## Defining an Informativeness Metric for Clustering Gene Expression Data

The Harvard community has made this article openly available. **Please share** how this access benefits you. Your story matters

<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Published Version</td>
<td>doi:10.1093/bioinformatics/btr074</td>
</tr>
<tr>
<td>Citable link</td>
<td><a href="http://nrs.harvard.edu/urn-3:HUL.InstRepos:8579873">http://nrs.harvard.edu/urn-3:HUL.InstRepos:8579873</a></td>
</tr>
<tr>
<td>Terms of Use</td>
<td>This article was downloaded from Harvard University’s DASH repository, and is made available under the terms and conditions applicable to Other Posted Material, as set forth at <a href="http://nrs.harvard.edu/urn-3:HUL.InstRepos:dash.current.terms-of-use#LAA">http://nrs.harvard.edu/urn-3:HUL.InstRepos:dash.current.terms-of-use#LAA</a></td>
</tr>
</tbody>
</table>
Defining an informativeness metric for clustering gene expression data

Jessica C. Mar¹,2,*, Christine A. Wells³ and John Quackenbush¹,2,4,∗

¹Department of Biostatistics, Harvard School of Public Health, ²Department of Biostatistics and Computational Biology, Dana-Farber Cancer Institute, Boston, MA 02115, USA, ³National Centre for Adult Stem Cell Research, Eskitis Institute for Cell and Molecular Therapies, Griffith University, Brisbane, Australia and ⁴Department of Cancer Biology, Dana-Farber Cancer Institute, Boston, MA 02115, USA

ABSTRACT

Motivation: Unsupervised ‘cluster’ analysis is an invaluable tool for exploratory microarray data analysis, as it organizes the data into groups of genes or samples in which the elements share common patterns. Once the data are clustered, finding the optimal number of informative subgroups within a dataset is a problem that, while important for understanding the underlying phenotypes, is one for which there is no robust, widely accepted solution.

Results: To address this problem we developed an ‘informativeness metric’ based on a simple analysis of variance statistic that identifies the number of clusters which best separate phenotypic groups. The performance of the informativeness metric has been tested on both experimental and simulated datasets, and we contrast these results with those obtained using alternative methods such as the gap statistic.

Availability: The method has been implemented in the Bioconductor R package attract; it is also freely available from http://compbio.dfci.harvard.edu/pubs/attract_1.0.1.zip.

Supplementary information: Supplementary data are available at Bioinformatics online.

Received on June 12, 2010; revised on January 3, 2011; accepted on February 6, 2011

1 INTRODUCTION

Clustering methods were among the first methods to be applied to DNA microarray data (Eisen et al., 1998; Michaels et al., 1998) and they remain one of the most commonly used techniques in the analysis of high-dimensional genomic data. The assumption is that samples sharing similar patterns of expression across large numbers of genes are members of a particular molecular class or that genes grouped in clusters are co-regulated across samples because they belong to a common functional group or pathway. While these assumptions have proven useful, determining where a cluster begins and ends, or equivalently, how many gene or sample clusters are present in a dataset is often arbitrary or treated as a post-clustering analysis problem. In either case, the lack of a robust and reliable method can lead to potentially incorrect conclusions. Underestimating the number of clusters can artificially group unrelated elements while overestimating can split related groups into subgroups that confound further analysis.

Here we focus on the problem of identifying informative gene expression clusters in experimental datasets resulting from comparison of multiple biological classes (such as treatment and control, or different cell types). The question we are trying to address is very specific: given a number of distinct phenotypic groups, what is the optimal cluster number (and membership) such that the clusters are maximally informative in their ability to distinguish the sample classes?

Given the history of using clustering approaches in gene expression analysis and for other applications, it is surprising that this problem has not been more effectively addressed. Statistical methods that evaluate the optimal number of clusters within a dataset exist but are rarely used in a systematic manner and may reflect the fact that there are an array of experimental applications in which clustering is used as a discovery tool.

Model-based cluster analysis methods assume that the collection of gene expression profiles can be decomposed into subgroups in which the genes display coordinated patterns of expression. Model-based approaches use statistical methods to search for the number of subgroups for which the consensus profiles best fit the available data (McLachlan et al., 2002). For model-based methods, metrics such as the Akaike Information Criterion (Akaikie, 1974) and the Bayesian Information Criterion (Schwarz, 1978) are both based on likelihood values and can be used to evaluate how well one model fits the data relative to another model. While these have been applied in other domains, in the analysis of microarray data, model selection can become difficult since there is often no a priori way of knowing what the structure of the underlying “true” model might be. These approaches also may require the estimation of a large number of parameters, and in some cases, the number of samples may not be sufficient to accurately complete this task. Finally, most model-based clustering algorithms assume a Gaussian distribution for variation that may not generally be appropriate for genomic profiling data.

