The Case for a 700+ GeV WIMP: Cosmic Ray Spectra from PAMELA, Fermi and ATIC

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Abstract

Multiple lines of evidence indicate an anomalous injection of high-energy $e^+e^-$ in the Galactic halo. The recent $e^+$ fraction spectrum from the Payload for Antimatter Matter Exploration and Light-nuclei Astrophysics (PAMELA) shows a sharp rise up to 100 GeV. The Fermi Gamma-ray Space Telescope has found a significant hardening of the $e^+e^-$ cosmic ray spectrum above 100 GeV, with a break, confirmed by HESS at around 1 TeV. The Advanced Thin Ionization Calorimeter (ATIC) has also observed a similar excess, falling back to the expected spectrum at 1 TeV and above. Excess microwaves towards the galactic center in the WMAP data are consistent with hard synchrotron radiation from a population of 10-100 GeV $e^+e^-$ (the WMAP “Haze”). We argue that dark matter annihilations can provide a consistent explanation of all of these data, focusing on dominantly leptonic modes, either directly or through a new light boson. Normalizing the signal to the highest energy evidence (Fermi and HESS), we find that similar cross sections provide good fits to PAMELA and the Haze, and that both the required cross section and annihilation modes are achievable in models with Sommerfeld-enhanced annihilation. These models naturally predict significant production of gamma rays in the galactic center via a variety of mechanisms. Most notably, there is a robust inverse-Compton scattered (ICS) gamma-ray signal arising from the energetic electrons and positrons, detectable at Fermi/GLAST energies, which should provide smoking gun evidence for this production.
I. INTRODUCTION

The search for astrophysical signatures of WIMP annihilation has blossomed in recent months with tantalizing announcements of electron and positron cosmic-ray spectra by three projects. Unexpected features in such spectra are of great interest for particle physics, because of the possibility that WIMP annihilation products could be observed this way.

The first project, ATIC, has measured the spectrum of $e^+ + e^-$ (ATIC cannot distinguish $e^+$ from $e^-$) from 20 to 2000 GeV, finding a hard spectrum ($\sim E^{-3}$) concluding with a broad bump at 300 – 800 GeV \[1\]. ATIC discriminates protons from electrons by comparing the shapes of the hadronic versus electromagnetic showers within its bismuth germanate (BGO) calorimeter. The electron energy is measured two ways: by the total amount of energy deposited in the calorimeter (usually about 85% of the incoming electron energy) and by the position of the shower maximum. Both techniques give consistent results \[74\], finding about 210 events at 300 – 800 GeV, compared to the 140 expected. This result confirms similar excesses seen previously by ATIC \[2\] and PPB-BETS \[3\]. Though suggestive, this alone would not be taken as strong evidence for WIMP annihilation, because there are astrophysical ways to accelerate electrons (SN shocks, pulsars, etc.). Dark matter annihilation would produce equal numbers of $e^+$ and $e^-$, so it is crucial to determine what fraction of the ATIC excess is positrons.

The second project, PAMELA \[4\], can distinguish between $e^+$ and $e^-$ and finds a sharp rise in the flux ratio $\phi(e^+)/($$\phi(e^+) + \phi(e^-)$$)$ above 10 GeV, continuing up to $\sim$ 80 GeV \[5\]. This confirms previous indications of an excess by HEAT \[6\] and AMS-01 \[7\], but at much higher confidence. Although lower energies ($\lesssim$ 10 GeV) are significantly affected by solar modulation, these high energy particles are not. The ordinary secondary positron spectrum, originating from cosmic ray (CR) interactions with the interstellar gas, is softer than the primary electron spectrum, so the positron fraction was expected to drop with energy. The surprising upturn in the positron fraction, therefore, is very strong evidence for a primary source of positrons. While astrophysical sources such as pulsars offer alternative explanations \[8, 9, 10, 11, 12\], dark matter remains a compelling explanation, especially, as we shall discuss, in light of the evidence for excess electronic production in the galactic center as well.

Finally, the Fermi Gamma-ray Space Telescope has recently published its spectrum of
the sum of electrons and positrons \[13\]. While they also see a significant hardening of the spectrum, they do not see a broad peak. Rather, they see a smooth spectrum with a break at $\sim$ TeV, which is also seen by HESS \[14, 15\]. Although the feature of ATIC is absent, the Fermi results are generally taken to support the PAMELA excess, and give a lower bound on the dark matter mass scale at around 1 TeV.

Before proceeding, it is instructive to make a simple empirical connection between PAMELA and Fermi, ATIC and PPB-BETS. For a casual observer of the PAMELA data, it seems clear that for energies between 10 and 80 GeV, the rise is well described by a power law added to the expected background spectrum. If we assume that this new component provides equal numbers of electrons and positrons, it constitutes $\sim 25\%$ of the total electronic activity at 100 GeV (i.e. positrons are $\sim 12\%$ of the total). A natural exercise is to fit this rise by assuming some new component of $e^+e^-$ which scales as a power of energy. One can extrapolate this power law to higher energies and see where it makes an order unity contribution to electronic activity (i.e., where the positron fraction is $\gtrsim 30\%$). The extrapolation of PAMELA (Figure 1) naturally yields an excess in the range of Fermi, ATIC and PPB-BETS similar to the one observed. While this argument is heuristic, it nonetheless makes a strong case that these signals arise from the same source, rather than two new, independent sources of high energy $e^+e^-$ coincidentally within a factor of a few in energy of each other.

This apparent connection between the high energy electron and PAMELA excesses is intriguing, but does not advance the argument that they arise from DM annihilation; it merely suggests that they arise from the same source and that source produces equal numbers of $e^+$ and $e^-$. In order to distinguish electrons and positrons coming from DM annihilations from those coming from conventional astrophysical sources, such as pulsars, we must look in regions where DM annihilation would produce strong signals relative to pulsars. The most obvious place for this is in the galactic center (GC) where pulsars are expected to have a relatively uniform abundance \[9, 16, 17\] while the DM density is expected to rise significantly. Since the annihilation power goes as the square of the WIMP density, any production of high energy $e^+e^-$ in the GC would likely be significantly enhanced, possibly by many orders of magnitude, for DM but not for astrophysical sources.

