80	426.16	448.93	473.53
28	4.546( 3)	2.982( 3)	3.134( 3)	2.774( 3)	2.453( 3)	2.251( 3)	2.255( 3)	1.506( 3)	2.369( 3)	7.165( 2)	2.571( 3)
	289.20	302.45	316.64	331.67	347.86	365.04	383.51	403.17	424.35	446.91	471.29
29	4.054( 3)	2.085( 3)	2.886( 3)	1.941( 3)	2.305( 3)	1.545( 3)	2.112( 3)	9.741( 2)	2.157( 3)	3.954( 2)	2.232( 3)
	288.51	301.69	315.81	330.76	346.86	363.94	382.30	401.83	422.86	445.27	469.46
30	3.453( 3)	1.449( 3)	2.513( 3)	1.348( 3)	2.033( 3)	1.052( 3)	1.856( 3)	6.249( 2)	1.853( 3)	2.127( 2)	1.848( 3)
	287.96	301.09	315.15	330.04	346.06	363.06	381.33	400.76	421.68	443.95	468.00



TABLE 2b. (continued)

$v'$	$v''$										
	11	12	13	14	15	16	17	18	19	20	21
31	2.825(3)	1.004(3)	2.089(3)	9.324(2)	1.704(3)	7.138(2)	1.549(3)	4.003(2)	1.521(3)	1.128(2)	1.472(3)
	287.52	300.61	314.63	329.46	345.44	362.37	380.56	399.91	420.74	442.91	466.85
32	2.231(3)	6.935(2)	1.668(3)	6.432(2)	1.368(3)	4.839(2)	1.240(3)	2.575(2)	1.201(3)	5.981(1)	1.136(3)
	287.19	300.24	314.23	329.02	344.95	361.84	379.97	399.26	420.02	442.12	465.97
33	1.707(3)	4.781(2)	1.286(3)	4.426(2)	1.059(3)	3.281(2)	9.569(2)	1.668(2)	9.171(2)	3.209(1)	8.527(2)
	286.93	299.97	313.92	328.69	344.59	361.44	379.53	398.77	419.48	441.52	465.30

TABLE 2c. Transition Probabilities ( $s^{-1}$ ) (Upper Entry) and Band Origins (nm) (Lower Entry) of the Second Negative Band System of  $O_2^+(A; v' \rightarrow X; v'' = 22 - 32)$ 

$v'$	$v''$										
	22	23	24	25	26	27	28	29	30	31	32
0	8.752(-3)	1.238(-3)	9.630(-4)	5.098(-5)	5.827(-5)	3.616(-5)	1.132(-6)	1.414(-11)	-1.749(-6)	-1.268(-5)	-7.481(-6)
	1473.53	1751.05	2140.65	2721.98	3690.37	5615.77	11244.16	318425.22	-12580.88	-6299.33	-4261.07
1	8.919(-1)	3.207(-2)	3.711(-3)	1.592(-5)	4.886(-5)	5.946(-5)	6.406(-6)	5.099(-8)	7.058(-10)	-7.327(-7)	-1.996(-6)
	1305.93	1519.34	1804.27	2200.34	2792.75	3771.24	5680.86	11082.14	131421.33	-13956.31	-6775.61
2	7.335(1)	5.811(0)	2.762(-1)	7.898(-3)	7.929(-5)	7.241(-7)	1.350(-7)	9.518(-8)	5.563(-9)	8.965(-13)	-2.468(-9)
	1176.31	1346.69	1565.88	1855.79	2260.15	2860.87	3840.11	5726.91	10870.97	78574.06	-15820.48
3	1.977(3)	2.807(2)	2.431(1)	1.336(0)	4.425(-2)	1.045(-4)	4.256(-5)	1.655(-6)	5.861(-6)	1.108(-6)	2.404(-9)
	1073.22	1213.26	1388.34	1611.56	1907.99	2319.08	2923.37	3902.03	5758.69	10594.41	54190.63
4	1.959(4)	5.068(3)	8.254(2)	8.303(1)	4.869(0)	1.745(-1)	1.580(-3)	2.551(-6)	2.655(-5)	8.595(-6)	4.229(-7)
	989.39	1107.21	1251.20	1429.67	1658.21	1960.19	2375.19	2983.08	3958.86	5769.13	10266.90
5	6.331(4)	3.400(4)	1.062(4)	2.043(3)	2.353(2)	1.531(1)	5.531(-1)	8.991(-3)	2.123(-5)	7.170(-6)	3.070(-7)
	920.00	1021.03	1142.25	1289.16	1472.12	1705.36	2011.05	2430.39	3041.07	4006.89	5759.25
6	3.546(4)	6.693(4)	4.907(4)	1.931(4)	4.392(3)	5.732(2)	4.252(1)	1.668(0)	2.830(-2)	3.656(-4)	1.317(-6)
	861.71	949.73	1053.75	1177.55	1328.34	1515.35	1752.00	2061.93	2485.36	3095.07	4045.98
