



# Modeling muscle function using experimentally determined subject-specific muscle properties

## Citation

Wakeling, James M., Chris Tijs, Nicolai Konow, Andrew Biewener. "Modeling muscle function using experimentally determined subject-specific muscle properties." *Journal of Biomechanics* 117 (2021): 110242. DOI: 10.1016/j.jbiomech.2021.110242

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1 **Original Article**

2

3 **Title: Modeling muscle function using experimentally determined subject-specific muscle**  
4 **properties.**

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16

17 **Word Count: 3483**

18 Introduction to Discussion, excluding references and equations

19 **Abstract**

20

21 Muscle models are commonly based on intrinsic properties pooled across a number of  
22 individuals, often from a different species, and rarely validated against directly measured muscle  
23 forces. Here we use a rich data set of rat medial gastrocnemius muscle forces recorded during *in-*  
24 *situ* and *in-vivo* isometric, isotonic, and cyclic contractions to test the accuracy of forces  
25 predicted using Hill-type muscle models. We identified force-length and force-velocity  
26 parameters for each individual, and used either these subject-specific intrinsic properties, or  
27 population-averaged properties within the models. The modeled forces for cyclic *in-vivo* and *in-*  
28 *situ* contractions matched with measured muscle-tendon forces with  $r^2$  between 0.70 and 0.86,  
29 and root-mean square errors (RMSE) of 0.10 to 0.13 (values normalized to the maximum  
30 isometric force). The modeled forces were least accurate at the highest movement and cycle  
31 frequencies and did not show an improvement in  $r^2$  when subject-specific intrinsic properties  
32 were used; however, there was a reduction in the RMSE with fewer predictions having higher  
33 errors. We additionally recorded and tested muscle models specific to proximal and distal  
34 regions of the muscle and compared them to measures and models from the whole muscle belly:  
35 there was no improvement in model performance when using data from specific anatomical  
36 regions. These results show that Hill-type muscle models can yield very good performance for  
37 cyclic contractions typical of locomotion, with small reductions in errors when subject-specific  
38 intrinsic properties are used.

39

40

## 41 Introduction

42 Quantifying muscle forces is necessary for understanding how movements are powered  
43 and controlled, yet muscle force is challenging to measure directly during voluntary movements.  
44 Some studies have recorded forces from common tendons that originate from multiple muscles  
45 (Komi, 1987; Gregor et al. 1987; Hoffer et al. 1987; Biewener and Blickhan, 1988; Finni et al.  
46 2000; Daley and Biewener, 2003); fewer studies have recorded forces directly from distinct  
47 tendons (Biewener et al., 1998; Eng et al., 2019; Herzog et al., 1993; Roberts et al., 1997;  
48 Walmsley et al., 1978). However, tendon and thus muscle forces for the majority of species,  
49 muscles and movements have not yet been recorded; and this is particularly the case for in  
50 humans. When muscle forces cannot be directly measured, they are often estimated using  
51 computational models (Zajac, 1989). One such model is the Hill-type muscle model that has seen  
52 widespread use in more recent years for both *in-situ* (James et al. 1996; Sandercock and  
53 Heckman, 1997; Wakeling and Johnson, 1999; Perreault et al. 2003; Wakeling et al. 2012;  
54 Millard et al. 2013) and *in-vivo* studies (Hodson-Tole and Wakeling, 2009; Gerus et al. 2012;  
55 Lee et al. 2013; Dick et al. 2017). Hill-type muscle models are now embedded in many  
56 musculoskeletal simulations of movement to understand muscle use during human movements in  
57 health and disease (for review: Seth et al. 2018).

58 Forces predicted by Hill-type muscle models are sensitive to the intrinsic muscle  
59 properties used in the model. Muscles show individual variation in pennation angle (Wickiewicz  
60 et al. 1983), muscle quality (isometric stress: Medler, 2002), passive stiffness (Azizi, 2014),  
61 intrinsic contraction speed (Sadoyama et al., 1988; Medler 2002), and excitability; with this  
62 variation often being caused by ageing (Lauretani et al. 2003), disuse (Narici and de Boer, 2011;  
63 Wisdom et al. 2014) and disease (Smith et al. 2019). Previous studies have shown how subject-

64 specific optimal lengths for fascicles and tendons can improve the accuracy of predicting forces  
65 from muscle models (Li et al. 2009; Gerus et al. 2012). However, it is not known how subject-  
66 specific fascicle force-length and force-velocity relations would additionally affect the predicted  
67 forces, due to the difficulty in measuring these parameters for model validation. In this study we  
68 investigate whether the forces predicted by Hill-type muscle models are improved when the  
69 models use these subject-specific intrinsic properties. We test these models on *in-vivo* and *in-situ*  
70 data obtained from a rat ankle plantarflexor muscle (medial gastrocnemius, MG), a muscle that  
71 allows direct measurements of the muscle force from the MG tendon. We test these predictions  
72 for contractions over a range of complexity: from *in-situ* isotonic, steady monotonic and cyclic  
73 work-loop contractions to unrestrained *in-vivo* locomotion.

74 Hill-type muscle models are commonly implemented with a single fascicle length and  
75 pennation that is assumed to represent the whole muscle that it is emulating (Zajac, 1989).  
76 However, skeletal muscles have heterogeneous architecture, and show regional variations in  
77 pennation angle, fascicle length, strain, fibre-type properties, and activation (eg. De Ruiter et al  
78 1995, Ahn et al., 2018; Azizi & Deslauriers 2014; Konow et al., 2010). Previously we have  
79 shown that Hill-type muscle models that have multiple contractile elements with different  
80 intrinsic properties (but the same architecture) predict more accurate forces at high velocity (Lee  
81 et al. 2013) and predict reduced metabolic costs of contraction (Lai et al. 2018). It is possible that  
82 model refinements that consider the regional differences in architecture may additionally  
83 improve the predicted forces. However, this has not been tested against directly measured force.  
84 In this study we measure *in-vivo* excitations and length changes in the proximal and distal  
85 regions of the rat MG, and test whether the forces predicted from different regions of the muscle  
86 would differ, whether they differ from the forces predicted from measures of the whole muscle

87 belly, and how well these predictions match experimentally measured forces on the tendon  
88 during *in-situ* and *in-vivo* contractions.

89 We tested the following hypotheses:

- 90 1) That model-predictions of muscle forces will be worse at the highest contractile  
91 frequencies but not the greatest magnitude of force;
- 92 2) That modeled muscle forces based on subject-specific muscle properties will result in  
93 significantly improved predictions of *in-vivo* force patterns compared with forces  
94 modeled using muscle properties averaged across a population; and
- 95 3) That region-specific fiber strain and EMG will result in significantly improved  
96 predictions of *in-vivo* forces compared to measures from the whole muscle belly.

97

98

99 **Methods**

100 *Animals*

101 All procedures were carried out under approval by the Harvard University (FAS)  
102 Institutional Animal Care and Use Committee (protocol 20-09), according to USDA guidelines.  
103 Seven male Sprague Dawley rats (body mass:  $369 \pm 87$  g; Table S1) were trained for three weeks,  
104 using verbal encouragement and light gusts with an air-duster to locomote at three different gaits/  
105 inclines on a motorized treadmill.