Remarkably, there are already indications of excess high energy electronic activity in the GC. Finkbeiner \[18\], while studying the foreground contributions to the WMAP 1-
FIG. 1: (a) A new power-law component of $e^+e^−$ fit to the PAMELA excess (long-dashed) with expected background $e^+$ model (solid) and total positron fraction (short-dashed). (b) Extrapolation of this new component to higher energies, assuming equal parts $e^+$ and $e^−$. For reference, the new component positrons are about 12% of the PAMELA fraction at 100 GeV, and therefore constitute about 1/4 of the Fermi flux $\phi(e^+) + \phi(e^-)$ at 100 GeV. The fact that the high energy electron+positron and PAMELA excesses are connected by such a generic argument suggests that a single mechanism, producing equal numbers of $e^+$ and $e^−$, explains both.

year data, found an excess of microwave radiation termed the “WMAP Haze”. Recently, Dobler & Finkbeiner showed that the Haze persists in the WMAP 3-year data and that it is spectrally consistent with hard synchrotron emission [19]. It was first argued in [20] that this hard synchrotron radiation could possibly be produced by high energy $e^+e^−$ products from DM annihilations. Additional studies have confirmed that the Haze can in fact arise from DM annihilations [21, 22], and that it would be natural for the same parameters that yield significant positron abundance in the 10-100 GeV range [22, 23].

Furthermore, previous measurements of gamma-rays in the GC [24] have indicated an excess above expected background levels [25] in the 10-100 GeV range. While this could arise from various sources, a very natural explanation would be from ICS of starlight photons from the same high energy $e^+e^−$ that generate the Haze.

Building on the remarkable qualitative consistency of these data, we explore possibilities for generating all of these signals from a single source of DM annihilation. The broad consistency of dark matter annihilation with all cosmic ray $e^+e^−$ data has been studied in
where it was shown that the best fit points to the whole data set were in leptonic modes. Others have also noted the connections between sources of hard positrons for PAMELA and the higher energy signals. More recently, the connection of ATIC and decaying dark matter was studied in, while considered the possibility of distinguishing DM and pulsar explanations with atmospheric Cherenkov telescopes. In terms of other experiments, showed the consistency between positron excesses at HEAT (which is consistent with current PAMELA results) and the Haze. In this paper we argue that modes with dominant annihilation into leptons (or through a light boson into leptons) naturally provide good fits to the high energy electron, PAMELA, and Haze data, with similar cross sections for each signal, along with fits to the EGRET data that are within the EGRET uncertainties. We shall see that a robust consequence of this class of annihilation modes is a large signal of ICS photons towards the GC.

II. DARK MATTER AS A SOURCE OF HIGH ENERGY PARTICLES

In this section we explore the possibility that the $e^+e^−, \gamma$-ray, and microwave signals mentioned in the previous section arise from WIMP annihilation. We examine the difficulty of obtaining a high-enough cross section to leptons without violating anti-proton and $\pi^0$ constraints, and propose a model that overcomes these difficulties.

Thermal dark matter (DM) naturally annihilates into high-energy cosmic rays, providing a source of electrons both locally and in the GC. The fact that WIMP DM naively predicts an excess of cosmic rays within a few orders of magnitude of what is observed makes it a natural candidate for understanding the various excesses, in spite of the challenges associated with achieving a signal as large as is seen. Dark matter may annihilate through various channels, which can produce $e^+e^−$ directly, or in decays of intermediate partners. The final particles may be detected directly by satellites or balloon experiments near Earth, or indirectly by their ICS and synchrotron signals (either locally, in the GC, in DM subhalos, or as an extragalactic background). These astrophysical signals of DM can constrain the particle mass, density, annihilation cross section, and annihilation channels.

Though this picture is appealing, attempts to explain the PAMELA excess through conventional annihilation channels (for instance to heavy flavors or gauge bosons) produce a softer positron spectrum than required. This problem is compounded by the ab-
sence of any anti-proton excess \cite{32}, since anti-protons would have been copiously produced from these annihilation modes. At the same time, direct annihilations to leptons are a model-building challenge as Majorana fermions have helicity-suppressed annihilations to these states, unless accompanied by a photon, which is $\alpha$-suppressed \cite{33}. This prompts consideration of vector \cite{34, 35} or Dirac \cite{36} particles. Nonetheless, in terms of annihilations directly to standard model modes, it appears at this point that only $\chi\chi \to e^+e^-, \mu^+\mu^-$, and to a lesser extent $\tau^+\tau^-$, are in good agreement with the data.

An alternative mechanism was proposed by \cite{22} as the means to produce hard leptons without anti-protons or excess $\pi^0$’s. Motivated by the requirement of a light ($\lesssim \text{GeV}$) boson $\phi$ in the XDM model of \cite{37} to explain a separate signal, they showed that annihilations $\chi\chi \to \phi\phi$, followed by $\phi \to e^+e^-$ or $\phi \to \mu^+\mu^-$ would naturally provide a hard lepton spectrum, explaining the HEAT and AMS-01 signals, and producing the Haze with similar parameters \cite{75}. These predictions provide a good fit to the PAMELA data \cite{28}, and are a central element of a proposed unified explanation of anomalies observed by PAMELA, ATIC, INTEGRAL, and EGRET \cite{38, 39}. Such models also naturally allow inelastic scattering, providing a possible explanation for the DAMA annual modulation signal \cite{40}. The light mass scale of the $\phi$ forbids or suppresses production of anti-protons. Furthermore, these light bosons can also help explain the amplitude of the signals by yielding the large cross section required to explain the cosmic-ray data via the Sommerfeld enhancement \cite{38, 76} or capture into bound states of “WIMPonioum” \cite{41}.