7	8.371(3)	1.035(4)	5.585(4)	6.121(4)	3.090(4)	8.350(3)	1.265(3)	1.058(2)	4.651(0)	9.202(-2)	1.734(-3)
	812.15	889.88	980.57	1086.90	1214.12	1368.49	1558.60	1799.19	2113.37	2538.60	3144.84
8	2.488(4)	2.624(4)	3.194(1)	3.526(4)	6.629(4)	4.397(4)	1.448(4)	2.566(3)	2.429(2)	1.231(1)	3.428(-1)
	769.57	839.02	919.18	1011.98	1121.38	1251.80	1409.01	1602.76	1847.41	2164.33	2590.00
9	1.337(4)	5.486(3)	3.287(4)	6.724(3)	1.434(4)	6.129(4)	5.675(4)	2.325(4)	4.848(3)	5.384(2)	3.329(1)
	732.70	795.38	867.07	949.17	1044.78	1157.09	1290.15	1450.73	1648.31	1896.02	2214.91
10	4.558(3)	2.502(4)	6.325(2)	2.283(4)	2.110(4)	1.581(3)	4.697(4)	6.651(4)	3.478(4)	8.807(3)	1.195(3)
	700.62	757.72	822.50	896.02	980.74	1079.06	1193.89	1330.13	1494.37	1695.16	1945.60
11	2.165(4)	1.562(3)	1.766(4)	1.149(4)	6.835(3)	3.000(4)	1.876(3)	2.684(4)	6.897(4)	4.853(4)	1.553(4)
	672.71	725.18	784.29	850.87	926.90	1014.24	1115.05	1233.00	1372.86	1540.49	1744.57
12	7.218(3)	9.100(3)	1.364(4)	3.205(3)	2.129(4)	2.154(1)	2.574(4)	1.371(4)	7.900(3)	5.981(4)	6.157(4)
	648.41	697.02	751.46	812.36	881.39	960.00	1049.84	1153.76	1275.33	1418.75	1590.05

13	7.385(2) 627.16	1.714(4) 672.52	2.558(0) 723.06	1.745(4) 779.28	1.295(3) 842.58	1.687(4) 914.14	7.340(3) 995.23	1.169(4) 1088.14	2.738(4) 1195.64	6.729(-1) 1320.81	3.936(4) 1468.05
14	1.088(4) 608.53	5.741(3) 651.15	8.692(3) 698.41	7.802(3) 750.72	6.820(3) 809.29	1.122(4) 875.09	4.411(3) 949.12	1.828(4) 1033.26	7.122(2) 1129.71	2.997(4) 1240.81	7.996(3) 1369.89
15	1.401(4) 592.16	8.719(1) 632.44	1.360(4) 676.94	1.106(1) 725.97	1.402(4) 780.60	1.196(1) 841.64	1.541(4) 909.90	3.749(2) 986.95	1.843(4) 1074.57	3.852(3) 1174.62	1.759(4) 1289.65
16	7.010(3) 577.77	5.659(3) 616.05	6.536(3) 658.19	5.713(3) 704.45	6.291(3) 755.78	6.319(3) 812.85	6.575(3) 876.35	7.023(3) 947.59	8.662(3) 1028.09	7.053(3) 1119.30	1.629(4) 1223.27
17	8.163(2) 565.09	1.062(4) 601.66	4.414(2) 641.79	1.048(4) 685.70	1.351(2) 734.23	1.096(4) 787.99	3.201(0) 847.51	1.210(4) 913.97	2.781(1) 988.63	1.499(4) 1072.68	5.472(0) 1167.80
18	5.767(2) 553.93	9.366(3) 589.03	1.154(3) 627.44	8.008(3) 669.34	2.185(3) 715.51	6.731(3) 766.46	3.733(3) 822.66	5.663(3) 885.13	5.873(3) 954.98	5.289(3) 1033.18	8.273(3) 1121.14
19	3.820(3) 544.12	4.851(3) 577.94	4.888(3) 614.88	3.020(3) 655.06	6.304(3) 699.22	1.401(3) 747.79	7.825(3) 801.20	3.455(2) 860.34	9.419(3) 926.17	5.344(-1) 999.55	1.159(4) 1081.65
20	6.708(3) 535.50	1.230(3) 568.23	7.191(3) 603.89	2.410(2) 642.61	7.483(3) 685.05	5.435(1) 731.61	7.172(3) 782.65	9.651(2) 838.98	6.229(3) 901.47	3.087(3) 970.84	5.232(3) 1048.11
21	7.542(3) 527.95	5.538(0) 559.73	6.906(3) 594.31	3.367(2) 631.77	5.747(3) 672.74	1.674(3) 717.59	3.929(3) 766.63	3.807(3) 820.60	1.901(3) 880.28	6.380(3) 946.31	4.545(2) 1019.58
22	6.596(3) 521.36	5.630(2) 552.33	5.061(3) 585.97	1.792(3) 622.35	3.147(3) 662.08	3.631(3) 705.47	1.193(3) 752.81	5.355(3) 804.79	5.563(1) 862.12	6.268(3) 925.35	4.905(2) 995.28
