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Title: 3D Structure of Individual Nanocrystals in Solution By Electron Microscopy

Authors:
Jungwon Park†1,2,3, Hans Elmlund†4,5, Peter Ercius†6, Jong Min Yuk7,8,9, David T. Limmer10, Qian Chen1,8, Kwanpyo Kim11, Sang Hoon Han12, David A. Weitz2,3, A. Zettl7,8,9, and A. Paul Alivisatos1,8,9 *

Affiliations:
1 Department of Chemistry, University of California, Berkeley, CA 94720, USA.
2 Department of Applied Physics, Harvard University, Cambridge, MA 02138, USA.
3 School of Engineering and Applied Sciences, Harvard University, Cambridge, MA 02138, USA.
4 Department of Biochemistry and Molecular Biology, School of Biomedical Sciences, Monash University, Clayton, VIC 3800, Australia.
5 ARC Centre of Excellence for Advanced Molecular Imaging, Clayton, VIC 3800, Australia.
6 The Molecular Foundry, Lawrence Berkeley National Laboratory, Berkeley, CA 94720, USA.
7 Department of Physics, University of California, Berkeley, CA 94720, USA.
8 Materials Sciences Division, Lawrence Berkeley National Laboratory, Berkeley, CA 94720, USA.
9 Kavli Energy NanoScience Institute, Berkeley, CA 94720, USA.
10 Princeton Center for Theoretical Science, Princeton University, Princeton, NJ 08540 USA.
11 Department of Physics, Ulsan National Institute of Science and Technology (UNIST), Ulsan 689-798, South Korea.
12 Amore-Pacific Co. R&D Center, Yongin 446-829, South Korea.

†These authors contributed equally to this paper.
*To whom correspondence should be addressed: alivis@berkeley.edu
Abstract:
Understanding structural details of colloidal nanoparticles is required to bridge our knowledge about their synthesis, growth mechanisms, and physical properties. We introduce a method for determining 3D structures of individual nanoparticles in solution. We combine a graphene liquid cell, high-resolution transmission electron microscopy, a direct electron detector, and an algorithm for single-particle 3D reconstruction originally developed for analysis of biological molecules to produce two near-atomic resolution 3D structures of individual Pt nanocrystals. Since our method derives the 3D structure from images of individual nanoparticles rotating freely in solution, it enables the analysis of heterogeneous populations of potentially unordered nanoparticles that are synthesized in solution, thereby providing a means to understand the structure and stability of defects at the nanoscale.

Main Text:
Colloidal nanoparticles are clusters of hundreds to thousands of inorganic atoms typically surrounded by organic ligands that stabilize them in solution. The atomic arrangement of colloidal nanoparticles determines their chemical and physical properties, which are distinct from bulk materials and can be exploited for many applications in biological imaging, renewable energy, catalysis, and more. The 3D atomic arrangement on the surface and in the core of a nanocrystal influences the electronic structure, which affects how the nanocrystal functions in catalysis or how it interacts with other components at the atomic scale (1). Introduction of atomic dopants, surface adatoms, defects, and grain boundaries alters the chemical properties of nanocrystals (2). Ensembles of synthesized nanocrystals in solution are structurally inhomogeneous due to the stochastic nature of nanocrystal nucleation and growth (3, 4). Therefore, a method for determination of the 3D atomic arrangement of individual unique nanoparticles in solution is needed.
Electron tomography is routinely used for 3D analysis of materials (5–9). This method cannot be applied to individual particles in a liquid because it relies on acquisition of images of a single object at many different tilt angles over 2 to 5 hours, assuming the object is static during the entire acquisition. Single particle cryo-electron microscopy (cryo-EM) is a common method for the determination of 3D structures in biological sciences. The average 3D Coulomb potential map (density) of a protein is reconstructed from tens of thousands of TEM images of randomly oriented copies of the same protein embedded in vitreous ice (10). The unknown 3D projection angles of the images are determined by computational methods (11). Single-particle cryo-EM has succeeded in reconstructing biological molecules with nearly 3 Å resolution (10, 12). A similar approach was recently applied to reconstruct the atomic structure of homogeneous ultrasmall gold clusters (13). However, the single-particle method is not readily applicable to 3D reconstruction of colloidal nanoparticles due to their intrinsic structural inhomogeneity at the atomic level.

TEM has undergone significant technical improvements in the past decades (5, 14–17). The image resolution has been improved with the introduction of electron lens aberration correctors (15). The development of direct electron detectors is providing a significant enhancement to single-particle cryo-EM due to improvements in image quality and rapid acquisition of movies that allow for the compensation for beam-induced specimen motion (18).