In this paper, we explore whether these annihilation channels provide a consistent picture that explains the entire set of data, including limits from the GC. We normalize our signal at the highest energies - using Fermi, ATIC and PPB-BETS - and proceed to lower energies, showing that similar parameters fit PAMELA and the Haze, while enforcing limits from EGRET. Rather than explore the model building questions, as in \cite{38}, we attempt to study the annihilation channels in a more model independent way. We extend the analysis of \cite{22, 28} by considering other modes, considering the total electron spectrum and considering the associated gamma ray signatures as well. We see that annihilations to $e^+e^-, \mu^+\mu^-, \phi\phi$ with $\phi \to e^+e^-$ and $\phi \to \mu^+\mu^-$ give good fits to the data. Modes with $\tau$’s generally give too broad a peak to explain ATIC, but are otherwise consistent with the electronic data. We also show that a natural consequence of these models is a significant ICS signal towards the GC from the scattering of starlight photons by the $e^+e^-$ arising from DM annihilation,
which may be observable by Fermi/GLAST. In the case of annihilation directly to $e^+e^-$, the energy cutoff of this signal should give a clear indication of the WIMP mass.

III. ANNIHILATION MODES AND THEIR COSMIC RAY SIGNALS

In this section we compute the expected cosmic-ray and photon signals for six primary annihilation modes. We consider $\chi\chi \rightarrow e^+e^-$, $\mu^+\mu^-$, and $\tau^+\tau^-$, as well as $\chi\chi \rightarrow \phi\phi$, followed by $\phi \rightarrow e^+e^-$, $\phi \rightarrow \mu^+\mu^-$, or $\phi \rightarrow \tau^+\tau^-$, the final three being modes that can arise in XDM models. For each annihilation mode, we produce a four-panel figure showing the local particle spectrum for high energy electrons/positrons and PAMELA, and the synchrotron and gamma-ray signals for the galactic center (Figures 3-8). We then consider the limits from diffuse gammas more generally, and estimate the astrophysical uncertainties of our predictions.

A. Analysis

Galactic cosmic ray propagation is a decades-old problem in astrophysics. Propagation parameters (diffusion and energy-loss coefficients, as well as boundary conditions) are constrained by isotope ratios of CR nuclei, measured as a function of energy. For example, the ratio of boron to carbon provides a constraint, since most carbon CRs were accelerated, but most boron CRs were made by spallation. Likewise, $^9$Be and $^{10}$Be are both made by spallation, but the short half-life ($1.5 \times 10^6$ yr) of $^{10}$Be serves as a clock, measuring the residence time of CRs in the galaxy. Using these and other constraints, it is possible to constrain a simple cylindrical model of the Milky Way galaxy to fit existing CR data, while predicting the behavior of a new leptonic component introduced by dark matter annihilation. To do this, we use a slightly modified version of GALPROP [42] version 50.1p [77].

GALPROP computes the steady-state solution to the usual propagation equations including diffusion, re-acceleration, nuclear interactions, and energy loss to ICS, bremsstrahlung and synchrotron for electron CRs; and hadronic collisions with interstellar gas for protons and heavier nuclei. Inputs to GALPROP include 3D estimates of the starlight, far IR, and CMB energy density, gas density, magnetic field energy density, diffusion parameters, and the primary source function from “conventional” processes (e.g. SN shocks). Outputs
include 3D density grids for each CR species; full-sky maps of gamma-rays due to ICS, bremsstrahlung, and $\pi^0$ gammas from ISM interactions; and a synchrotron map.

We run the code in 2D mode, solving the propagation equations on an \((r, z)\) grid. Note that this azimuthal symmetry is imposed to obtain the steady-state CR distribution, but then skymaps are generated using the (best-guess) 3D distributions of Galactic gas. These assumptions vastly oversimplify the Galaxy, and it is important to bear in mind that the quantitative results derived from such a model are suspect at the factor of 2 level (at least).

A recent addition to GALPROP is a feature allowing a DM profile to be specified, and the $e^+e^-$ injected by DM annihilation to be tracked independently of other primary and secondary $e^+e^-$. Because the results in the inner galaxy are so important for ICS and synchrotron predictions, it is crucial to treat the central spatial bin of the GALPROP grid carefully. This pixel represents a cylinder of radius $dr = 0.1$ and height $dz = 0.05$. At a distance of 8.5 kpc, 0.1 kpc corresponds to $0.67^\circ$. Version 50.1p sub-samples each spatial bin and averages the DM density. However, the annihilation power goes as the square of the density, so it is important to compute $\langle \rho^2 \rangle$, not $\langle \rho \rangle^2$. Furthermore, the averaging code incorrectly samples the DM distribution near $r = 0$, and sometimes introduces large errors for divergent profiles.

We have fixed these problems by summing $d\Omega a^2 \rho^2 da$ over each annular \((r, z)\) pixel, where \(a\) is the 3D radial coordinate, and $d\Omega$ is the solid angle subtended by the intersection of the pixel with a sphere of radius $a$. By handling this averaging carefully down to scales of $dr/100$, we are able to obtain good convergence properties for the $dr$ and $dz$ given above, even for profiles as cuspy as $\rho \propto r^{-1.2}$.

In this paper, we use the Einasto profile; following Merritt et al. [43] we assume a DM halo density profile of the form

$$\rho = \rho_0 \exp \left[ -\frac{2}{\alpha} \left( \frac{r^\alpha - R_\odot^\alpha}{r_{-2}^\alpha} \right) \right],$$

with \(\rho_0 = 0.3\) GeV cm\(^{-3}\) as the DM density at $r = R_\odot = 8.5$ kpc, and $r_{-2} = 25$ kpc.

For reference, the benchmark parameters used in our runs are the following. The cylindrical diffusion zone has a radius of 20 kpc and height $\pm 4$ kpc. The diffusion constant, $K(E) = 5.8 \times 10^{28}(E/4\text{ GeV})^\alpha$ cm\(^2\) s\(^{-1}\) where $\alpha = 0.33$, has the energy dependence expected for a turbulent magnetic field with the Kolmogorov spectrum. The rms magnetic
field strength \( \langle B^2 \rangle^{1/2} \) is modeled with an exponential disk,

\[
\langle B^2 \rangle^{1/2} = B_0 \exp\left(-\frac{(r - R_{\odot})}{r_B} - \frac{|z|}{z_B}\right)
\]

where \( r_B = 10 \text{ kpc} \) is the radial scale, \( z_B = 2 \text{ kpc} \) is the vertical scale, and \( B_0 = 5.0 \mu \text{G} \) is the value locally.