23	4.844(3) 515.64	1.743(3) 545.91	2.975(3) 578.75	3.159(3) 614.22	1.170(3) 652.88	4.529(3) 695.04	6.687(1) 740.94	4.996(3) 791.24	4.425(2) 846.58	4.101(3) 907.47	2.466(3) 974.64
24	3.097(3) 510.70	2.737(3) 540.38	1.395(3) 572.54	3.815(3) 607.22	2.048(2) 644.98	4.315(3) 686.09	1.587(2) 730.78	3.634(3) 779.66	1.562(3) 833.35	1.905(3) 892.28	3.832(3) 957.13
25	1.747(3) 506.46	3.239(3) 535.64	4.802(2) 567.22	3.778(3) 601.25	2.682(0) 638.24	3.488(3) 678.47	7.224(2) 722.14	2.193(3) 769.84	2.404(3) 822.13	5.697(2) 879.44	3.983(3) 942.38
26	8.677(2) 502.87	3.275(3) 531.63	8.720(1) 562.72	3.312(3) 596.19	1.740(2) 632.55	2.523(3) 672.04	1.247(3) 714.86	1.120(3) 761.57	2.687(3) 812.71	5.697(1) 868.67	3.347(3) 930.01
27	3.709(2) 499.86	2.995(3) 528.26	1.585(-2) 558.95	2.679(3) 591.96	4.289(2) 627.78	1.687(3) 666.67	1.534(3) 708.79	4.782(2) 754.68	2.530(3) 804.87	1.988(1) 859.71	2.467(3) 919.75
28	1.286(2) 497.36	2.559(3) 525.47	4.484(1) 555.83	2.053(3) 588.46	6.206(2) 623.85	1.067(3) 662.24	1.581(3) 703.78	1.604(2) 749.00	2.146(3) 798.41	1.537(2) 852.35	1.670(3) 911.34
29	3.060(1) 495.33	2.083(3) 523.20	1.170(2) 553.29	1.517(3) 585.61	7.064(2) 620.65	6.491(2) 658.63	1.459(3) 699.71	3.468(1) 744.40	1.701(3) 793.18	2.887(2) 846.40	1.071(3) 904.53
30	2.342(0) 493.70	1.635(3) 521.38	1.690(2) 551.26	1.094(3) 583.34	6.986(2) 618.10	3.862(2) 655.75	1.251(3) 696.46	1.544(0) 740.72	1.290(3) 789.01	3.631(2) 841.65	6.645(2) 899.11
31	1.057(0) 492.42	1.247(3) 519.96	1.890(2) 549.66	7.764(2) 581.55	6.287(2) 616.09	2.277(2) 653.50	1.017(3) 693.92	2.859(0) 737.85	9.499(2) 785.75	3.743(2) 837.94	4.064(2) 894.88
32	6.248(0) 491.43	9.297(2) 518.86	1.821(2) 548.44	5.451(2) 580.18	5.283(2) 614.55	1.347(2) 651.77	7.931(2) 691.97	1.116(1) 735.64	6.849(2) 783.25	3.418(2) 835.09	2.481(2) 891.63
33	1.025(1) 490.69	6.795(2) 518.03	1.590(2) 547.51	3.796(2) 579.15	4.210(2) 613.39	8.058(1) 650.46	5.987(2) 690.50	1.673(1) 733.98	4.864(2) 781.36	2.872(2) 832.95	1.527(2) 889.19

TABLE 2d. Transition Probabilities ( $s^{-1}$ ) (Upper Entry) and Band Origins (nm) (Lower Entry) of the Second Negative Band System of  $O_2^+(A; v' \rightarrow X; v'' = 33 - 43)$

$v'$	$v''$											
	33	34	35	36	37	38	39	40	41	42	43	
0	-6.373(-6)	-9.087(-5)	-1.948(-4)	-1.629(-4)	-3.337(-5)	-2.065(-5)	-2.154(-4)	-4.667(-4)	-5.583(-4)	-4.224(-4)	-1.802(-4)	
	-3251.42	-2649.11	-2250.17	-1967.22	-1756.32	-1593.18	-1463.45	-1358.13	-1271.17	-1198.36	-1136.64	
1	-2.145(-7)	-1.952(-5)	-6.500(-5)	-7.752(-5)	-3.030(-5)	-9.555(-7)	-7.139(-5)	-2.105(-4)	-3.029(-4)	-2.700(-4)	-1.434(-4)	
	-4535.91	-3443.63	-2798.63	-2373.96	-2073.50	-1849.86	-1677.23	-1540.33	-1429.43	-1338.01	-1261.53	
2	-2.782(-8)	-2.631(-8)	-2.382(-9)	-1.247(-7)	-3.210(-7)	-3.275(-7)	-1.354(-7)	-1.483(-9)	-9.217(-8)	-3.220(-7)	-4.983(-7)	