We present a hybrid method for reconstructing the 3D structures of individual nanoparticles in solution. The method represents a combination of three technological advancements from TEM imaging in biological and materials science: (1) the development of graphene as a covering to hold a liquid in vacuum (the so-called graphene liquid cell, or GLC) that allows atomic-resolution imaging of nanoparticles that move and rotate freely in solution by aberration-corrected TEM (3, 19), (2) the advent of direct electron detectors, producing movies with millisecond frame-to-frame time
resolution of the rotating nanocrystals (18), and (3) a theory for ab initio single-particle 3D reconstruction used to solve the inverse problem of recovering the unknown 3D orientations of the individual noisy nanocrystal projections (11). The resulting hybrid technique called SINGLE (3D Structure Identification of Nanoparticles by Graphene Liquid Cell EM) was used to separately reconstruct the 3D structures of two individual Pt nanocrystals in solution.

Pt nanoparticles were chosen because of their high electron scattering strength, because their detailed atomic structure is important for catalysis, and because earlier graphene liquid cell studies have shown that they grow by nanoparticle aggregation, resulting in complex structures that are not possible to determine by any previously developed method. Pt nanocrystals with sub-2 nm diameter were prepared in solution. Two graphene sheets were grown by the chemical vapor deposition method and used to entrap solvated nanocrystals (3). The graphene provides an ultra-thin covering of material to maintain liquid conditions in the TEM vacuum and presents an inert surface onto which the nanoparticles do not adsorb. The translational and rotational motions of the particles in liquid pockets with sub-50 nm diameter were imaged in situ using TEAM I, a TEM instrument with geometrical and chromatic aberration-correction, operated at 300 kV using a direct electron detector (see schematic illustration in Fig. 1 (A)). The corrector was set to apply a slightly negative spherical aberration coefficient of about -10 μm. Under these imaging conditions, we produced white atom contrast when using a small under-focus value of 30 – 50 Å.

Movies of the moving particles had a temporal resolution of 50 frames per second, a field of view of 1,024 by 1,024 pixels and a Nyquist sampling limit of 0.56 Å. Each movie frame represents a two-dimensional (2D) projection of many particles in random orientations. In order to reconstruct the individual 3D structures, a small region around each single particle of interest was chosen in each individual frame to create a set of projections per particle. The 3D orientations of the resulting series of noisy 2D images of
a single rotating particle were recovered computationally using an ab initio 3D reconstruction algorithm adapted from one originally developed to recover orientations from cryo-EM images of many identical individual particles (11).

Although the TEM movies contain many particles, not all particles could be used for reconstruction due to overlap with other particles and insufficient rotation. Here, we present the two most reliable 3D reconstructions from a 1561 image series (particle 1 in Fig. 1 (B), (C), and Movie S1) and a 1171 image series (particle 2 in Fig. (D), (E), and Movie S2). Fig. 1 (B) to (E) show the EM density maps of the two Pt nanocrystals. The rendered particle volumes/diameters are 5,300 Å³/22 Å (particle 1) and 4,800 Å³/20 Å (particle 2). Along with the direct visualization of the spatial distribution of Pt atomic-planes, external and internal structures of the particle are uncovered. Each reconstruction shows three distinct crystal domains in both of the Pt particles. In Fig. 1 (B) and (D), we show views of the EM maps in an orientation that reveals distinct lattice planes of the core domain. Differently oriented 3D density maps are shown in Fig. 1 (C), (E), Movie S1, and Movie S2.

Our 3D reconstruction methodology produced near-atomic resolution reconstructions from relatively small sets of noisy experimental TEM images of nanocrystals in random orientations. We tested the validity of SINGLE using 1000 multislice TEM simulations of a randomly oriented Pt nanocrystal with dodecahedral symmetry and corresponding size. A near-atomic resolution reconstruction was obtained from images with a signal-to-noise ratio (SNR) roughly corresponding to that of the experimental images (see Fig. S1). This verified that the experimental images can conform to the projection-slice theorem with ideal microscope conditions (20).

In order to confirm the existence of a projected lattice in the experimental images, we calculated their power spectra, showing distinct spots along different crystalline zone axes (Fig. S2). Closer examination of the power spectra and corresponding orientation
coverage throughout the image series revealed that each particle continuously undergoes small local rotations followed by rapid orientation changes, often accompanied by lateral movement. The noise variance in the individual frames of the movie exceeds the signal variance approximately fivefold, despite the strong scattering from the heavy Pt atoms (Movie S3 and S4 show 200 raw TEM images). Although sufficiently thin to observe atomic detail, the liquid between the graphene sheets introduces a granular background, making it difficult to distinguish the facets of the nanocrystal in the individual frames. To enhance the image contrast and allow accurate 3D orientation determination, we averaged the image series in sets of five consecutive frames, resulting in a time resolution of ~100 ms. After frame averaging, we carefully scanned the image series to remove a small fraction (~20%) of those averages that did not show any lattice contrast because the particles had moved out of the narrow ideal focal plane of the aberration corrected microscope.