106

107 *In vivo measurements*

108 Each animal was anesthetized (isoflurane gas to effect; 1-2%, via mask). Two sets of  
109 bipolar silver wire electromyography (EMG) electrodes and four 1-mm sonomicrometry  
110 transducers were inserted into the medial gastrocnemius (MG), and a custom-fabricated ‘leaf-  
111 spring’ force transducer was attached to the MG tendon using sterile surgery procedures (Fig.  
112 S1; see (Eng et al., 2019; Konow et al., 2020; Richards and Biewener, 2007). The pairs of  
113 sonomicrometry crystals were placed along proximal and distal fascicle axes (8-10mm apart,  
114 spanning ~80-85% fascicle length). Misalignment of crystals never exceeded  $5^\circ$ , yielding errors  
115 in fascicle strain due to misalignment  $<1\%$ . The separation of the proximal and distal-most  
116 crystals provided measurement of the length of the muscle belly that excluded the tendon.  
117 Analgesics (Flunixin meglumine, 2 mg/kg) were administered twice over the 48 hours following  
118 surgery.

119 After surgery recovery, recordings were obtained as animals moved at the steadiest  
120 possible speed (walk  $\sim 0.3$  m  $s^{-1}$ ; trot  $\sim 0.8$  m  $s^{-1}$ ; gallop  $\sim 1.0$  m  $s^{-1}$ ) on the level and  $14^\circ$  upslope.

121 Electrode and transducer signals were sampled at 5 kHz (MP150 16-bit A/D converter, Biopac  
122 Systems, Inc., Goleta, CA, USA).

123

#### 124 *In-situ measurements*

125 After *in-vivo* experiments, animals were re-induced on isoflurane gas. A femur clamp  
126 was secured to a stereotaxic frame and the foot was zip-tied to a plastic plate on the frame. The  
127 MG and the sciatic nerve were exposed using blunt dissection. A cuff electrode (inter-pole  
128 spacing of 5.0 mm) was secured around the sciatic nerve, and all sciatic branches distal to the  
129 cuff electrode were severed, except for the one innervating MG (Tijs et al., 2014). The calcaneus  
130 was cut with the MG tendon intact and attached to the lever arm of a servomotor (Fig. S1A). The  
131 muscle and exposed tissue were immersed in mineral oil pooled in a loosened skin flap and  
132 regulated at  $35\pm 1^\circ\text{C}$ .

133 Isometric force-length (FL) and isotonic force-velocity (FV) curves were constructed for  
134 maximal (amplitude: 2-3 V) and submaximal (amplitude:  $\sim 1\text{V}$ ) stimulations to the nerve  
135 (1.5mA; frequency, 125Hz; pulse width, 0.2ms; train duration: 300ms) via a Grass S48  
136 stimulator. Isotonic shortening contractions relied on servomotor force-control, with contractions  
137 crossing the isometric optimal length ( $l_0$ ) for both proximal and distal fascicles. As  $l_0$  is affected  
138 by muscle activation (Holt and Azizi, 2016; Rack and Westbury, 1969; Rassier et al., 1999), we  
139 first determined  $l_0$  for each region independently. Three-minute rest periods between successive  
140 muscle contractions were used to minimize muscle fatigue. Experimental data were only used for  
141 analysis if tetanic force remained  $\geq 90\%$  of the maximum isometric force  $F_0$  during the *in-situ*  
142 tests.



143 *In-situ* forces from the MG were measured during cyclic work-loop contractions. The  
144 muscle length trajectories were set to match those during *in-vivo* upslope gallop strides of a  
145 single rat using 3D fluoroscopy (Konow et al., 2020; peak amplitude of 1.2mm and cycle  
146 frequency of 3.5Hz); with stimulus onset 60ms before peak MTU length and EMG duty cycle  
147 46%, as per *in-vivo* gallop data (Eng et al. 2019). This baseline work-loop condition was then  
148 varied in cycle frequency (2 to 10Hz) and peak-to-peak amplitude (0.6 to 2.4mm), with some  
149 conditions being low amplitude and high frequency, and others being high amplitude and low  
150 frequency. All conditions were recorded for maximal and submaximal stimulations.

151 MG force and EMG signals were sampled at 4kHz; and muscle belly, proximal fascicle,  
152 and distal fascicle lengths were sampled at 520Hz via the sonomicrometer. Animals were  
153 euthanized after the experiment (pentobarbital sodium overdose, IP). The MG was excised post-  
154 mortem, weighed and bisected in the sagittal plane to measure whole muscle belly length and  
155 total length of the proximal and distal fascicles, as well as their resting pennation angle  $\beta_0$  (Table  
156 S1). These measurements were used to correct for the length of fascicles and muscle not spanned  
157 by the sonomicrometry crystals. Lastly, tendon transducer output was calibrated to ergometer  
158 force measured for a series of *in-situ* isometric tetanic contractions.

159

### 160 *Modelling isometric and isotonic muscle force*

161 We took the approach of initially determining phenomenological relations to describe the  
162 intrinsic force-length and force-velocity characteristics of the muscle. We then used these  
163 intrinsic properties, combined with measures of the time-varying excitation, length and velocity  
164 of the muscle during *in vivo* and *in situ* contractions to predict what the muscle forces would be  
165 during these contractions, and compared these predicted forces to independently measured

166 forces. We used models to predict forces from the muscle belly (using the length and velocity of  
 167 the muscle belly, and the mean EMG-intensity from both muscle regions), and from either the  
 168 proximal or distal region of the muscle (using fascicle length and velocity and EMG-intensity  
 169 from that region).

170 The peak active force from the FL tests gave the maximum isometric force  $F_0$  and the  
 171 optimal length  $l_0$  for the proximal and distal fascicles and the muscle belly. The proximal  
 172 fascicle, distal fascicle and muscle belly lengths were normalized  $\hat{l}$  to their respective optimal  
 173 lengths for each rat.

174 The FL data were fit to an active  $\hat{F}_a(\hat{l})$  and a passive  $\hat{F}_p(\hat{l})$  model (normalized to  $F_0$ )  
 175 using least squares minimization:

$$176 \quad \hat{F}_a(\hat{l}) = e^{-\left|\frac{\hat{l}^w - 1}{s}\right|^r} \quad (\text{equation 1})$$

177 where  $r$  determines roundness,  $w$  determines skewness and  $s$  determines width of the force-  
 178 length relationship (Otten, 1985; Hodson-Tole and Wakeling, 2009), and

$$179 \quad \hat{F}_p(\hat{l}) = e^{(c_1 + c_2 \hat{l})} \quad (\text{equation 2})$$

180 where  $c_1$  and  $c_2$  are empirical coefficients.

181 The FV data from the concentric ( $\frac{d\hat{l}}{dt} < 0$ ) isotonic contractions were fit to a piecewise  
 182 function  $\hat{F}_v\left(\frac{d\hat{l}}{dt}\right)$ , normalized to  $F_0$ , using least squares minimization (Lee et al. 2013):

$$183 \quad \hat{F}_v\left(\frac{d\hat{l}}{dt}\right) = 0 \quad \text{for} \quad \frac{d\hat{l}}{dt} < -1 \quad (\text{equation 3})$$

$$184 \quad \hat{F}_v\left(\frac{d\hat{l}}{dt}\right) = \frac{1 + \left(\frac{d\hat{l}}{dt}\right) \frac{1}{v_0}}{1 - \left(\frac{d\hat{l}}{dt}\right) \frac{1}{kv_0}} \quad \text{for} \quad -1 \leq \frac{d\hat{l}}{dt} < 0$$

$$185 \quad \hat{F}_v\left(\frac{d\hat{l}}{dt}\right) = 1.5 - \frac{0.5 \left[1 - \left(\frac{d\hat{l}}{dt}\right) \frac{1}{v_0}\right]}{1 + 7.56 \left(\frac{d\hat{l}}{dt}\right) \frac{1}{kv_0}} \quad \text{for} \quad \frac{d\hat{l}}{dt} \geq 0$$

186 where  $k$  is the curvature of the force-velocity relationship, and  $v_0$  is the maximum unloaded  
 187 contraction velocity. For the eccentric portion of the FV curve ( $\frac{dl}{dt} \geq 0$ ) curve parameters were  
 188 taken from Otten (1987): note these parameters were not specific to the individual rats.