	-7348.41	-4854.08	-3663.84	-2968.61	-2513.21	-2192.01	-1953.73	-1770.43	-1625.48	-1508.30	-1411.81	
3	-4.061(-9)	-1.162(-6)	-7.058(-6)	-1.132(-5)	-4.723(-6)	-7.027(-7)	-2.157(-5)	-6.240(-5)	-9.050(-5)	-8.046(-5)	-4.089(-5)	
	-18375.19	-8041.85	-5228.06	-3918.56	-3162.21	-2669.95	-2324.61	-2069.66	-1874.28	-1720.18	-1595.79	
4	4.175(-10)	-6.128(-8)	-1.575(-6)	-4.369(-6)	-2.680(-6)	-1.898(-7)	-1.218(-5)	-4.061(-5)	-6.405(-5)	-6.066(-5)	-3.291(-5)	
	40773.41	-22025.20	-8902.46	-5673.80	-4214.29	-3383.04	-2847.12	-2473.87	-2199.78	-1990.49	-1825.81	
5	7.496(-10)	2.876(-9)	-6.922(-9)	-7.008(-8)	-3.990(-8)	-1.945(-8)	-4.323(-7)	-1.505(-6)	-2.742(-6)	-3.076(-6)	-2.053(-6)	
	9924.65	32434.99	-27704.63	-9998.49	-6209.08	-4558.75	-3636.38	-3048.86	-2643.00	-2346.56	-2121.03	
6	5.756(-8)	2.818(-7)	2.154(-8)	-2.994(-9)	-1.277(-8)	-1.345(-8)	-4.982(-7)	-2.494(-6)	-5.542(-6)	-6.679(-6)	-4.250(-6)	
	5737.75	9582.59	26716.59	-37749.84	-11424.73	-6857.14	-4963.42	-3929.79	-3280.49	-2835.83	-2512.92	
7	7.573(-5)	1.328(-6)	6.757(-7)	8.838(-8)	-1.375(-9)	-1.716(-8)	-9.948(-7)	-3.851(-6)	-6.735(-6)	-7.596(-6)	-5.266(-6)	
	4079.86	5708.47	9237.67	22556.91	-59855.28	-13331.38	-7653.94	-5445.31	-4273.31	-3548.51	-3056.97	
8	8.681(-3)	3.413(-4)	1.339(-5)	5.485(-9)	1.093(-9)	-1.180(-11)	-5.945(-9)	-7.322(-7)	-3.377(-6)	-3.933(-6)	-1.312(-6)	
	3192.59	4110.20	5669.86	8892.76	19450.83	-145088.95	-15991.56	-8656.09	-6028.03	-4679.68	-3860.97	
9	1.291(0)	3.820(-2)	3.625(-4)	3.743(-5)	3.678(-7)	3.044(-7)	1.200(-11)	-6.273(-9)	-1.564(-7)	-2.433(-9)	-1.180(-6)	
	2641.23	3239.57	4136.39	5623.14	8561.84	17095.96	350548.81	-19944.17	-9949.65	-6742.91	-5164.85	
10	9.282(1)	4.510(0)	1.298(-1)	4.294(-4)	2.694(-6)	1.441(-5)	6.386(-8)	1.908(-9)	-2.565(-8)	-5.704(-8)	-1.423(-6)	
	2267.03	2694.13	3286.76	4160.93	5577.51	8265.31	15302.95	80943.88	-26307.57	-11653.68	-7626.46	
11	2.622(3)	2.535(2)	1.461(1)	4.476(-1)	4.003(-3)	9.455(-5)	1.473(-5)	2.316(-6)	6.957(-9)	-4.037(-9)	-1.839(-7)	
	1998.67	2323.40	2751.20	3338.25	4192.55	5548.94	8027.37	13970.16	47136.37	-37618.19	-13909.08	
12	2.568(4)	5.445(3)	6.518(2)	4.554(1)	1.698(0)	2.903(-2)	5.581(-4)	1.057(-5)	2.776(-6)	6.639(-8)	-1.336(-10)	
	1798.44	2057.16	2385.60	2814.83	3398.79	4238.75	5547.00	7856.38	13000.68	34339.36	-61760.88	
13	6.835(4)	3.869(4)	1.052(4)	1.581(3)	1.363(2)	6.348(0)	1.587(-1)	3.020(-3)	9.835(-6)	1.117(-6)	1.705(-7)	
	1643.93	1857.46	2121.14	2453.84	2886.12	3470.04	4300.32	5569.54	7741.02	12287.42	27722.72	
14	1.541(4)	6.318(4)	5.202(4)	1.870(4)	3.581(3)	3.852(2)	2.280(1)	7.557(-1)	1.544(-2)	6.718(-5)	1.191(-9)	
	1521.81	1703.04	1922.12	2191.36	2529.73	2967.40	3554.24	4379.02	5618.12	7680.64	11780.65	
15	2.418(4)	8.478(2)	4.413(4)	6.014(4)	2.985(4)	7.418(3)	1.010(3)	7.641(1)	3.287(0)	7.990(-2)	5.849(-4)	
	1423.43	1580.77	1767.80	1993.00	2269.03	2614.98	3060.24	3652.59	4476.02	5694.29	7674.47	