Initial 3D models were obtained using our recently developed framework (PRIME) for ab initio single-particle 3D reconstruction (11). The standard technique used in biological single-particle cryo-EM (10) assigns each image the single best matching orientation, as determined by correlation matching to a gallery of reference images, obtained by projecting an a priori available 3D reference model. Two fundamental limitations of the standard technique are the bias introduced by the initial 3D model and the lack of mechanisms for modeling the alignment errors when data are noisy and the model is of poor quality. These limitations may be quite significant when reconstructing nanocrystals, because every particle is different and the particle population cannot be averaged, as in traditional single-particle EM. The individual frames also have a low SNR because of the relatively low per-frame electron dose and because of the granular background introduced by the liquid. PRIME overcomes these drawbacks by utilizing weighted orientation assignment and stochastic optimization for determination of an optimal orientation weight distribution without any a priori information about the nanoparticles.
To initialize the 3D reconstruction process, we assigned the random orientations to images, producing a feature-less spherical density map. The random orientations were refined by stochastic optimization of the correlation between the images and re-projections of the density map, using information from 30 Å to 3 Å and a discrete search space of orientations. The resulting initial model had a resolution of 2.5 Å according to the 0.143 Fourier shell correlation (FSC) criterion (21). We extended the PRIME algorithm by introducing a continuous orientation search space and used stochastic optimization to determine a continuous distribution of weights that related the continuous distribution of orientation parameters to the 3D reconstruction. Each round of the PRIME iterative alignment procedure involved determination of orientation weights for all particle images, followed by a weighted 3D reconstruction by direct Fourier reconstruction using a Kaiser-Bessel interpolation kernel. A few hundred iterations were executed, and in every round the FSC was calculated and used to construct a 3D Wiener filter that filters the map such that the optimal SNR is obtained at the current resolution (22). The resolution of the final refined maps was measured to 2.10 Å (particle 1) and 2.14 Å (particle 2), respectively.

Even though the FSC methodology provides an accurate measure of the resolution when the reference structure used for matching has been appropriately low-pass filtered, it does not ensure against grossly incorrect structures. In order to validate our structures, we determine the agreement between the individual images used for reconstruction and the corresponding re-projections of the reconstructed 3D map. All image-re-projection pairs (Fig. S3) were generated for the two reconstructions, and the Fourier Ring Correlation (FRC) (23) was calculated between all pairs. The average FRC was larger than 0.143 to a resolution of 1 Å and showed a distinct peak spanning the 1-2 Å resolution region (Fig. S3). This peak is due to the correlation between atomic densities in the re-projections and atomic densities in the images. We concluded that our reconstructions showed excellent agreement with the images. The spatial resolution is higher for particle 1 which has a
larger number of frames, indicating that the current resolution can be improved by acquisition of longer movies that cover a wider range of rotational orientations.

We had anticipated that the Pt nanocrystals would have at least two-fold rotational symmetry, perhaps even cubic symmetry. Remarkably, the reconstructions appeared asymmetrical and attempts to apply C2, C4, C5, and D2 point-group symmetry by aligning the images to the principal symmetry axis and doing symmetric orientation refinement failed to improve the correlation between the re-projections and the images. This suggests that the Pt nanocrystals do not possess icosahedral, cubic, or pentagonal symmetry but are intrinsically asymmetrical. Reconstruction by the traditional single-particle cryo-EM technique, using an initial model based on a faceted face-centered-cubic (FCC) nanoparticle, would suffer severe initial model bias and would not reproduce the true asymmetrical multi-domain structure.