**B. Results**

The results of our analyses are presented in Figures 3-8 and 16. Qualitatively, we see that all modes considered give acceptable fits to the data. A few comments are in order, however.

The modes with annihilations directly to electrons or \( \phi \)-mediated electrons give the best fit to the ATIC/PPB-BETS excess, with only direct annihilations to electrons yielding a true peak (see Figure 16). This is simply a reflection of the hardness of the injection spectra (monochromatic and flat, respectively). These modes also require the lowest boost factors. Again, this is because none of the energy is partitioned into invisible modes (as with muons or taus) or into very soft electrons and positrons (as with pions from tau decays). Direct annihilation to muons also gives an acceptable fit to the ATIC excess, while \( \phi \)-mediated muons are slightly too soft. Annihilations to \( \tau \)-s and to \( \phi \)-mediated \( \tau \)-s are significantly too soft to achieve the “peaky” nature of the excess. In summary, modes with broad cutoffs (such as taus) give poor fits to ATIC, while modes with sharp cutoffs (electrons and \( \phi \)-mediated electrons) give better fits, as well as smaller boost factors.

In contrast, essentially all the annihilation modes except direct to electrons can fit the Fermi data well. The smooth cutoff (coupled with the larger error bars at higher energies) make essentially all of them compatible, although the \( \tau^+\tau^- \) and XDM \( \tau \) modes require somewhat uncomfortably large boost factors, if this is to be a thermal relic.

A careful observer will note that there appear to be two components to the ATIC excess: a “plateau” from approximately 100-300 GeV, and a “peak” from 300-700 GeV. None of the modes we have considered independently give both of these features, but it is possible that multiple annihilation channels could exist, for instance some linear combination of \( e^+e^- \), \( \mu^+\mu^- \) and \( \tau^+\tau^- \). This could arise if \( \phi \) could decay into multiple states, or multiple types of \( \phi \) particles were produced in the annihilation as would be expected for a non-Abelian
version of $\phi$-mediated DM annihilation $^{38, 39}$. However, the absence of such a signal at Fermi makes such elements probably unnecessary.

All modes give a good fit for the PAMELA positron fraction. It is not unexpected, given Figure 11, that a reasonable, smooth fit to Fermi and ATIC also fits PAMELA with similar boost factors. Quite remarkably, the boost factors required for the Haze are within a factor of two of those needed for Fermi, ATIC and PAMELA. This relationship was noted in $^{22}$, where $\phi$-mediated electron and muon modes were studied as explanations for the excesses observed by previous positron cosmic ray experiments (HEAT, AMS-01). There it was found that the Haze signal naturally required a boost factor very similar to that needed for the excess that has since been seen at PAMELA.

The overall boosts needed for Fermi and PAMELA differ approximately by a factor of two. Too much should not be made of this. To begin with, the fits are done separately, and in that light, the closeness of the required boosts is actually very encouraging. Secondly, there are uncertainties in the instruments; in particular, the Fermi acceptances are not precisely known. Additionally, since PAMELA actually measures a ratio, a similar signal can be found with a lower boost by employing a softer primary electron spectrum. This would change the Fermi fit somewhat and would require a larger boost to fit the Fermi data. Finally, we have attempted to hit the central value of the highest PAMELA data points. Should these come down, so, too, will the boost. Thus, absent a measurement of the electron spectrum only (i.e., not $e^+e^-$) from PAMELA, it is difficult to say whether they are in tension, or if there are simply small systematics that will allow agreement. Future data should clarify this.

We should note that we find larger boost factors needed for the Haze than calculated in $^{21}$ (and noted in $^{11}$). The principle reasons are the very cuspy profile used in $^{21}$ and the relatively low levels of inverse Compton scattering assumed by them. In $^{21}$ the cuspy profile $\rho \propto r^{-1.2}$ was used, leading to more power in DM annihilations in the center of the galaxy, resulting in lower boost factors to fit the Haze. In contrast, we use the Einasto profile (Eq. 1) with fits established by Merritt et al. $^{43}$. As was shown in $^{22}$, the Einasto profile yields similar boost factors as the NFW profile with $\rho \propto r^{-1}$. For electrons with $E \gtrsim 5$ GeV, the dominant energy losses are due to ICS and synchrotron radiation. $^{21}$ considered a homogeneous magnetic field of 10 $\mu$G and homogeneous energy loss rates of $5 \times 10^{-16}(E/\text{GeV})^2$ GeV/s and $2.5 \times 10^{-16}(E/\text{GeV})^2$ GeV/s. As the magnetic field that we consider here has a peak value of 11.7 $\mu$G at the center of the galaxy (corresponding to
3.0 eV cm$^{-3}$), our energy losses to synchrotron radiation in the GC are very similar to those in [21]. However, our energy losses to inverse Compton scattering increase with decreasing distance from the center of the galaxy due to the inhomogeneity of the interstellar radiation field. The radiation field model used in GALPROP is large in the center of the galaxy, with energy densities of 18.8 eV cm$^{-3}$ at $r = 0$ and 14.3 eV cm$^{-3}$ at $r = 0.5$ kpc. As a result, the larger ICS losses compete against the synchrotron losses, and less power is emitted in synchrotron radiation. Thus, less energy is radiated into the 23 GHz band, resulting in higher boost factors. We note that [21] did not include bremsstrahlung energy losses, but this has a minor effect on the overall boost. Nonetheless, one should conclude that there is at least a factor of a few uncertainty in the overall normalization of the cross section needed to explain the Haze. And, while we take it as a positive that the conventional parameter choice leads to very similar boosts for PAMELA, Fermi and the Haze, too much should not be made of this in light of this uncertainty.