16	2.616(3)	3.154(4)	4.765(3)	1.857(4)	5.672(4)	4.162(4)	1.382(4)	2.428(3)	2.369(2)	1.313(1)	3.971(-1)	
	1342.99	1482.19	1645.41	1838.81	2071.28	2355.78	2711.15	3166.01	3766.64	4593.67	5801.20	

17	2.021( 4) 1276.43	2.182( 3) 1401.53	2.055( 4) 1546.60	2.097( 4) 1716.27	1.463( 3) 1917.11	3.929( 4) 2158.36	4.867( 4) 2452.94	2.264( 4) 2819.43	5.267( 3) 3286.06	6.702( 2) 3898.37	4.800( 1) 4734.74
18	7.360( 3) 1220.89	8.993( 3) 1334.85	1.520( 4) 1465.80	3.489( 3) 1617.33	2.942( 4) 1794.49	3.957( 3) 2004.18	1.543( 4) 2255.72	4.481( 4) 2561.97	3.164( 4) 2941.54	1.009( 4) 3422.78	1.699( 3) 4051.08
19	1.427( 2) 1174.21	1.536( 4) 1279.25	1.200( 1) 1399.02	2.027( 4) 1536.42	2.041( 3) 1695.42	1.819( 4) 1881.39	1.882( 4) 2101.37	7.307( 2) 2364.69	2.867( 4) 2684.41	3.600( 4) 3079.54	1.662( 4) 3578.96
20	5.978( 3) 1134.79	5.175( 3) 1232.60	8.590( 3) 1343.42	7.534( 3) 1469.62	8.098( 3) 1614.44	1.502( 4) 1782.20	2.057( 3) 1978.38	2.433( 4) 2210.08	4.721( 3) 2486.91	8.877( 3) 2822.41	3.070( 4) 3236.30
21	9.016( 3) 1101.41	2.861( 0) 1193.32	1.182( 4) 1296.90	4.202( 1) 1414.12	1.509( 4) 1547.72	7.742( 1) 1701.23	1.737( 4) 1879.11	3.336( 3) 2086.92	1.170( 4) 2332.04	1.682( 4) 2624.59	2.252( 0) 2978.86
22	6.282( 3) 1073.12	2.494( 3) 1160.18	5.941( 3) 1257.85	5.005( 3) 1367.83	6.451( 3) 1492.43	6.236( 3) 1634.67	9.102( 3) 1798.23	4.283( 3) 1987.63	1.452( 4) 2208.75	1.936( 2) 2469.46	1.663( 4) 2780.60
23	2.444( 3) 1049.15	5.505( 3) 1132.22	9.644( 2) 1225.05	8.520( 3) 1329.13	3.034( 2) 1446.48	1.100( 4) 1579.70	2.713( 2) 1731.93	1.246( 4) 1906.95	1.274( 3) 2109.56	1.106( 4) 2346.13	5.827( 3) 2625.21
24	3.614( 2) 1028.90	5.890( 3) 1108.67	8.056( 1) 1197.53	6.980( 3) 1296.79	1.065( 3) 1408.26	7.527( 3) 1534.23	2.168( 3) 1677.43	8.371( 3) 1841.08	2.042( 3) 2029.25	2.012( 4) 2247.22	5.060( 2) 2501.99
25	2.951( 1) 1011.87	4.460( 3) 1088.92	1.281( 3) 1174.51	3.712( 3) 1269.84	3.671( 3) 1376.54	2.663( 3) 1496.66	5.954( 3) 1632.61	2.075( 3) 1787.24	7.084( 3) 1964.03	2.440( 3) 2167.51	6.415( 3) 2403.58
26	4.901( 2) 997.63	2.691( 3) 1072.44	2.482( 3) 1155.37	1.303( 3) 1247.50	4.878( 3) 1350.32	2.984( 2) 1465.72	6.650( 3) 1595.86	4.253( 0) 1743.29	7.529( 3) 1911.09	1.035( 1) 2103.21	7.822( 3) 2324.77
27	1.015( 3) 985.83	1.353( 3) 1058.83	2.953( 3) 1139.58	2.247( 2) 1229.11	4.526( 3) 1328.80	7.463( 1) 1440.40	5.089( 3) 1565.89	7.870( 2) 1707.59	4.934( 3) 1868.27	1.482( 3) 2051.47	4.791( 3) 2261.71
28	1.312( 3) 976.17	5.682( 2) 1047.69	2.803( 3) 1126.69	2.311(-1) 1214.13	3.473( 3) 1311.31	6.250( 2) 1419.86	3.118( 3) 1541.66	1.967( 3) 1678.81	2.339( 3) 1833.87	3.067( 3) 2010.07	1.802( 3) 2211.49
29	1.362( 3) 968.36	1.914( 2) 1038.70	2.344( 3) 1116.30	1.107( 2) 1202.07	2.385( 3) 1297.26	1.121( 3) 1403.40	1.641( 3) 1522.27	2.533( 3) 1655.85	8.155( 2) 1806.51	3.509( 3) 1977.24	3.557( 2) 2171.82