189 An intensity envelope was fit to the EMG signals using an EMG-specific wavelet  
 190 analysis (Lee et al. 2011). The muscle excitation was taken as the square-root of this EMG-  
 191 intensity and normalized to the maximum excitation that occurred across all conditions for each  
 192 recording channel. The excitation was converted to an activation signal using three coupled  
 193 differential equations as a transfer function (Lee et al. 2011), with rat-specific time-constants  
 194 calculated from MG twitches recorded in the rat: these were general time-constants fit to pooled  
 195 data from both proximal and distal EMG-intensities. Muscle activations  $\hat{a}(t)$  as a function of  
 196 time  $t$  were calculated separately for the EMG from the proximal and distal locations of the  
 197 muscle, and the mean of these activations was used to model the forces for the muscle belly.

198 Muscle forces  $F_m$  for both the *in-situ* work-loop and the *in-vivo* locomotion data were  
 199 calculated as follows:

$$200 \quad F_m = F_0 \left[ \hat{a}(t) \hat{F}_a(\hat{l}) \hat{F}_v\left(\frac{d\hat{l}}{dt}\right) + \hat{F}_p(\hat{l}) \right] \hat{F}_\beta$$

201 We assumed that the thickness of the muscle belly was constant during the experiment  
 202 (Lee et al. 2013) and calculated it from the post-mortem fiber length and pennation  $\beta_0$ . The time-  
 203 varying pennation angle  $\beta_i$  was calculated from the fibre length during contraction and belly  
 204 thickness. Given that the FL properties were measured using the fiber-lengths, but these fibers  
 205 were already at a pennation angle relative to the line-of-action of the muscle belly, the effect of  
 206 the time-varying pennation angle  $\beta_i$  during contraction was factored in by  $\hat{F}_\beta$ , where:

$$207 \quad \hat{F}_\beta = \frac{\cos(\beta_i)}{\cos(\beta_0)}$$

208 for the force predictions from the proximal and distal fascicles, and

$$209 \quad \hat{F}_\beta = \frac{\cos(\beta_0)}{\cos(\beta_i)}$$

210 for the force predictions from the muscle belly length.

211 We separated the *in-situ* data into work-loop cycles, and *in-vivo* data by stride cycles  
212 from continuous locomotion bouts that were ~5 seconds long.

213

### 214 **Statistical analysis:**

215 The predicted muscle forces were evaluated by their coefficient of determination ( $r^2$ ) and  
216 root-mean square error (RMSE, relative to  $F_0$ ) by comparison with experimentally measured  
217 tendon forces. Values in the text are reported as mean  $\pm$  standard deviation. All statistical tests  
218 used the General Linear Model function in Systat v.12 and involved an initial full-factorial  
219 design, factoring individual, modeling method (population based vs. subject-specific), and  
220 muscle region. Model-simplifications were carried out when factors were non-significant.

221

222 To test **hypothesis 1** we used a nested factorial design to hold either the “force” or  
223 “frequency” parameter constant, while testing across conditions for the alternate parameter.  
224 Force was dictated *in-vivo* by the treadmill slope condition (Konow et al., 2020), and *in-situ* by  
225 sub- or supra-maximal muscle stimulation. Frequency was dictated *in-vivo* by gait condition, and  
226 *in-situ* by varying work-loop frequency. Tests were run separately for the *in-situ* and *in-vivo*  
227 conditions, and within each condition, for the population average (All) and subject specific (Rat)  
228 methods of modeling.

229 To test **hypothesis 2** we isolated the effect of the method factor to discriminate the effect  
230 of using subject-specific (Rat) as opposed to population averages (All) muscle activation and  
231 strain-trajectories when modeling muscle force.

232 To test **hypothesis 3** we used post-hoc testing with pair-wise comparisons of  $r^2$  and  
233 RMSE for the muscle's proximal and distal regions, and the whole muscle belly.

234

## 235 **Results**

236 Consistent active isometric FL curves were obtained across animals for proximal and  
237 distal MG regions, as well as for the whole muscle (Fig. 1A-C). The active FL curve was  
238 narrower for the muscle belly compared with the proximal and distal regions. The passive FL  
239 curves, however, were more variable across animals (Fig. 1D-F), in large part due to variable  
240 disruption of adjacent fascial compartments needed to isolate the MG to obtain *in-situ* FL and  
241 FV measurements. For isotonic FV relationships (Fig. 1G-H), the normalized maximum  
242 shortening velocities were significantly different between regions ( $F_{2,10}=14.88$ ;  $p=0.001$ ) without  
243 effect of individual ( $F_{5,10}=3.32$ ;  $p=0.050$ ). Maximum shortening velocities of the muscle belly  
244 ( $5.06\pm 0.98\text{ s}^{-1}$ ) were lower than for the proximal ( $10.82\pm 3.01\text{ s}^{-1}$ ;  $p<0.01$ ) and distal ( $9.82\pm 3.22\text{ s}^{-1}$ ;  
245  $p<0.05$ ) region, while the difference between the proximal and the distal region was not  
246 significant ( $p>0.05$ ) These FL and FV relations were determined before, and independently of,  
247 the evaluation of the Hill-type model force predictions of the cyclic *in situ* contractions and the  
248 *in vivo* behaviours.

249 In general, the time-varying length and activation resulted in excellent model predictions  
250 of MG force for both the *in-vivo* locomotor conditions (Fig. 2A-C) and the *in-situ* work-loops  
251 (Fig. 2D). However, these model predictions were not as good as for the steady FL and FV data

252 (Fig. 3). When averaged across the proximal, distal and muscle belly rat-specific models, the  
253 mean  $r^2$  for the model predictions was  $0.996 \pm 0.004$ ,  $0.857 \pm 0.100$  and  $0.699 \pm 0.207$  for the  
254 steady, cyclic *in-situ*, and *in-vivo* conditions, respectively, and the mean RMSE for the model  
255 predictions was  $0.016 \pm 0.013$ ,  $0.101 \pm 0.050$  and  $0.133 \pm 0.063$  and for the steady, cyclic *in-situ*,  
256 and *in-vivo* conditions, respectively. The prediction-accuracy of forces became worse with each  
257 increase in *in-vivo* stride frequency (walk to gallop in Figs. 4 and S3) (GLM:  $F_{2,1179} = 107.99$ ;  
258  $p < 0.001$ ) and *in-situ* work-loop frequencies (Figs. S2 and S3) ( $F_{5,693} = 35.98$ ;  $p < 0.001$ ), but  
259 generally exhibited similar or lower  $r^2$ , and greater RMSE with increased *in-vivo* force as the  
260 locomotor grade changed from level to upslope, and increased *in-situ* stimulation intensity.

261 The quality of model-predictions of forces, as shown by their  $r^2$ , did not substantially  
262 change between models with subject-specific muscle parameters compared to the population  
263 means (Fig. 5A). Indeed, the statistical tests for *in-vivo* showed no significant main effect of the  
264 model type (subject-specific or population-averaged parameters) on the  $r^2$  values ( $F_{1,1175} = 0.01$ ;  
265  $p > 0.05$ ), but there was a statistically significant decrease of the RMSE values ( $F_{1,1179} = 12.98$ ;  
266  $p < 0.001$ ) for the predicted forces when using subject-specific data (Fig. S3. For *in-situ* work  
267 loops, the subject-specific model yielded significantly higher  $r^2$  ( $F_{1,689} = 57.62$ ;  $p < 0.001$ ). In  
268 general, we found that models using the population-averaged parameters predicted forces with  
269 higher RMSE errors more often than models that used subject-specific muscle parameters (Fig.  
270 5B).