Signals at EGRET and Fermi/GLAST

With the successful operation of Fermi/GLAST, there is naturally great interest in gamma ray signatures of dark matter models. It is especially important within the context of the present PAMELA, Fermi electron, ATIC and PPB-BETS results, because, as we have emphasized, the galactic center may offer the ideal testing ground of the dark matter explanation of these data. It is then noteworthy that a generic prediction of scenarios involving WIMP annihilation is a significant production of ICS gamma rays in the galactic center. We believe this to be independent of the particular annihilation mode which explains the electron and positron signals, and only that the significant electronic production here is reflected in the galactic center.

Background gamma rays in the galactic center are expected to come from a variety of sources, specifically, $\pi^0$s from protons interacting with the ISM, inverse Compton scattering (ICS) from cosmic ray electrons, as well as a small component of bremsstrahlung. (See Figure 2) Note that the spectrum due to conventional sources is expected to fall dramatically as one moves to higher energies.

In the context of our present discussion, the behavior of the gamma ray spectrum at the higher energies detectable by Fermi/GLAST should be dramatically changed. If dark matter is responsible for an O(1) correction to the local flux of cosmic ray electrons in the 400-800
FIG. 2: The dominant contributions to gamma rays in the galactic center (inner 5°) from conventional astrophysical CR interactions. Shown are the photons from π⁰’s, electron ICS signals and bremsstrahlung. In this and following figures, “ISM” denotes gammas produced by CR interactions with the interstellar radiation field, as well as the interstellar medium (gas and dust). The π⁰ line refers to π⁰ γ-rays produced by the hadronic CRs interacting with the interstellar medium. The slope of the π⁰ curve at high energies is tied to the primary p CR spectrum, and is better constrained than the amplitude.

GeV range, then it would be expected to be the dominant contributor to the electron flux in this energy range in the galactic center. Such electrons are responsible for upscattering photons to energies $E_{\text{upscatter}} \approx 2E_{\text{initial}}\gamma^2$. For (initially) optical photons, this will result in a major contribution to photons in the 10 - 1000 GeV range. Note that these photons are independent of other sources, such as the final-state radiation (FSR) gammas from charged particle production or π⁰’s produced in e.g., τ decay. Rather, these photons are intimately linked to the production of high-energy electrons and positrons, the same population of particles which we believe should be yielding the Haze.

Indeed, this basic intuition is borne out in Figures 3-8. One sees very significant gamma ray signatures at high energies in all channels. One should not read too much into the fact that many modes seem to exceed the EGRET values - as we shall discuss shortly, there is a factor of a few uncertainty arising from astrophysics. While modes with τ’s can have gamma ray fluxes dominated by π⁰ production (often exceeding present EGRET limits quite significantly), the fluxes for the electron and muon modes are dominated by ICS gammas.
FSR signals tend to be significant only at the highest energies, which are out of the range of Fermi/GLAST for the dark matter masses suggested by the break at \( \sim \) TeV seen at Fermi, HESS and ATIC. (Fermi/GLAST has an upper energy reach of \( \sim 300 \) GeV for photons.) The collinear approximation we have used for the FSR gammas is not appropriate at the highest energies, where FSR becomes important, and should probably be taken as an upper bound on the FSR signal in that energy range. Additionally, the size and shape of the FSR signal is model dependent; it depends on the parameters involved (notably the \( \phi \) mass in the \( \phi \)-mediated modes). That said, it is possible that a lower value for the ISRF energy density could lead to a lower ICS signal, as we shall discuss shortly, in which case FSR signals could be quite relevant in the Fermi range, even for the large masses considered. In contrast, the ICS signal should be present for any population of electrons with the same spectrum which explains the high energy electron signal and PAMELA, and, more to the point, almost any population of DM-produced electrons which explains the Haze. This strong signal should be observed by Fermi/GLAST and would be a smoking gun of this massive high energy electronic production in the galactic center.

We note that none of our current models seem to give a good fit to the EGRET data points in the 2 – 5 GeV range. The difficulty these EGRET observations present for standard \( \gamma \)-ray production mechanisms was pointed out previously by [25], who proposed an “optimized” model, with modified electron and proton CR spectra. Because this excess appears everywhere on the sky, not just the galactic center, it is unlikely to be related to ICS from dark matter. A modified proton spectrum is also not likely in our model, given that no significant anti-proton excess has been observed. However, the potential for DM annihilation to affect the average electron spectrum is obvious.

C. Limits from diffuse gamma rays

One of the most important consequences of this scenario is the presence of significant ICS gamma ray production in the inner few degrees of the galaxy. This is a natural byproduct of these new sources of \( e^+e^- \). These signals are naturally dependent on the positrons and electrons produced, and hence on the cosmic ray propagation models. In contrast, predictions of photons from \( \pi^0 \)'s or final state radiation \([33, 47, 48, 49, 50, 51, 52, 53, 54, 55]\) depend only on the DM halo profile and annihilation modes. It is worth considering the
FIG. 3: The cosmic ray signals from dark matter annihilations $\chi\chi \to e^+e^-$. Upper left: Predicted positron fraction vs. energy (solid and dashed lines), expected positron fraction vs. energy due to secondary production only (dotted), and PAMELA data points. BF is the boost factor required relative to $\langle \sigma_A v \rangle = 3 \times 10^{-26}$ cm$^3$/s and the reference local DM density of $\rho_0 = 0.3$ GeV cm$^{-3}$. Upper right: Spectrum of DM $e^+e^-$ (solid and dashed), background $e^+e^-$ (dot-dashed), and total (solid and dashed) with data from Fermi, ATIC and PPB-BETS. Lower left: Predicted WMAP Haze signal vs. galactic latitude at 23 GHz (solid and dashed) and data points from WMAP. Error bars are statistical only. Lower right: Total diffuse gamma ray spectrum (solid and dashed) and background diffuse gamma ray spectrum (dotted) for the inner 5° of the Milky Way, computed with GALPROP. Data points are from the Strong et al. re-analysis of the EGRET data, which found a harder spectrum at 10 – 100 GeV within a few degrees of the GC, using improved sensitivity estimates.
FIG. 4: The cosmic ray signals of dark matter annihilations as in Figure 3 but with \( \chi \chi \to \mu^+ \mu^- \). Constraints these prompt photons place on DM annihilation, using both galactic center and diffuse extra-galactic limits.