30	1.247( 3) 962.15	4.480( 1) 1031.56	1.816( 3) 1108.06	2.620( 2) 1192.52	1.535( 3) 1286.14	1.325( 3) 1390.40	7.691( 2) 1506.99	2.492( 3) 1637.78	1.825( 2) 1785.02	3.117( 3) 1951.53	3.763( 0) 2140.84
31	1.051( 3) 957.31	3.841( 0) 1025.99	1.344( 3) 1101.63	3.488( 2) 1185.08	9.545( 2) 1277.49	1.285( 3) 1380.30	3.279( 2) 1495.13	2.127( 3) 1623.78	1.124( 1) 1768.41	2.428( 3) 1931.69	7.253( 1) 2116.99
32	8.382( 2) 953.59	8.666(-1) 1021.73	9.654( 2) 1096.72	3.629( 2) 1179.40	5.862( 2) 1270.89	1.111( 3) 1372.60	1.287( 2) 1486.09	1.673( 3) 1613.13	7.909( 0) 1755.78	1.762( 3) 1916.63	1.961( 2) 2098.91
33	6.408( 2) 950.81	6.287( 0) 1018.53	6.808( 2) 1093.03	3.283( 2) 1175.14	3.606( 2) 1265.94	8.917( 2) 1366.83	4.671( 1) 1479.33	1.251( 3) 1605.17	3.713( 1) 1746.35	1.229( 3) 1905.40	2.600( 2) 2085.45

TABLE 2e. Transition Probabilities ( $s^{-1}$ ) (Upper Entry) and Band Origins (nm) (Lower Entry) of the Second Negative Band System of  $O_2^+(A; v' \rightarrow X; v'' = 44 - 54)$

$v'$	$v''$										
	44	45	46	47	48	49	50	51	52	53	54
0	-1.602(-5) -1083.78	-3.433(-5) -1038.14	-2.144(-4) -998.47	-4.565(-4) -963.80	-6.538(-4) -933.38	-7.420(-4) -906.60	-7.110(-4) -882.95	-5.915(-4) -862.03	-4.310(-4) -843.51	-2.727(-4) -827.10	-1.449(-4) -812.57
1	-2.690(-5) -1196.75	-6.239(-6) -1141.34	-9.527(-5) -1093.57	-2.449(-4) -1052.12	-3.852(-4) -1015.98	-4.644(-4) -984.32	-4.651(-4) -956.51	-4.010(-4) -932.01	-3.013(-4) -910.39	-1.966(-4) -891.30	-1.083(-4) -874.45
2	-5.097(-7) -1331.17	-3.789(-7) -1262.97	-2.004(-7) -1204.73	-6.155(-8) -1154.62	-2.341(-9) -1111.24	-1.680(-8) -1073.48	-7.483(-8) -1040.48	-1.436(-7) -1011.56	-1.997(-7) -986.14	-2.323(-7) -963.78	-2.405(-7) -944.11
3	-5.793(-6) -1493.53	-4.658(-6) -1408.20	-4.232(-5) -1336.19	-1.008(-4) -1274.83	-1.543(-4) -1222.15	-1.834(-4) -1176.63	-1.819(-4) -1137.10	-1.551(-4) -1102.64	-1.150(-4) -1072.51	-7.338(-5) -1046.12	-3.890(-5) -1022.98
4	-5.467(-6) -1693.17	-2.823(-6) -1584.34	-3.134(-5) -1493.76	-7.845(-5) -1417.49	-1.236(-4) -1352.65	-1.503(-4) -1297.12	-1.519(-4) -1249.25	-1.320(-4) -1207.78	-9.981(-5) -1171.72	-6.518(-5) -1140.29	-3.566(-5) -1112.86
5	-5.474(-7) -1944.10	-3.303(-8) -1801.99	-1.328(-6) -1685.72	-4.043(-6) -1589.22	-6.995(-6) -1508.18	-9.014(-6) -1439.46	-9.513(-6) -1380.74	-8.581(-6) -1330.26	-6.745(-6) -1286.65	-4.634(-6) -1248.85	-2.742(-6) -1216.02
6	-7.795(-7) -2268.34	-4.415(-7) -2077.20	-5.088(-6) -1924.22	-1.313(-5) -1799.48	-2.107(-5) -1696.27	-2.574(-5) -1609.84	-2.574(-5) -1536.75	-2.168(-5) -1474.48	-1.545(-5) -1421.09	-9.127(-6) -1375.12	-4.168(-6) -1335.42
7	-1.192(-6) -2702.49	-5.399(-7) -2435.48	-7.912(-6) -2227.82	-2.209(-5) -2062.32	-3.687(-5) -1927.88	-4.610(-5) -1817.00	-4.725(-5) -1724.43	-4.144(-5) -1646.40	-3.168(-5) -1580.12	-2.105(-5) -1523.49	-1.183(-5) -1474.92
8	-9.891(-10) -3312.24	-1.003(-6) -2919.90	-2.914(-6) -2626.39	-5.530(-6) -2399.39	-9.419(-6) -2219.33	-1.444(-5) -2073.66	-1.906(-5) -1953.96	-2.109(-5) -1854.37	-1.942(-5) -1770.71	-1.476(-5) -1699.90	-9.071(-6) -1639.65