271 The model predictions of *in-vivo* force did not improve when using region-specific fiber  
272 strain and EMG as compared to the data for the whole muscle belly (Fig. 3). In our population-  
273 average (All) modeling approach, averaging proximal and distal activation and using muscle  
274 belly length to model the muscle belly forces, in fact, yielded significantly higher  $r^2$  than using

275 regional data collected from distal or proximal compartments ( $F_{1,666} = 18.39$ ;  $p < 0.001$ ). The post-  
276 hoc test remained significant for the individual-level comparison ( $p < 0.001$ ) despite significant  
277 individual variation across the regions. None of the three corresponding RMSE comparisons  
278 were statistically significant ( $F_{1,666} = 0.007$ ;  $p > 0.05$ ).

279

## 280 Discussion

281 We show here that generally good, to excellent, fits of muscle force can be achieved by  
282 muscle models that incorporate subject-specific muscle properties, as well as when properties are  
283 pooled across individuals. Rat-specific MG models yielded fits with  $r^2$  that ranged from 0.699–  
284 0.857 for *in-vivo* locomotor and *in-situ* work-loop contractions to 0.996 for steady FL and FV  
285 contractions (Fig. 3), and the RMSE for these rat-specific muscle models ranged from 0.101–  
286 0.132 during dynamic *in-vivo* and *in-situ* contractions, respectively, to as low as 0.016 for steady  
287 monotonic contractions (relative to  $F_0$ ; Fig. 3).

288 An important aspect of our modeling approach is that the models were not optimized  
289 across all input parameters of the model to achieve a best fit. Instead, we relied on rat-specific  
290 values of measured intrinsic muscle properties (active and passive isometric FL,  $l_0$ , isotonic FV)  
291 and fascicle architecture, which were then driven by measured activations (from indwelling  
292 EMG) of the muscle during both steady and dynamic *in-vivo* and *in-situ* contractions. Using this  
293 approach, we achieved the best predictive fits from Hill-type muscle models to measured muscle  
294 forces that have been reported to date. In comparison, prior animal (cat (Perreault et al., 2003;  
295 Sandercock and Heckman, 1997); goat (Lee et al., 2013) and human (Dick et al., 2017)) muscle  
296 models have achieved fits against measured muscle forces, with  $r^2$  ranging from 0.40–0.63 and  
297 RMSE ranging from 0.10–0.23 (average ranges when they were reported relative to  $F_0$ ). It

298 should be noted that the increases in the mean  $r^2$  and decreases in mean RMSE were larger than  
299 their median values, due to the skewed nature of the distributions of  $r^2$  and RMSE. Not only did  
300 the mean and median measures improve with the rat-specific intrinsic properties (Fig. 5), but  
301 there was a reduction in the skewness of the distributions, with a reduction in the number of  
302 cases of poor model fits when compared to models that used population-averaged intrinsic  
303 properties.

304 A large source of variability, and likely error, arising from our rat MG model was the  
305 considerable experimental variation in  $l_0$  and passive FL properties measured for the MG across  
306 individual rats (Fig. 1D-F, Table 2). The resting length for elastic tissues, including tendons, is  
307 often assumed to occur at muscle  $l_0$ . Passive muscle stiffness strongly influences the time-  
308 varying force predicted by a muscle model in relation to activation and changes in muscle length  
309 (Thelen, 2003; Li et al. 2009; Gerus et al. 2012, 2015). Nevertheless, despite the considerable  
310 variation in resting length that we observed across individual muscle preparations, which likely  
311 reflected the unavoidable disruption of fascial compartments to obtain *in-situ* measurements of  
312 muscle properties (Tijs et al. 2020), the models predicted good fits (Fig. 2) for dynamic changes  
313 in force during *in-situ* work-loop and *in-vivo* locomotion contractions.

314 The predicted muscle forces showed worse fits ( $r^2$ ) and greater errors (RMSE) for the  
315 higher cycle and stride frequencies, in a manner consistent with previous reports for cyclic  
316 contractions (James et al. 1996; Wakeling and Johnston 1999, Dick et al. 2017). This speed-  
317 sensitivity may reflect the increasing importance of time-sensitive processes such as deactivation  
318 rates (Askew and Marsh, 1998) as cycle durations become shorter. Whilst errors appear greater  
319 for upslope versus level *in-vivo* gait, and maximal versus submaximal *in-situ* stimulations, it  
320 should be noted that these errors are all relative to the maximal isometric force: the errors



321 relative to the peak force during each contraction cycle were less for cycles that generated  
322 greater force. The greater  $r^2$  values for level *versus* upslope locomotion may reflect the more  
323 complex patterns of muscle fascicle strain during upslope locomotion, where the muscle  
324 experiences periods of both active lengthening and active shortening (Fig. 2; Eng et al. 2019;  
325 Konow et al., 2020). Active lengthening of a muscle likely incurs history-dependent effects that  
326 are not captured by the steady FL and FV properties used in Hill-type models. When a muscle  
327 develops force with prior active lengthening its force may be elevated compared to its isometric  
328 force at the same length (Abbott and Aubert 1952; Cavagna and Citterio 1974; Edman et al.  
329 1982; Herzog and Leonard 2002; Hisey et al. 2009), and force may be reduced when the muscle  
330 reaches that length with prior active shortening (Abbott and Aubert 1952; Marechal and Plaghki  
331 1979; Meijer et al. 1998; Herzog et al. 2000). These history-dependent effects may be included  
332 in models of muscle force (Rode et al. 2009; Herzog et al. 2012; Herzog 2014; Nishikawa et al.  
333 2012, McGowan et al. 2013; Ross et al. 2018); however, most current Hill-type models do not  
334 consider contraction history and so there is still scope for increasing model accuracy. Whilst  
335 accounting for active lengthening is important for eccentric contractions, the amount of active  
336 lengthening was small for these typical gaits in the rat and thus the scope for such model  
337 improvement is limited in this case.

338         Our modelled MG forces did not improve when region-specific length and EMG data  
339 were used, rather than muscle belly length and mean EMG intensity across the muscle. This  
340 possibly reflects the complexity and heterogeneity of the architecture and recruitment within the  
341 rat MG. Additionally, the supramaximal stimulation of the sciatic nerve for the *in situ*  
342 contractions will have induced the same recruitment for the two regions, reducing the scope for  
343 region-specific differences in force. It would seem that the whole muscle output cannot

344 necessarily be predicted from one isolated region, but rather will emerge from the outputs and  
345 interactions between the different muscle regions.

346 We were surprised to find, therefore, that modelled forces did not statistically improve  
347 when subject-specific intrinsic properties were used compared to the models with more generic  
348 population-averaged parameters: this may partly reflect the very good model fits that were  
349 already achieved with the generic models. However, it should be noted that the muscle models  
350 with subject-specific models were more likely to achieve lower errors than the generic model.  
351 Consequently, for clinical assessments there may be considerable merit in using patient-specific  
352 parameters for muscle models, which may deviate more substantially from the distribution of  
353 values across a healthy population.

354

### 355 **Acknowledgements**

356 We thank Pedro Ramirez for husbandry care of the rats. This work was funded by the National  
357 Institutes of Health [5R01-AR055648 to A.A.B. and J.M.W.].

358

### 359 **Declaration of Competing Interest**

360 The authors declare that they have no known competing financial interests or personal  
361 relationships that could have appeared to influence the work reported in this paper.