We show in Figure 10 the limits on boost factors (BF) for different \( \gamma \)-ray production modes, both for NFW and Einasto profiles. To generate these plots, we calculate the total flux of prompt photons, either from FSR or \( \pi^0 \) decays, from the different sky regions as defined in [25]. We consider annihilations to \( \tau^+ \tau^- \), \( \pi^0 \pi^0 \), and \( e^+ e^- \), as well as the mediator decay modes \( \chi \chi \to \phi \phi \), with \( \phi \to \tau^+ \tau^- \), \( \phi \to \pi^0 \pi^0 \) and \( \phi \to e^+ e^- \). To generate these limits, we use the EGRET bounds from [45], and take the 2-sigma upper bounds to be conservative (no background subtraction is included). We show limits for both NFW (dashed) and Einasto (solid) profiles. Note that the inclusion of backgrounds can make these limits significantly stronger - we present them in this form to be clear what an incontestable upper
FIG. 5: The cosmic ray signals of dark matter annihilations $\chi \chi \rightarrow \tau^+ \tau^-$.

bound is.

Other limits can be found from HESS data \cite{56} or from the inner 1° of the Milky Way. These limits are highly dependent on the details of the profile, and we limit ourselves to the more conservative ones from the EGRET data. \cite{78}

D. Other modes

While we have focused on the six simple modes, there are many alternatives. In particular, if $\phi$ is a vector, it can go to combinations of various modes \cite{28,38,55}. This tends to have little effect on the electronic spectra of Fermi and ATIC \cite{28}, which are dominated by the hardest significant mode, and only moderate effect on PAMELA. Similarly, the Haze, which
FIG. 6: The cosmic ray signals of dark matter annihilations $\chi \chi \rightarrow \phi \phi$, followed by $\phi \rightarrow e^+ e^-$. is dictated by the same energy range as PAMELA, is not extremely sensitive to such changes in the annihilation channel, but only the total power in it (this is in part due to the fact that the overall spectrum of the Haze is still not well known). However, the presence of additional soft electrons and positrons can change the spectrum of ICS photons. As an example we show the cosmic ray signatures for a mode with an additional soft component in Figure 11 where $\chi \chi \rightarrow \phi \phi$ where $\phi$ decays to $e^+ e^-$, $\mu^+ \mu^-$ and $\pi^+ \pi^-$ in a 1:1:2 ratio. For ICS photons in a more intermediate situation, we show in Figure 12 the gamma ray spectrum for the case of annihilations $\chi \chi \rightarrow \phi \phi$, where $\phi$ subsequently decays to $e^+ e^-$, $\mu^+ \mu^-$ and $\pi^+ \pi^-$ in a 4:4:1 ratio.

Similarly, we consider how well an annihilation mode with hadronic elements fits the data. We show in Figure 13 the electronic signals of $\chi \chi \rightarrow W^+ W^-$. Such a mode is
FIG. 7: The cosmic ray signals of dark matter annihilations $\chi \chi \rightarrow \phi \phi$, followed by $\phi \rightarrow \mu^+ \mu^-$. An approximately 1 TeV WIMP gives the best fit to the high energy break observed by Fermi, ATIC and HESS (dominantly through its hard leptonic decays), but it does a poor job of reproducing the spectrum. Going to higher masses does not help, as in the PAMELA energy range, dark matter would significantly overproduce positrons and provide a poor fit, even with smaller boost factors (note that the approximate fits to the PAMELA data have boosts only one third as large as those for Fermi). Extragalactic limits on diffuse gammas are stronger than this, as discussed by [59], where boosts of $\sim 100$ were found to be borderline with EGRET within the context of an NFW profile. With the strong $\bar{p}$ limits, any explanation of the high energy electron excess and PAMELA with W bosons would be expected to be due to significant local production.
Consequently, neither a Haze nor an ICS signal would be expected (as the similar boost would not be expected in the center of the galaxy).

Finally, if \( \phi \) is a scalar, then one can expect a branching ratio to \( \gamma \gamma \) up to \( \sim 10\% \) \cite{22}. We show how such a contribution to the Fermi/GLAST signal would appear in Figure \ref{fig:14}. One can see that in the Fermi range, the gamma ray spectrum is swamped by ICS contributions. Only at the highest energies are the gammas from DM annihilation visible. Should the high energy (\( \gtrsim 300 \) GeV) electrons not arise from dark matter, and if the \( \phi \) is sufficiently light (\( \lesssim 300 \) MeV), this contribution may appear as a small peak at the end of the \( E^2 \) gamma distribution (as the spectrum of these photons is flat in energy).
FIG. 9: Different contributions to gamma rays in the galactic center for different dark matter annihilation modes.
FIG. 10: Boost factor limits (compared to $\sigma v = 3 \times 10^{-26}$ cm$^3$s$^{-1}$ and $\rho_0 = 0.3$GeV cm$^{-3}$ for a) NFW profile, b) Einasto profile. In each panel, lines are shown for XDM electrons ($\chi\chi \rightarrow \phi\phi$, $\phi \rightarrow e^+e^-$), direct electrons ($\chi\chi \rightarrow e^+e^-$), XDM taus ($\chi\chi \rightarrow \phi\phi$, $\phi \rightarrow \tau^+\tau^-$), direct taus ($\chi\chi \rightarrow \tau^+\tau^-$), XDM pions ($\chi\chi \rightarrow \phi\phi$, $\phi \rightarrow \pi^0\pi^0$), and direct pions ($\chi\chi \rightarrow \pi^0\pi^0$). The limits come from prompt FSR and $\pi^0$ gammas only. Limits are determined by requiring that no EGRET data point is exceeded by more than 2$\sigma$.

E. Astrophysical Uncertainties

One of the most robust predictions of the dark matter scenarios considered above is the ICS signal in the center of the galaxy. One might naturally wonder how robust this is.