9	-2.360(-6) -4227.89	-6.621(-7) -3608.92	-3.517(-7) -3170.93	-3.168(-6) -2845.86	-4.705(-6) -2596.04	-3.070(-6) -2398.92	-8.071(-7) -2240.16	-1.674(-9) -2110.24	-2.840(-7) -2002.57	-5.380(-7) -1912.47	-3.828(-7) -1836.55
10	-1.684(-6) -5746.12	-4.010(-12) -4659.89	-3.547(-6) -3954.58	-1.011(-5) -3461.48	-1.085(-5) -3098.78	-5.756(-6) -2821.99	-1.159(-6) -2604.83	-1.221(-8) -2430.80	-7.133(-7) -2289.04	-1.157(-6) -2172.08	-8.585(-7) -2074.66
11	-1.300(-7) -8710.54	-5.070(-8) -6436.23	-3.098(-7) -5164.11	-8.754(-10) -4354.14	-1.573(-6) -3795.35	-7.383(-6) -3388.31	-1.419(-5) -3080.00	-1.667(-5) -2839.62	-1.345(-5) -2648.04	-7.449(-6) -2492.76	-2.406(-6) -2365.30
12	-1.193(-7) -16920.63	-8.401(-7) -10033.47	-1.020(-6) -7249.52	-3.838(-7) -5748.36	-6.109(-8) -4812.87	-8.717(-8) -4176.61	-6.397(-7) -3717.87	-2.308(-6) -3373.19	-4.610(-6) -3106.22	-6.119(-6) -2894.71	-5.930(-6) -2724.24
13	-3.285(-10) -146274.03	-2.808(-9) -21095.53	-5.723(-7) -11671.71	-2.335(-6) -8216.95	-2.869(-6) -6430.32	-1.339(-6) -5342.86	-9.058(-8) -4614.50	-1.658(-7) -4095.13	-4.995(-7) -3708.22	-3.551(-7) -3410.70	-5.090(-8) -3176.50
14	1.275(-7) 23822.59	3.499(-12) 709202.75	-1.461(-8) -27126.87	-6.828(-9) -13720.03	-4.799(-7) -9372.08	-1.741(-6) -7227.92	-2.391(-6) -5956.12	-1.518(-6) -5118.25	-2.956(-7) -4527.80	-5.129(-8) -4091.96	-7.035(-7) -3759.41
15	3.474(-6) 11442.42	1.337(-7) 21355.11	9.034(-10) 116913.39	-1.923(-8) -36404.70	-6.775(-8) -16317.81	-6.054(-9) -10760.18	-1.551(-7) -8164.76	-8.929(-7) -6668.36	-1.724(-6) -5699.93	-1.821(-6) -5026.03	-1.123(-6) -4533.47
16	4.790(-3) 7723.79	3.791(-5) 11248.19	2.168(-7) 19751.39	4.871(-9) 68460.21	-9.605(-9) -52065.08	-9.177(-8) -19662.11	-1.185(-7) -12437.58	-3.158(-8) -9269.05	-2.217(-8) -7498.24	-2.839(-7) -6373.97	-7.566(-7) -5602.06

17	1.858( 0)	3.306(-2)	3.103(-4)	6.932(-7)	7.290(-9)	-2.701(-9)	-8.065(-8)	-1.949(-7)	-1.907(-7)	-7.523(-8)	-6.092(-14)
	5941.88	7829.02	11178.67	18714.76	50968.40	-83108.18	-24053.06	-14480.33	-10577.77	-8470.16	-7159.28
18	1.585( 2)	7.977( 0)	1.965(-1)	2.306(-3)	6.316(-6)	1.736(-9)	-3.042(-10)	-4.807(-8)	-1.661(-7)	-2.138(-7)	-1.422(-7)
	4903.40	6120.96	7993.66	11226.26	18095.25	42353.85	-168587.34	-29925.69	-16979.43	-12133.22	-9612.08
19	3.794( 3)	4.669( 2)	3.087( 1)	1.029( 0)	1.583(-2)	6.989(-5)	3.748(-8)	-6.648(-13)	-1.758(-8)	-9.418(-8)	-1.740(-7)
	4228.28	5103.71	6342.67	8220.99	11386.13	17801.95	37549.71	-1172204.18	-37976.91	-20058.04	-13991.34
20	2.259( 4)	7.270( 3)	1.205( 3)	1.060( 2)	4.753( 0)	9.871(-2)	6.879(-4)	1.179(-6)	4.732(-11)	-5.635(-9)	-3.533(-8)
	3758.17	4434.20	5340.57	6612.73	8517.18	11660.81	17788.82	34806.08	307511.56	-49330.05	-23872.58
21	1.641( 4)	2.382( 4)	1.156( 4)	2.667( 3)	3.174( 2)	1.923( 1)	5.485(-1)	5.818(-3)	1.747(-5)	1.230(-9)	-3.575(-9)