362

363

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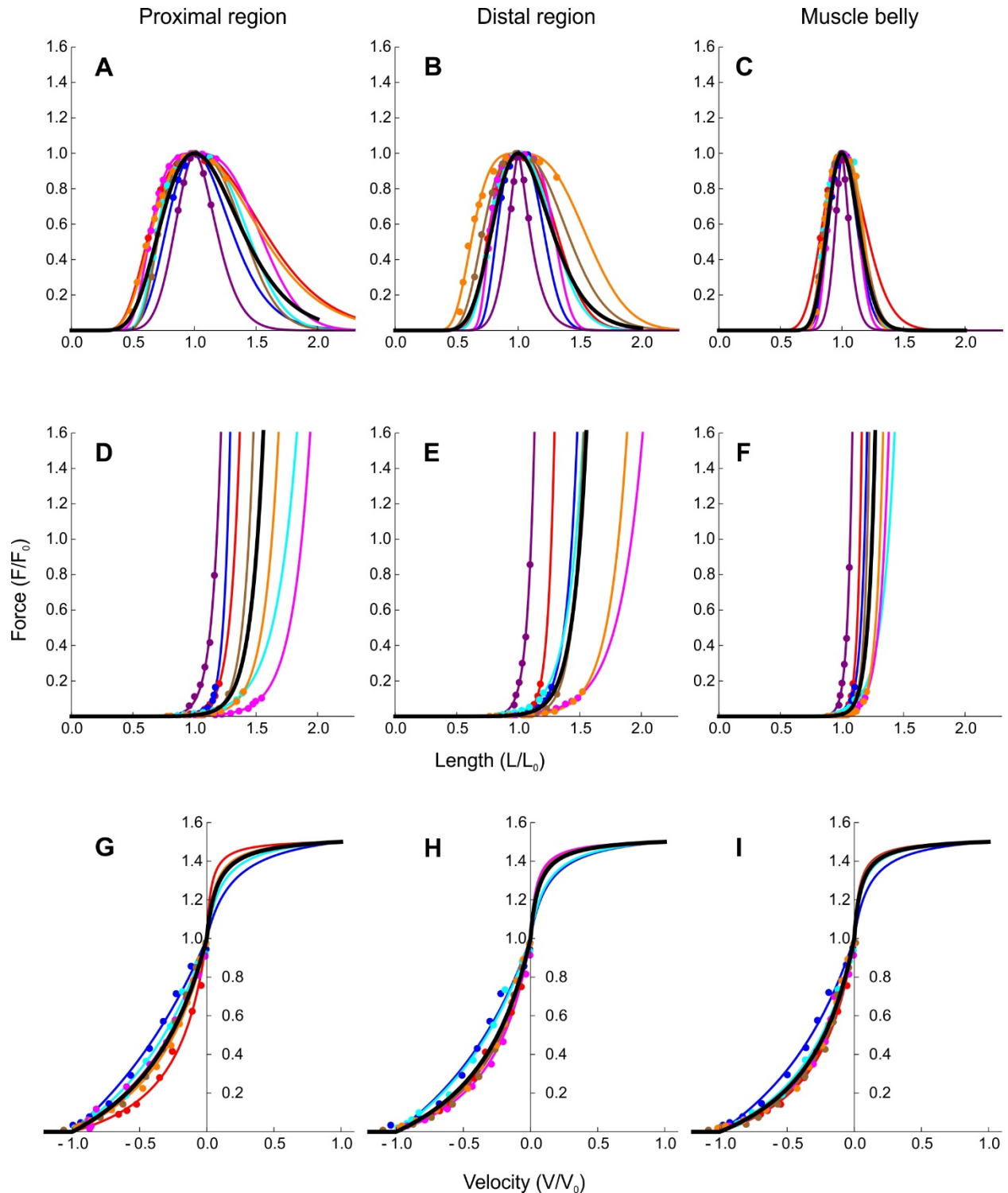


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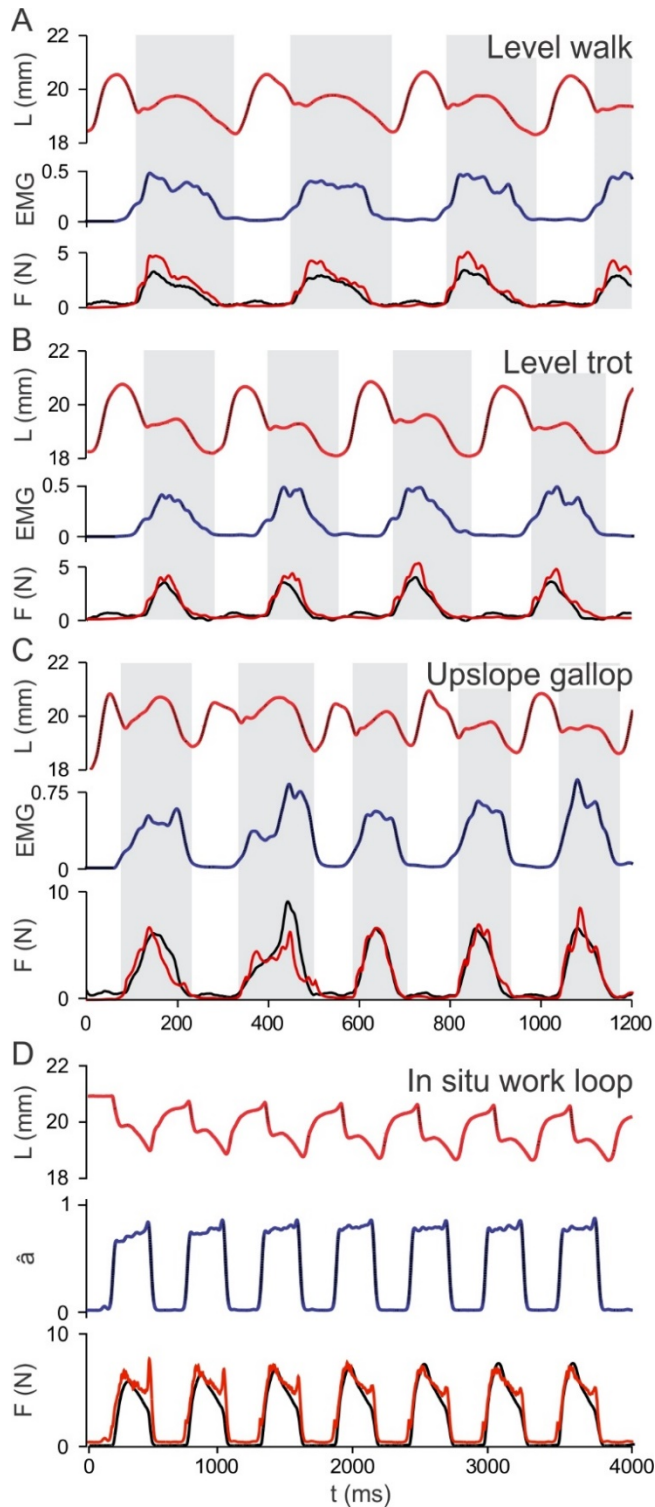
548

549 **Fig. 1. Isometric force-length (active A-C; passive (D-F), and isotonic force-velocity (G-I)**

550 **relations for the rat medial gastrocnemius.** Individual rats are distinguished by color

551 (experimental data: points and fitted models: lines). The pooled FL and FL curves (black lines)

552 were fit to all the data across the different individuals.