For the analysis of microarray data, a number of methods have been developed for estimating optimal cluster number based on an assessment of two properties of ‘good’ gene clusters: compactness and stability. A compact cluster is defined such that the intra-cluster variability is small relative to the average inter-cluster variability. Metrics assessing compactness that have been applied to array data include the gap statistic (Tibshirani et al., 2001), the Silhouette width (Rousseeuw, 1987), the Dunn index (Dunn, 1974) and the...
connectivity score (Hand et al., 2005). A stable cluster on the other hand, is one that is robust to the removal of a small number of samples from the dataset. Stable cluster metrics include the average proportion of non-overlap (APN), the average distance (AD), and the figure of merit (FOM) (Yeung et al., 2001). These too fundamentally look at the relationship between intra- and inter-cluster variability. The aim of these metrics is to identify a set of clusters that individually display tightly grouped representative profiles, while finding clusters that are each distinct from the others. Despite the propagation of methods, none of these has become established as a de facto solution to the problem of estimating cluster number. However, this problem is not unique and predates arrays; in a comparative study of thirty statistical metrics on a variety of simulated datasets, which concluded that while some metrics performed adequately some of the time, the best metric to use may be arbitrarily data dependent (Milligan and Cooper, 1985).

In the analysis of most genomic datasets, the question is generally less abstract. What we often want to know is whether there are replicate samples for groups of interest. This is a question that spans the boundary between unsupervised clustering and statistical analysis on a gene-by-gene basis since we are searching for gene groups that share similar profiles, and which are distinguishable statistically significant model fit.

For each of the p clusters, we then fit an analysis of variance (ANOVA) model to the mean expression profile of that cluster which estimates the degree of dependency between the mean expression profile \( \mathbf{T}_c \), and a covariate that denotes group membership; in other words, we are able to quantify how much of the variability in \( \mathbf{T}_c \) can be explained by group membership alone. We call a cluster ‘informative’ if its mean expression distinguishes the different biological classes or groups as defined by a statistically significant model fit.

Formally, we fit a one-way fixed-effects ANOVA model to the mean expression profile \( \mathbf{T}_c \) (as defined in (2)) of each cluster \( c \) using a single factor that denotes each sample’s group effect through the model parameter \( \mu_k \) for \( k = 1, ..., m \) groups; a standard representation of the linear model underlying the ANOVA is represented by the following model equation:

\[
\mathbf{Y}_{ijk} = \mu + \mu_k + \epsilon_{ijk}
\]

where \( \mu \) represents the overall mean, \( \mu_k \) measures the effect of group \( k \) and \( \epsilon_{ijk} \) represents the random normal residual error term.

The null hypothesis, \( H_0: \mu_1 = \mu_2 = \ldots = \mu_m \), states all group means are equivalent while the alternative hypothesis, \( H_1 \) assumes that not all \( \mu_k \)’s are equal or, equivalently, that at least two groups have different mean expression values.

The mean expression for group \( k \) in cluster \( c \) is given by

\[
\mathbf{T}_{c,k} = \frac{1}{n_c} \sum_{j=1}^{n_c} \mathbf{T}_{c,j}
\]

which is simply the expression averaged over the genes in cluster \( c \), then averaged over the \( n_c \) replicates. Note this is reflected by the double dot notation which indicates the two indices over which the summations occur, one over the gene index \( j \) (from 1 to \( g \), as shown in (2)) and the second over the replicate index \( i \) (from 1 to \( n \) for the \( k \)-th group).

The overall mean value represents the average of all \( m \) group means in cluster \( c \),

\[
\mathbf{T}_{c} = \frac{1}{m} \sum_{k=1}^{m} \left( \frac{1}{n_k} \sum_{j=1}^{n_k} \mathbf{T}_{c,j} \right)
\]

where the triple dots indicate summations over the gene index \( i \) (from 1 to \( g \), for cluster \( c \)), the replicate index \( j \) (from 1 to \( n_k \) replicates for the \( k \)-th group) and the group index \( k \) (from 1 to \( m \) groups).

From the fitted model \( M0 \) for cluster \( c \), we obtain the MSS statistic (also known as the mean treatment sum of squares) which captures the amount of variation attributed to group-specific effects:

\[
\text{MSS}_c = \frac{1}{m-1} \sum_{k=1}^{m} (\mathbf{T}_{c,k} - \mathbf{T}_{c})^2
\]

and the RSS statistic (the residual sum of squares, also known as the mean error sum of squares) which represents the residual variation remaining after
different values. In this situation, the sum of squares calculation in the MSS
the data, this is manifested by observing group means that adopt distinctly
distinct the group means become, the sum of the deviations from the overall
statistic is not influenced by the presence of group structure in the data. The
statistic is large whereas the sum of squares calculation in the RSS

Fig. 1. Overall workflow of the informativeness metric-based approach.