The greatest source of uncertainty is the extrapolation of the local annihilation signal, as observed by PAMELA, Fermi, and ATIC, to the galactic center. This extrapolation is uncertain for many reasons, not least because of the assumption of a smooth dark matter distribution in the galactic halo, in spite of the fact that simulations show clumpy substructure. Dark matter in subhalos, which might ordinarily have annihilation power comparable to that of the smooth halo even in conventional models, can dominate by a large factor in the case of Sommerfeld enhanced annihilation \cite{38}, because the velocity dispersion of subhalos is small (see \cite{60, 61, 62, 63, 64, 65, 66, 67} for further discussion). In this case the annihilation power in the galactic center has more to do with the mass distribution and survival rate of clumps in the galactic center than the properties of the smooth halo. Additionally, dark
FIG. 11: The cosmic ray signals of dark matter annihilations as in Figure 3, but with $\chi \chi \to \phi \phi$, followed by $\phi \to e^+ e^- : \phi \to \mu^+ \mu^- : \phi \to \pi^+ \pi^-$ in a $1 : 1 : 2$ ratio.

matter can form a dark disk, leading to high annihilation rates [68]. On the other hand, the halo could be less cuspy than we’ve assumed here, and substructure could be destroyed in the center, lowering the annihilation signal relative to our expectations. Taking into account the uncertainties in both the dark matter distribution and the particle physics, our simple extrapolation from local annihilation rate to the galactic center is probably uncertain by one or two orders of magnitude.

However, if the central density is too low, we would be unable to explain the Haze with dark matter annihilations, or the 511 keV signal from INTEGRAL through the exciting dark matter mechanism. But it happens that the boosts needed to explain the Haze are very similar to those needed for Fermi and PAMELA, and so we constrain most of these
FIG. 12: The gamma ray signals from a model that annihilates into electrons, muons, and pions in a 4:4:1 ratio. The gamma ray spectrum is noticeably softer than that for annihilations into just electrons with the same mass.

FIG. 13: PAMELA and high energy electron signals of dark matter annihilations $\chi \chi \rightarrow W^+W^-$. 

uncertainties using the normalization of the Haze. This still is not perfect; there is always a factor of a few uncertainty in the boosts associated with the Haze, simply arising from uncertainties in the strength of the magnetic field in the galactic center, as well as its spatial distribution.

Putting aside this uncertainty, we examine the range of signals possible for Fermi/GLAST. In doing this, it is important to distinguish the different components contributing to the
FIG. 14: Gamma ray signals including a 10% BR of $\phi \rightarrow \gamma \gamma$.

Fermi DM signal, namely, ICS, FSR and $\pi^0$ gammas. The $\pi^0$ gammas arise only from the modes with $\tau$'s, but all the modes we consider have an FSR signal, whether the annihilation goes directly into charged particles or via intermediate $\phi$ states (see appendix). Given a WIMP model, these photons (FSR and $\pi^0$) are uncertain only at the level of the overall dark matter annihilation in the galactic center, which is naturally the appropriate size to produce the Haze.

The ICS photons are also produced by all the modes under consideration, and are, in general, the most model-independent prediction of these scenarios, arising directly from the interactions of electrons and positrons with starlight. This, however, can vary significantly, because the electrons share their energy between ICS and synchrotron, depending on the relative energy densities of starlight and the magnetic field. If the magnetic field in the galactic center is larger than the $11.7 \mu G$ we assume ($= 3 \text{ eV cm}^{-3}$), then the signal in WMAP is increased, at the expense of the ICS signal, assuming constant power. If the annihilation power is normalized to the Haze, then the inferred ICS power drops further. Additionally, a change in the diffusion constant can result in fewer electrons trapped in the galactic center region, allowing more signal to propagate away from the inner $5^\circ$. Finally, if the energy density of starlight is lower than in the ISRF maps employed in GALPROP [for a discussion of the ISRF used in GALPROP and the associated uncertainties, see 69], the ICS signal can be decreased by a corresponding factor of up to roughly two at higher
energies. We attempt to quantify these uncertainties in Figure 15 for the ICS signal from \( \chi \chi \to \phi \phi \), with \( \phi \to e^+ e^- \). We see that the signal can be suppressed by a factor of 3-6, depending on energy.

FIG. 15: Synchrotron (as a function of radial distance from the GC, left) and ICS (right) towards the GC for five different diffusion models. Model 0: the “benchmark” model given in §III A. Model 1: \( B_0 \) doubled leading to more energy losses from synchrotron compared to ICS. Model 2: Diffusion zone scale height decreased from 4 kpc to 2 kpc. Model 3: Diffusion index, \( \alpha \), changed from 0.33 (Kolmogorov spectrum) to 0.5. Model 4: Optical intensity in the interstellar radiation field (ISRF) reduced by half leading to less ICS of optical photons (decreased ICS at energies above 10 GeV) and increased synchrotron. Model 5: \( B_0 \) doubled and optical intensity in the ISRF reduced by half. Since Model 5 yields the largest synchrotron output, if we normalize the boost factor to fit the Haze data with this model, the implied ICS (“HN * Model 5”) emission is roughly a factor of 4 below the “benchmark” Model 0.

The dominant gamma ray contribution for most modes is from ICS, as we show in Figure 9. Aside from this contribution and its uncertainty, we see that for the tau modes there is significant production of gamma ray radiation from \( \pi^0 \) gammas. Normalizing to the Haze, we expect a possibility of variation in this contribution at roughly a level of a factor of 2, that is, just in proportion to the overall changes in DM annihilation needed for the Haze. A similar level of uncertainty can be made for the FSR gammas, although they are less important. Thus, explaining the existing data, Haze+High Energy Electrons+PAMELA, with dominant tau modes seems in significant tension with existing EGRET data. This
should be easily clarified by Fermi/GLAST, however.