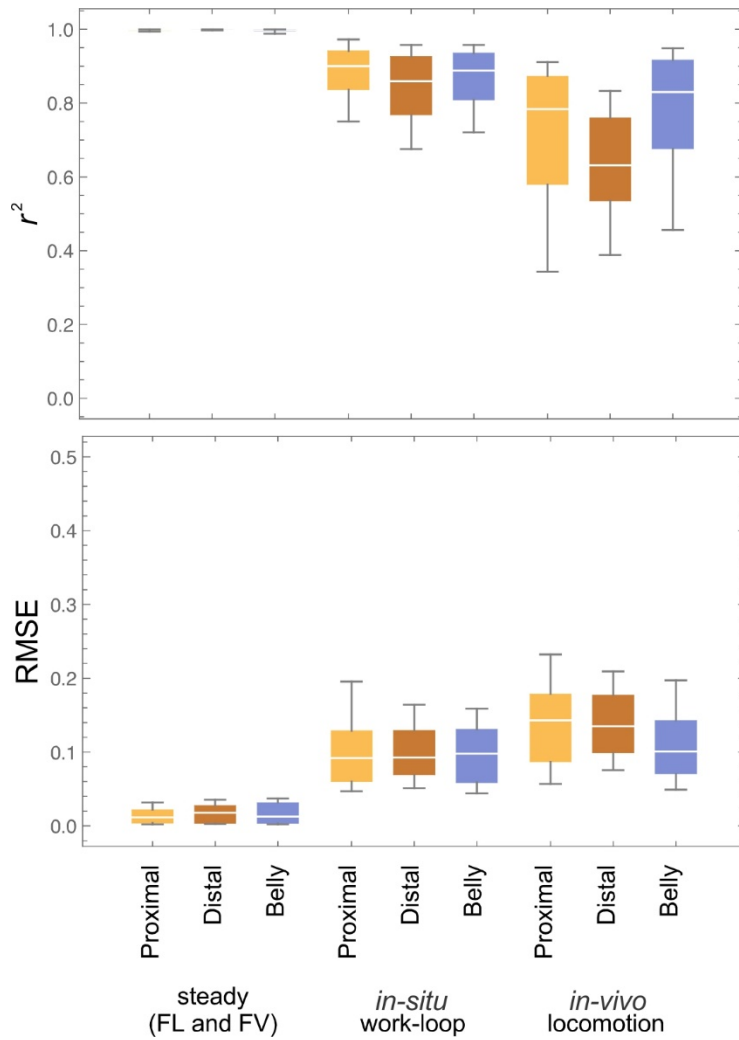
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554 **Fig. 2. Rat MG length, EMG and forces for *in-vivo* locomotion (A-C) and *in-situ* work-loop**

555 **recordings.** Length is from the sonomicrometry measures of the muscle belly. EMG-intensity

556 (*in-vivo*) or activation (*in-situ*) is pooled between the proximal and distal sites. Forces were

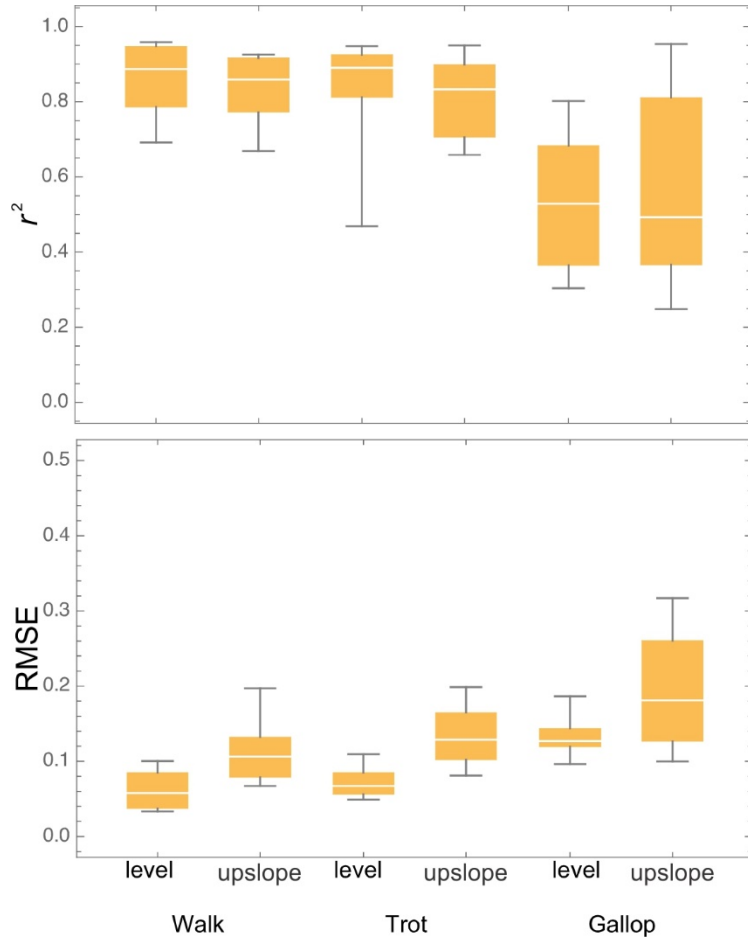
557 measured at the tendon (black) or predicted from the muscle models (red lines).



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559

560 **Fig. 3. Summary box plots ( $r^2$  and RMSE) comparing quality of modelled forces when**  
 561 **using rat-specific intrinsic properties in the models.** Box plots show median values with 25/75  
 562 quartiles, and whiskers delineating the 90% quartile ranges.



563

564 **Fig. 4. Box plots ( $r^2$  and RMSE) across *in-vivo* conditions averaged for the whole muscle**

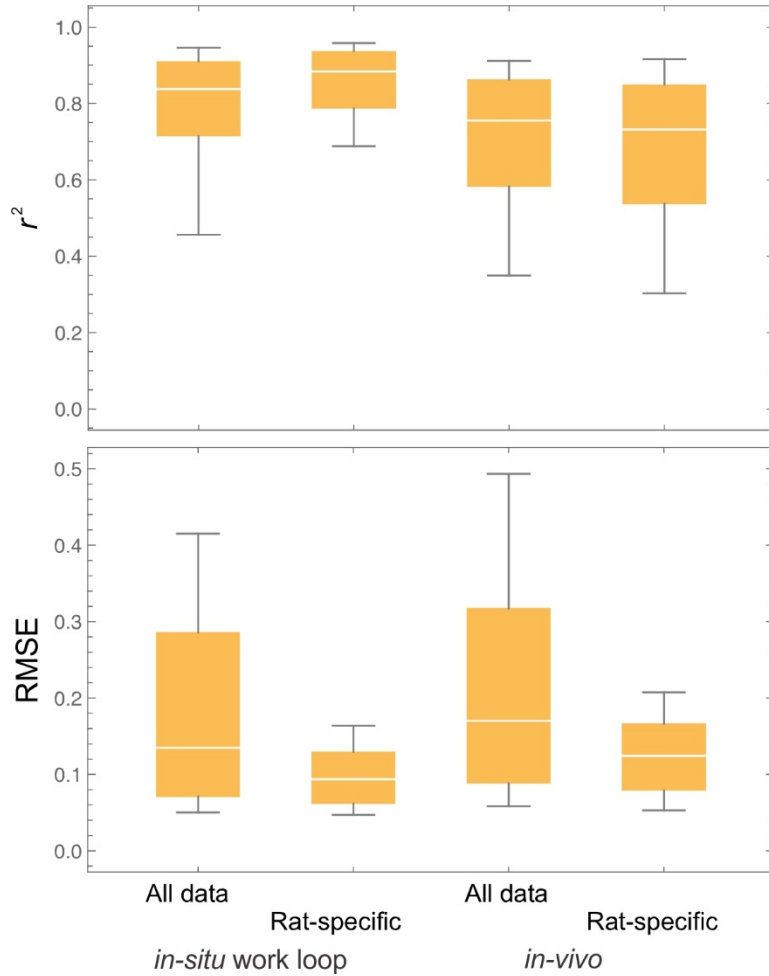
565 **belly.** Data are taken for the whole muscle belly. These models using rat-specific intrinsic

566 properties yielded forces with lower  $r^2$  and higher RMSE for gallop compared with trotting and

567 walking conditions (see Fig. S3 for statistical evaluation). RMSE was generally higher for

568 upslope gait versus level gait conditions. Box plots show median values with 25/75 quartiles, and

569 whiskers delineating the 90% quartile ranges.