	3415.41	3964.73	4673.99	5620.26	6938.96	8891.94	12059.95	18039.26	33382.34	155462.33	-65854.36
22	6.314( 3)	2.884( 3)	1.737( 4)	1.452( 4)	4.910( 3)	8.114( 2)	6.730( 1)	2.645( 0)	4.164(-2)	1.868(-4)	2.359(-8)
	3157.30	3621.09	4203.70	4953.84	5950.62	7331.52	9358.47	12599.13	18555.67	32929.01	114273.79
23	4.304( 3)	1.330( 4)	7.397( 2)	6.514( 3)	1.321( 4)	7.198( 3)	1.723( 3)	1.999( 2)	1.097( 1)	2.488(-1)	1.638(-3)
	2958.46	3361.95	3858.43	4481.28	5281.60	6341.80	7803.85	9934.70	13301.65	19359.17	33291.56
24	1.153( 4)	6.189( 2)	7.845( 3)	6.850( 3)	1.611( 2)	7.241( 3)	7.836( 3)	2.921( 3)	4.905( 2)	3.815( 1)	1.238( 0)
	2802.89	3162.48	3597.99	4133.75	4805.45	5667.50	6807.24	8373.95	10645.17	14201.37	20492.52
25	4.202( 3)	3.598( 3)	7.145( 3)	2.572( 2)	7.475( 3)	2.183( 3)	1.238( 3)	5.540( 3)	3.723( 3)	9.580( 2)	1.084( 2)
	2679.98	3006.88	3397.93	3871.85	4455.12	5186.49	6124.96	7364.76	9065.93	11523.45	15346.34
26	1.977( 1)	7.398( 3)	6.163( 2)	5.322( 3)	2.760( 3)	1.514( 3)	4.808( 3)	2.948( 2)	1.777( 3)	3.209( 3)	1.412( 3)
	2582.36	2884.54	3242.53	3671.35	4191.72	4832.95	5637.91	6671.72	8038.09	9912.36	12615.64
27	1.484( 3)	4.986( 3)	7.718( 2)	5.223( 3)	3.525( 1)	4.511( 3)	5.572( 2)	2.041( 3)	2.234( 3)	4.383( 0)	1.479( 3)
	2504.79	2788.09	3121.15	3516.52	3991.08	4568.17	5280.84	6177.44	7331.34	8859.19	10957.75
28	3.416( 3)	1.707( 3)	2.965( 3)	2.029( 3)	1.838( 3)	2.568( 3)	5.230( 2)	2.692( 3)	1.154( 1)	1.632( 3)	7.285( 2)
	2443.34	2712.17	3026.31	3396.59	3837.31	4367.84	5014.94	5816.67	6828.69	8135.54	9871.67
29	3.824( 3)	2.087( 2)	3.613( 3)	2.531( 2)	2.968( 3)	4.913( 2)	1.936( 3)	9.046( 2)	7.806( 2)	1.201( 3)	5.754( 1)
	2395.01	2652.74	2952.52	3303.91	3719.43	4215.75	4815.49	5550.04	6464.12	7623.31	9127.49
30	3.195( 3)	1.995( 1)	2.974( 3)	2.781( 1)	2.597( 3)	1.142( 0)	2.068( 3)	4.155( 1)	1.380( 3)	2.103( 2)	6.493( 2)
	2357.39	2606.67	2895.55	3232.74	3629.49	4100.57	4665.78	5352.12	6197.20	7254.81	8604.21
31	2.305( 3)	2.409( 2)	2.026( 3)	3.070( 2)	1.738( 3)	2.277( 2)	1.453( 3)	8.840( 1)	1.129( 3)	4.890( 0)	7.531( 2)
	2328.50	2571.39	2852.09	3178.66	3561.45	4013.94	4553.95	5205.48	6001.44	6987.97	8231.43
32	1.543( 3)	4.285( 2)	1.255( 3)	5.296( 2)	1.017( 3)	4.656( 2)	8.354( 2)	3.016( 2)	6.754( 2)	1.359( 2)	5.045( 2)
	2306.65	2544.77	2819.38	3138.08	3510.59	3949.45	4471.12	5097.54	5858.43	6794.83	7964.74
33	9.974( 2)	4.879( 2)	7.462( 2)	5.876( 2)	5.588( 2)	5.410( 2)	4.354( 2)	3.999( 2)	3.466( 2)	2.392( 2)	2.653( 2)
	2290.41	2525.02	2795.14	3108.09	3473.10	3902.06	4410.49	5018.87	5754.76	6655.76	7774.34

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A. Dalgarno, Harvard-Smithsonian Center for Astrophysics, Cambridge, MA 02138

J. L. Fox, Department of Mechanical Engineering, State University of New York at Stony Brook, Stony Brook, NY 11794.

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