Our reconstructions of particles 1 and 2 revealed different asymmetrical crystal structures with the same underlying principle: a dense central disc of atomic planes (the core) with conical extensions anchored on each side, protruding in opposing and orthogonal directions with respect to the equatorial plane (see schematics in Fig. 2 (A) with the lattice in different crystal domains colored blue and orange). Despite this similarity, the reconstructed 3D structures of the two Pt particles show interesting differences. First, the atomic arrangements on the surfaces observed in the EM density maps of particle 1 and 2 were distinct, as shown in Fig. 1 (C) and 2 (E). Second, the two particles showed different degrees of crystallinity in each domain. Whereas straight {111} crystal planes in three domains of particle 1 are shown throughout the cross-sectional images along the mid-vertical plane (Fig. 2 (B)) and vertical planes at different depths (Fig. S4), particle 2 shows more disordered internal structures within the domains. Also in particle 1, the conical protrusions have {111} atomic planes tilted with respect to the {111} atomic planes in the core. Particle 2 exhibits protrusions with a larger degree of disorder compared to the well-aligned {111} lattices in the particle 1 protrusions. Views of the
reconstructions perpendicular to the equatorial plane (Fig. 2 (C)) and a schematic illustration (Fig. 2 (D)) show the overlaid lattices of the core (blue lines) and protrusions (yellow lines) with different tilting angle for particle 1 (14°) and 2 (7°). The cross-sectional views along the equatorial plane (Fig. 2 (E)) for particle 1 and 2 show similar arrangements of the \{111\} lattice planes, but cross-sectional images along the horizontal planes below and above the equatorial plane for the two particles (particle 1 in Fig. 3 (C), (D), and (E) and particle 2 in Fig. S5) indicate the two particles are assembled by multiple domains but in unique geometries. The multiple domains and twisted grain boundaries that are present in the reconstructions are similar to previous observations of Pt nanocrystal growth trajectories, where small particles joined along surfaces with low ligand coverage (3). The multi-domain arrangement is also supported by other tomography reconstructions of larger Pt nanocrystals containing multiply twinned domains with decahedral symmetry and central screw dislocations (3, 5). Multi-domain structures are common in many other colloidal metal nanoparticles, which likely evolve due to multiple coalescence events during growth (3, 24–26). Our observation of heterogeneously structured Pt nanoparticles formed in the same solution confirms that individual particles from the same synthesis follow different nucleation and growth trajectories.

Fig. 3 (A) presents a 3D density map with colored sections indicating the upper (blue), core (gray) and lower (purple) domains of particle 1. Fig. 3 (B) shows a cross-section perpendicular to the equatorial plane with the tentative atomic positions (different colored dots in each domain) indicating \{111\} lattice planes of FCC crystal that have repetition in every three crystal planes in all three crystal domains. Atoms closer to the surface seem to deviate further from a perfect FCC structure. This is presumably explained by the fact that surface atoms are prone to relax excess free energy due to lack of coordination and stabilization by surface ligand binding. In addition, the interface between the domains is disordered and not flat, a general consequence of the reduction in surface energies expected for nanoscale crystals relative to their bulk counterparts. The locations of three
cross-sections along horizontal planes named cross-section 1, equator, and cross-section 2 are indicated in Fig. 3 (A). Cross-sections 1 and 2 are positioned near the interface between the central disk and the upper/lower conical protrusions, respectively. Cross-section 1 exposes two facing surfaces from the upper and core domains (blue and gray densities in Fig. 3 (C), respectively). Cross-section 1 shows a (100) surface with red dashed lines that trace the {111} planes exposed on the (100) surface. The cross-section at the equator (Fig. 3 (D)) exhibits a (110) surface, and blue dashed lines indicate the {111} planes exposed to the (110) surface. The red and blue lines are mapped onto the pseudo-atomic illustration of (100) and (110) surfaces with the proper orientation (a 14° rotation angle) in the right image of Fig. 3 (D). At cross-section 2, near the interface between the central disk and the lower conical protrusion, a surface structure with pseudo (100) patterns traced by red dotted lines is exposed from the core and lower domains (gray and purple densities in Fig. 3 (E), respectively), which deviate from the ideal FCC structure. Fig. 3 shows that the conical protrusions and the core join along (100) and (110) surfaces with distortions at the interface. Multiple domains merging along the low index crystal planes, such as (100) and (110), are presumably formed by coalescence events between small particles during the particle growth as a route to minimize excess surface energy. We have previously observed a similar scenario: two small Pt particles join along the (111) surfaces during growth (3). Presumably, coalescence along the low index surfaces and the following evolution of the interface structure are mechanisms by which the nanocrystals reduce free energy.

To examine whether there is a thermodynamic rationale for the multi-domain structures that we observed, we computed the free energies for the grain boundary formation and for the ligand exposed surfaces. This was done using the Frenkel-Ladd method (27) for an embedded atom model of Pt (28), using an appropriate thermodynamics integration path (Fig. S6). We found that for low-angle-misalignments, like those observed in particle 1 (14° rotation angle between {111} planes exposed on (110) and (100) surfaces from the central disc and upper domain in Fig. 3), the grain boundary free energy for a
nanoparticle with \( N = 1200 \) atoms is 0.3 J/m\(^2\), and increases to 0.55 J/m\(^2\) for misalignment angles of up to 59\(^\circ\) (Fig. 4). Small rotational relaxation of the crystal grains is found to be energetically viable these interfaces, which may explain the orientation of the side protrusions in particle 1 with respect to its central section.