570

571 **Fig. 5. Summary box plots ( $r^2$  and RMSE) across steady versus dynamic *in-situ* work-loop**

572 **and *in-vivo* conditions.** Note how the models using intrinsic properties pooled across the

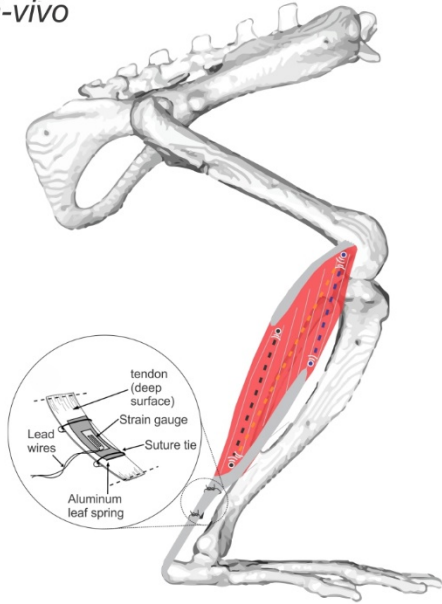
573 population of rats had model fits with higher RMSE than compared to models with rat-specific

574 properties. Box plots show median values with 25/75 quartiles, and whiskers delineating the 90%

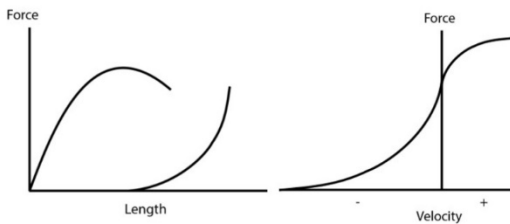
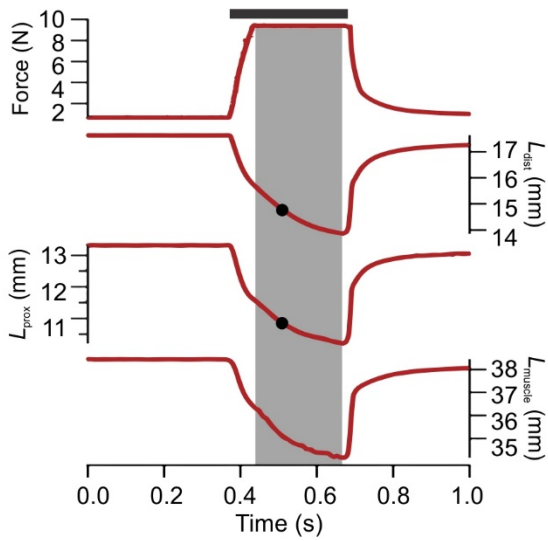
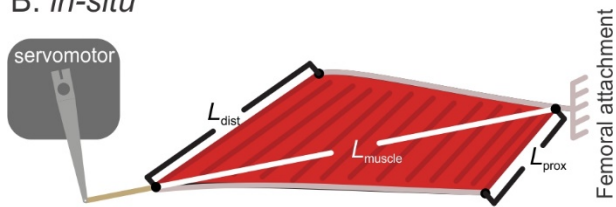
575 quartile ranges.