Fig. 2. Schematic diagram of the assumptions underlying calculation of the
informativeness metric. Individual dots represent data points that represent
an expression profile; by definition, an informative profile will be one whose
points sit far away from the overall mean in each condition.

group-specific effects have been accounted for (Fig. 1),

\[
RSS = \frac{1}{p-1} \sum_{m=1}^{m} \sum_{k=1}^{k} (Y_{m,k} - \bar{Y}_{m,k})^2
\]  

(7)

An informative cluster c will yield a large MSS statistic relative to
the RSS statistic. This is because when genuine group structure exists in
the data, this is manifested by observing group means that adopt distinctly
different values. In this situation, the sum of squares calculation in the MSS
statistic is large whereas the sum of squares calculation in the RSS statistic
shrinks to zero (Fig. 2).

In calculating the RSS statistic, we are always comparing elements of
the mean expression profile back to their respective group means and so the
statistic is not influenced by the presence of group structure in the data.
The MSS statistic on the other hand compares the group means to the overall
mean directly (which ignores any group structure) and therefore the more
distinct the group means become, the sum of the deviations from the overall
mean will increase giving rise to a larger MSS statistic.

We define two final measures that collectively represent how informative
the overall cluster analysis is. These measures are obtained by averaging
the cluster-specific MSS and RSS, statistics for the p clusters found in the
dataset:

\[
\text{MSS}^{(p)} = \frac{1}{p} \sum_{c=1}^{p} \left[ \frac{1}{m-1} \sum_{k=1}^{k} (\bar{Y}_{m,k} - \bar{Y}_{m,k})^2 \right] = \frac{1}{p} \sum_{c=1}^{p} \text{MSS}
\]

(8)

Given that a single informative cluster c will be associated with a large
MSS, and a small RSS value then by extension, the overall MSS\(^{(p)}\) and
RSS\(^{(p)}\) values will be large and small respectively, for an informative set
of p clusters. The MSS\(^{(p)}\) statistic best captures the size of the group-
specific effect directly for each of the p clusters and therefore we define
the informativeness metric to be the MSS\(^{(p)}\) statistic defined in (8).

In standard ANOVA analysis, it is more common to focus on the ratio of
the MSS and RSS statistics or equivalently, the F statistic:

\[
F = \frac{\text{MSS}}{\text{RSS}}
\]

to assess the significance of a fitted model.

For the p clusters generated by the cluster analysis, we can extend the Fc
cluster-based statistic and similarly define Fc\(^{(p)}\) in the following way:

\[
F^{(p)} = \frac{1}{p} \sum_{c=1}^{p} \left[ \frac{1}{m-1} \sum_{k=1}^{k} (\bar{Y}_{m,k} - \bar{Y}_{m,k})^2 \right] = \frac{1}{p} \sum_{c=1}^{p} \text{MSS}
\]

\[
= \frac{1}{p} \sum_{c=1}^{p} \text{RSS}
\]

(9)

Our results presented for the modified F statistic are calculated from the Fc\(^{(p)}\)
definition. Note that there is an alternative way to define Fc\(^{(p)}\):

\[
F^{(p)} = \frac{1}{p} \sum_{c=1}^{p} \left[ \frac{1}{m-1} \sum_{k=1}^{k} (\bar{Y}_{m,k} - \bar{Y}_{m,k})^2 \right] = \frac{1}{p} \sum_{c=1}^{p} \text{MSS}
\]

\[
= \frac{1}{p} \sum_{c=1}^{p} \text{RSS}
\]

(10)

In theory, the F-based statistic appears to be potentially useful as a
means to measure informativeness since a large MSS, and small RSS,
will give rise to a large F value. However, based on tests using simulated
datasets, the F-based statistic as defined in (10) was inconsistently incorrect
in estimating the correct number of clusters (see Supplementary Material).

For the experimental dataset, the F-based statistic estimated a set of clusters
which were sub-optimal describing the diversity of expression profiles for
the biological classes in this dataset. This can be demonstrated by comparing
the profiles in panel A versus B in Figure 3 where the emergence of Cluster 1 in
panel B reveals a cluster that would otherwise have been masked when fewer
numbers of clusters are specified, as shown in panel A (and Supplementary
Informativeness metric

Fig. 3. Average expression profiles for the MAPK pathway with different numbers of cluster applied. These clusters were generated from complete linkage agglomerative hierarchical clustering, using Pearson’s correlation metric. (A) Two clusters. (B) Average cluster expression profiles for the MAPK pathway with the number of clusters prescribed by the informativeness metric. Note the appearance of the first cluster which has an expression profile distinct from those identified using other methods.