The surface free energy for the ligand-exposed interfaces was computed to be 2.8 J/m\(^2\) as averaged over the (100) and (111) surfaces, weighted appropriately for the cuboctahedral shape. The disparity of scales between the grain boundary free energies and the much larger exposed surface free energies confirms that there is a large thermodynamic driving force for coalescence, even when such events result in grain boundary formation. As the free energy gain upon coalescence is much larger than thermal energies, initial aggregations is likely irreversible. The resultant grain boundaries are then kinetically arrested over laboratory time scales (additional information is found in Supplementary Materials).

We show that near-atomic (~2 Å) resolution 3D reconstructions of metallic nanocrystals are possible to produce using the SINGLE methodology, which can now be applied to investigate the structural principles underlying the assembly and transient morphology of any stable, small nanoparticle in solution. We envision that the SINGLE method can be applied directly to in-situ 3D structural studies of many other kinds of solvated particles.
Figures:

**Fig. 1.** Schematic illustration of *in situ* TEM imaging of Pt nanocrystals freely rotating in a graphene liquid cell (GLC) and 3D EM density maps calculated from individual Pt nanoparticles in solution. (A) A movie of the single rotating Pt nanocrystal provides 2D projected TEM still snapshots in many orientations for ab initio particle reconstruction. (B) EM density map obtained from the 3D reconstruction of particle 1. The orientation of the particle is aligned to expose \{111\} planes of the core domain. Three distinct crystal domains can be identified. (C) 3D EM density map of particle 1 with alternative viewing angles. (D) EM density map obtained from the 3D reconstruction of particle 2. (E) 3D
EM density map of particle 2 with alternating view angles. Each panel in (C) and (E) presents the two particles with the same angle and direction with respect to the orientations in (B) and (D). Scale bars represent 0.5 nm.
Fig. 2. The underlying structural principle of the small Pt nanoparticles studied here. (A) Schematic illustration of the front view of particle 1 and 2 shown in Fig. 1. Both particles are composed of a dense central disc of atomic planes (blue lines) with conical protrusions (orange lines) anchoring on each side of the disc. (B) Cross-sectional view of the EM density map of particle 1 and 2 along the vertical plane. (C) View orthogonal to (A), showing the overlaid lattices. Scale bar represents 0.5 nm. (D) Schematic illustration
of the top view of particle 1 and 2 shown in (C). (E) Cross-sectional view of the EM density map of particles 1 and 2 along the equatorial plane.

Fig. 3. Cross-sectional study of particle 1. (A) 3D density map of particle 1 with color coding to highlight the three sections. Cross-section 1 and 2 are in arbitrary positions near crystal domain interfaces. Scale bar represents 0.5 nm. (B) Slab through the 3D reconstruction of particle 1 along the vertical plane with tentative atomic positions indicated. ABC repeats of \{111\} planes are visible. (C) Slab along cross-section 1. The exposed (100) surface of the FCC Pt crystal is shown consistently in both exposed surfaces. Intersections with \{111\} planes in the top domain are displayed by red dashed lines. (D) Slab along the equatorial plane of (A) exposes a (110) plane. The intersections with \{111\} planes are shown by blue dashed lines. Pseudo-atomic structure (right) demonstrates the rotation angle (14°) between the (100) and (110) surfaces from the top and bottom domains, respectively. (E) Slab along cross-section 2. The disordered (100) surface of the FCC Pt crystal is shown consistently in both exposed surfaces.
Intersections with pseudo \{111\} planes in the bottom domain are displayed by red dashed lines.

**Fig. 4.** Twist grain boundary free energies as a function of misalignment angle for the (110)-(100) crystal planes of a $N = 1135$ atom nanocrystal. Shaded regions indicate error bars of 1 and 2 standard deviations. The inset shows a relaxed nanocrystal with an initial misalignment angle of 14°. The non-flat grain boundary is located in the center of the nanocystal. Images around the perimeter show the two relaxed planes at the grain boundary from the 100 (red) and 110 (white) grains for different misalignment angles.
References and notes:


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Supplementary Materials:

Captions for Movies S1 to S4
Molecular Dynamics Simulation
Materials and Methods
Figs. S1 to S9
References (30 – 38)
Movies S1 to S4