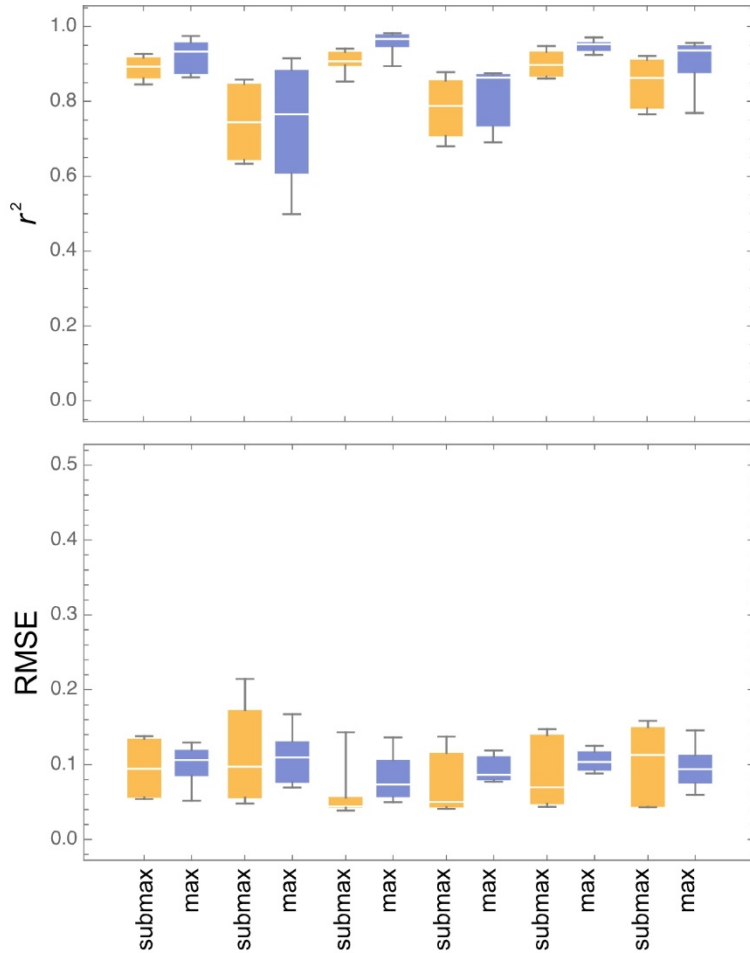
A. *in-vivo*



B. *in-situ*



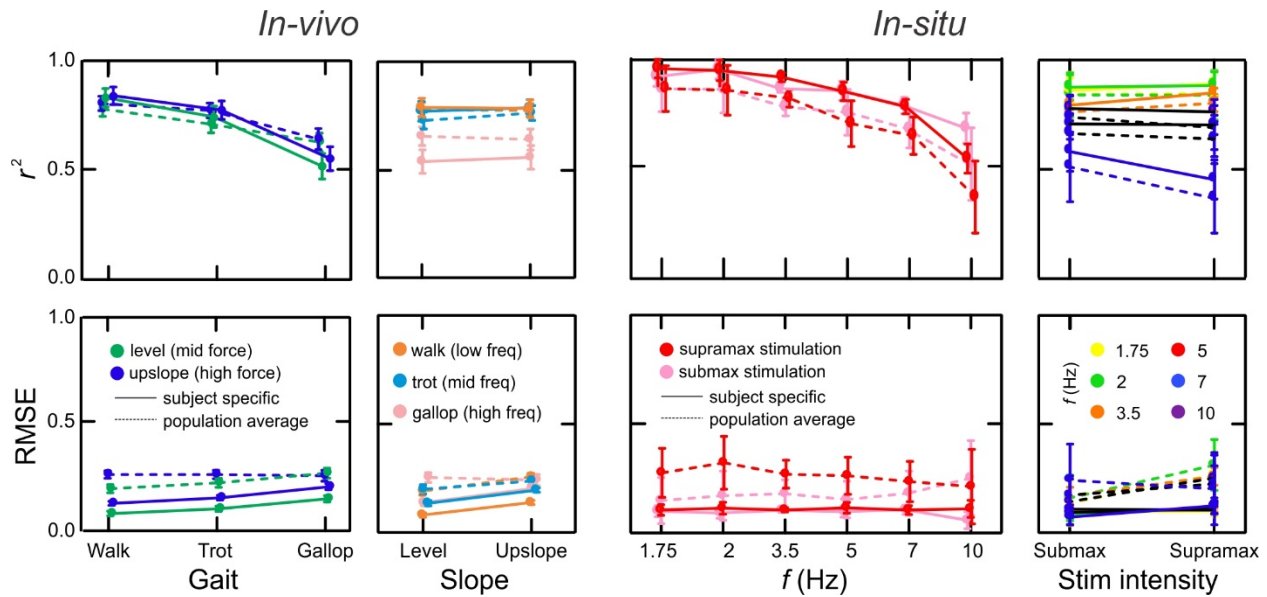
577 **Fig. S1. Schematic of (A) *in-vivo* and (B) *in-situ* force and length measurements.** (A) *In-vivo*  
578 MG forces were recorded using a leaf-spring force transducer surgically attached to the free MG  
579 tendon (Richards and Biewener, 2007; Eng et al. 2019). Proximal and distal fascicle length  
580 changes, as well as whole muscle belly length were recorded using 1.0 mm sonomicrometry  
581 crystals, along with fine-wire EMG electrodes implanted in both regions (not shown). (B) *In-situ*  
582 MG forces were measured by isolating the MG tendon and calcar attachment to a lever-based  
583 ergometer, with the proximal origin of the muscle remaining attached to the femur, which was  
584 fixed by a clamp. Stimulation of the muscle via the sciatic nerve elicited tetanic FL and FV  
585 contractions under supramaximal (2-3 v) and submaximal (~1 v) conditions, allowing active and  
586 passive FL and isotonic FV curves to be constructed.



Length (cm) 0.6 0.6 1.2 1.2 2.4 2.4  
 Frequency (Hz) 3.5 7.0 3.5 7.0 1.75 3.5

587  
 588

589 **Fig. S2. Box plots ( $r^2$  and RMSE) comparing quality of modelled forces when using rat-**  
 590 **specific intrinsic properties in the models across *in-situ* work-loop conditions ( $\Delta$ length &**  
 591 **frequency) for the whole muscle belly.** Predictive fits of rat-specific muscle models to forces  
 592 measured during *in-situ* work-loops were generally similar across the range of imposed lengths  
 593 and frequencies, with  $r^2$  averaging  $0.88 \pm 0.10$  and RMSE averaging  $0.09 \pm 0.04$ . No significant  
 594 difference in RMSE or  $r^2$  was observed for model fits to supramaximal versus submaximal  
 595 intensity work-loops (Fig. S3). Box plots show median values with 25/75 quartiles, and whiskers  
 596 delineating the 90% quartile ranges.



597  
 598 **Fig. S3. Least-Square Means plots** summarizing the statistical results related to testing  
 599 hypothesis 1; that model-predictions of muscle forces will be less accurate at the highest  
 600 contractile frequencies but not the greatest magnitude of force. For both *in-vivo* (Left) and *in-situ*  
 601 (Right), we used a nested factorial design to keep either the “force” or “frequency” parameter  
 602 constant, while testing across conditions for the alternate parameter. Force was dictated *in-vivo*  
 603 by the treadmill slope condition (Konow et al., 2020), and *in-situ* by sub- or supra-maximal  
 604 muscle stimulation. Frequency was dictated *in-vivo* by gait condition, and *in-situ* by varying  
 605 work-loop frequency. Within each condition, tests were run separately for the population average  
 606 and subject specific model inputs. Results are largely consistent across conditions, with  $r^2$  values  
 607 being significantly reduced by increasing cycle frequency but remaining largely invariant by  
 608 changes in force. RMSE values are generally better for modeling based on population average  
 609 data. For statistical test results, please see the results section.

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**Table 1. Active FL parameters.** See equation 1. Rat-specific parameters are shown as mean $\pm$ SD.

		$r$	$w$	$S$	$l_0$ [mm]	$F_0$ [N]	$r^2$	RMSE
Proximal	Pooled	2.37	0.217	0.475	8.57	8.52	0.857	0.128
	Rat	2.83 $\pm 0.75$	0.206 $\pm 0.256$	0.501 $\pm 0.691$	8.74 $\pm 2.45$	9.88 $\pm 6.26$	0.998 $\pm 0.002$	0.013 $\pm 0.007$
Distal	Pooled	2.29	0.135	0.417	9.48	8.54	0.732	0.209
	Rat	2.93 $\pm 0.78$	0.091 $\pm 0.159$	0.289 $\pm 0.592$	9.14 $\pm 3.03$	9.89 $\pm 6.27$	0.994 $\pm 0.012$	0.019 $\pm 0.012$
Belly	Pooled	2.17	0.096	0.567	22.0	8.56	0.846	0.125
	Rat	2.57 $\pm 0.50$	0.079 $\pm 0.204$	0.477 $\pm 1.236$	21.9 $\pm 3.1$	9.90 $\pm 6.26$	0.994 $\pm 0.006$	0.019 $\pm 0.012$

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**Table 2. Passive FL parameters.** See equation 2. Rat-specific parameters are shown as mean $\pm$ SD.

		$c_1$	$c_2$	$r^2$	RMSE
Proximal	Pooled	-13.0	7.74	0.021	0.329
	Rat	-14.3 $\pm$ 4.2	9.26 $\pm$ 4.11	0.997 $\pm$ 0.003	0.005 $\pm$ 0.006
Distal	Pooled	-12.3	7.44	0.040	0.308
	Rat	-14.1 $\pm$ 4.6	9.26 $\pm$ 4.51	0.998 $\pm$ 0.001	0.006 $\pm$ 0.009
Belly	Pooled	-21.3	16.7	0.079	0.185
	Rat	-23.8 $\pm$ 7.0	19.3 $\pm$ 6.72	0.995 $\pm$ 0.007	0.008 $\pm$ 0.012

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**Table 3. FV parameters.** See equation 3. Rat-specific parameters are shown as mean±SD.

		$k$	$v_0$ [s <sup>-1</sup> ]	$r^2$	RMSE
Proximal	Pooled	0.802	10.82	0.983	0.064
	Rat	1.24±1.20	10.82±3.01	0.998±0.002	0.027±0.013
Distal	Pooled	0.638	9.82	0.989	0.051
	Rat	0.775±0.473	9.82±3.22	0.997±0.002	0.028±0.011
Belly	Pooled	0.509	5.06	0.989	0.051
	Rat	0.599±0.391	5.06±0.98	0.997±0.002	0.026±0.014

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**Table S1. Measurements from the subjects used in this study.**

Rat	Body mass (g)	MG mass (g)	$l_{\text{muscle}}$ (mm)	Proximal $l_{\text{fascicle}}$ (mm)	Distal $l_{\text{fascicle}}$ (mm)	Proximal $\theta_{\text{fascicle}}$ (deg)	Distal $\theta_{\text{fascicle}}$ (deg)
1	207	0.446	19.1	6.7	8	27	19
2	247	0.673	27.6	6.8	8.3	20	15
3	289	0.719	29.1	7.8	8.9	21	17
4	362	0.976	33.2	8.8	10.3	22	17
5	380	1.035	31.8	8.4	10.3	25	21
6	360	0.911	30.1	7.9	9.6	21	20

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