IV. CONCLUSIONS

The hard electron spectrum in the energy range $\sim 400 - 800$ GeV, observed previously by earlier experiments of ATIC and PPB-BETS, has now been confirmed by the recent run of ATIC and the even more recent Fermi results (though we should add that Fermi did not observe the pronounced peak in the spectrum). This gives a new piece of evidence for a new primary source of electronic production in the halo. Recent results by the PAMELA experiment point in a similar direction. Simple extrapolations of PAMELA seem to connect the experiments, calling out for consideration of a unified explanation.

In this paper, we have studied the possibility that dark matter annihilations could simultaneously explain the excesses seen by Fermi, ATIC, PPB-BETS, PAMELA and WMAP. We find remarkable agreement, with very similar boost factors to explain each one of them. The presence of the Haze in the center of the galaxy gives some weight to the dark matter interpretation of the signal, as astrophysical sources would not be expected to give significant positron fluxes in the galactic center, much less at latitudes of $5^\circ$ to $10^\circ$ (700 pc to 1400 pc) off the galactic disk. The Fermi/GLAST observations of ICS and other photons in the galactic center should give clear evidence for this scenario. Should these gamma rays extend to the reach of the Fermi/LAT experiment, the ubiquity and scale of excess electronic production would make dark matter the definitive explanation.

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FIG. 16: Electron spectra fits to ATIC from various annihilation modes.

APPENDIX A: FITS TO ATIC

In light of the current Fermi data, it is natural to focus on those data for normalizing our electron spectra at high energies. However, prior to Fermi, ATIC gave the first indication of a mass scale, and the presence of an excess at higher energies. In a previous version of the paper, prior to the Fermi data release, fits to ATIC were presented as well. While the updated Fermi data may cast significant doubt on the need for a sharp "peak" in the spectrum, it is still worthwhile to see how "peaky" a signal can be achieved with these modes. Thus, we show these fits here.
APPENDIX B: FINAL STATE RADIATION

Final state radiation is very important for annihilations into charged states [47, 48, 49, 54, 56]. An exhaustive study of FSR is well beyond our purposes here, but we include it in the spectra presented. The FSR for the dark matter direct annihilation to fermions is [47, 54]

\[
\frac{d\sigma(\chi\chi \rightarrow f\bar{f}\gamma)}{dx} \approx \frac{\alpha Q_f^2}{\pi} F(x) \log \left( \frac{s(1-x)}{m_f^2} \right) \sigma(\chi\chi \rightarrow f\bar{f})
\]  

(B1)

where \( s = 4m_{\chi}^2, \) \( x = 2E_{\gamma}/\sqrt{s}, \) and \( F(x) = ((1-x)^2 + 1)/x. \)

For the decays of \( \phi \rightarrow f\bar{f}, \) we need a slightly different formula.

Working from eq. (B1), we can instead consider the case of \( \phi \) decay, which has the same essential formula, but with \( s = m_{\phi}^2. \) If \( \phi \) is boosted by an amount \( \gamma = m_\chi/m_\phi, \) and we assume the \( \gamma \) is emitted at angle \( \theta \) relative to the boost, we have the relationship

\[
y = \frac{E_\gamma}{m_\chi} = \frac{x}{2}(1 + \cos \theta)
\]

(B2)

Then we have a distribution of \( \gamma \)'s for every \( \phi \)

\[
\frac{dN}{dy} = \frac{1}{2} \int_{\cos \theta_{min}}^{1} d\cos \theta \frac{dN}{dx} \frac{dx}{dy}
\]

(B3)

where \( \cos \theta_{min} = 2y - 1 \) is the minimum angle in the \( \phi \) frame for which boosted photons can have energy \( ym_\chi. \) This gives

\[
\frac{dN}{dy} = \frac{\alpha Q_f^2}{2\pi} \int_{\cos \theta_{min}}^{1} d\cos \theta \frac{1}{y}(1 + (1-x)^2)(\log(m_{\phi}^2/m_f^2) + \log(1-x)) \frac{2}{1 + \cos \theta}
\]

(B4)

The first term, proportional to \( \log(m_{\phi}^2/m_f^2), \) is dominant at small \( x, \) and is easily evaluated, while the second is somewhat more complicated. We write this as

\[
\frac{dN}{dy} = \frac{\alpha Q_f^2}{y\pi}(\log(m_{\phi}^2/m_f^2)P_1 + P_2),
\]

(B5)

where

\[
P_1 = 2 - y + 2y \log y - y^2
\]

(B6)

and

\[
P_2 = \log(2) + (3 - y - y^2) \log(1-y) - \left(1 + \frac{\pi^2}{3} - y \right) y \\
+ y \log(y)(\log(y) + 2) + \text{Re} \left[2y \text{Li}_2\left(\frac{1}{y}\right)\right]
\]

(B7)
A few points to consider: one must of course recall that this is the $\gamma$ distribution per $\phi$, and that there are two $\phi$'s per annihilation. We have taken the approximation that $m_\phi \gg m_f$. (See [53] for a further discussion.) Also, we have used the approximate formula [B1] which is only valid in the collinear limit. The hardest part of the spectrum we show would then be expected to be somewhat softer that what we have displayed. A complete analysis is warranted.

[66] Q. Yuan et al. (2009), 0905.2736.
ph/0412403.


[74] see Figure s8 in the Supplement to [1]

[75] See [70] for a subsequent discussion of what has been termed “secluded” WIMP models which includes XDM as a subset.

[76] The importance of this effect in the context of multi-TeV scale dark matter interacting via W and Z bosons was first discussed by [71, 72], and more recently emphasized with regards to PAMELA in the context of “minimal dark matter,” with similar masses by [57, 73].

[77] GALPROP and the resource files we employed are available at http://galprop.stanford.edu; our modifications are available upon request.

[78] Subsequent to the initial version of this paper, specific limits from HESS have appeared for many of the scenarios considered here [50, 51, 52, 53, 55] and we refer the interested reader to those works. These works find, as we do, that modes with $\tau$’s are highly constrained, as are modes annihilating directly to leptons. Annihilation into hard electrons or muons are constrained except in very soft halos, while XDM annihilation modes are consistent for Einasto profiles.