Material). Therefore, our tests of the $F$-based statistics on both simulated and experimental datasets indicate that these statistics do not perform reliably as measures of cluster information content.

By clustering the expression dataset, the goal is to reveal underlying substructures that reflect the gene sets driving the group-specific differences observed. Changing the number of clusters will effectively alter the resolution at which those substructures can be observed, and the optimal number of clusters will give rise to a set of clusters that highlight these group-specific differences at maximum resolution. Therefore, as the number of clusters ($p$) approaches this optimal value, the clusters become more informative, as reflected by an increase in the MSS($p$) statistic and a much smaller RSS($p$) statistic. The $F$($p$)-based statistic failed to provide reliable discriminatory power and a careful analysis of all three collective measures on both simulated and real data indicate that MSS($p$) has the greatest discriminatory power and consequently, we chose MSS($p$) as a measure of cluster information content—the informativeness metric, coupled with the simple expectation that an informative set of clusters will be associated with a much smaller RSS($p$) statistic.

To determine the optimal number of clusters using the informativeness metric, we vary the number of clusters in a cluster analysis over a finite range and calculate the informativeness metric for each value within this space (Fig. 1). The value which maximizes the informativeness metric is taken to be the optimal number of clusters with the accompanying condition that the $F$($p$)-statistic computed for the $p$ clusters should be much smaller than the informativeness metric. Instances where the informativeness metric and the RSS($p$) statistic produce similar values over the interval in which the number of clusters is altered suggest there is an absence of group structure (see Supplementary Material). The range over which the number of clusters ($p$) is tested can be chosen arbitrarily. In practice, the approach we have adopted is to set the lower limit of this range to one and the upper limit is determined by the maximum value of $p$ that gives rise to clusters that have a minimum number of genes (for example, a minimum of five genes).

3 RESULTS

3.1 Evaluation of the informativeness metric

To evaluate the performance of the informativeness metric relative to other eight other widely used measures (Datta and Datta, 2003; Dunn, 1974; Rousseeuw, 1987; Tibshirani et al., 2001; Yeung et al., 2001), we chose to use both simulated and an experimental dataset. The advantage of a simulated dataset is that it allows us to assess performance where the number of clusters are known and can be used as an objective measure of performance while an experimental dataset provides the opportunity to evaluate whether the results lead to biologically relevant conclusions.

As noted previously, the clustering algorithm adopted throughout our analyses was agglomerative hierarchical clustering where clusters were joined based on complete linkage and the distance metric used was based on $(1 - R)$ where $R$ is the Pearson correlation coefficient. Complete linkage was used instead of the more commonly used average linkage because the former produced a much more stable clustering. Complete linkage has been shown to perform better than average linkage for non-ratio based expression values (Gibbons and Roth, 2002). Since the informativeness metric simply measures the optimal number of clusters given a particular clustering algorithm, we chose not to explore the effect of the clustering method and instead focused only on the ability of cluster metrics to identify the optimal number of clusters within a given clustering result.

3.2 Comparison of performance on simulated dataset

We evaluated cluster-number metric performance of three simulated datasets which had four, six and eight clusters, respectively.
Table 1. Optimal number of clusters inferred for the simulated datasets

<table>
<thead>
<tr>
<th>Number of simulated clusters</th>
<th>Compactness Metrics</th>
<th>Stability Metrics</th>
<th>$F$-statistic</th>
<th>Informativeness metric</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Gap statistic</td>
<td>Connectivity</td>
<td>Dunn index</td>
<td>Silhouette width</td>
</tr>
<tr>
<td>4</td>
<td>5</td>
<td>2</td>
<td>3</td>
<td>3</td>
</tr>
<tr>
<td>6</td>
<td>6</td>
<td>2</td>
<td>5</td>
<td>4</td>
</tr>
<tr>
<td>8</td>
<td>8</td>
<td>2</td>
<td>7</td>
<td>6</td>
</tr>
</tbody>
</table>

To construct these, we simulated a small gene expression dataset under a Normal distribution for 300 genes and 100 samples. For each dataset, the samples were grouped into four sets of 28 representing distinct phenotypic classes on which we had repeated measures. Supplementary Figures 1, 2 and 3 shows the distinct expression profiles for data representing six, four and eight clusters, respectively. For each cluster we assume that expression is normally distributed with a standard deviation held constant at 1.5.

Of the nine metrics analyzed, only the informativeness metric was successful in correctly estimating the number of clusters for all three simulated datasets (Table 1). For both the six-cluster and the eight-cluster datasets, the gap statistic and the informativeness metric identified the correct number of clusters. For these two datasets, all of the other compactness-based methods underestimated the optimal number of clusters (Table 1). None of the stability-based methods (APN, AD, ADM and FOM) were able to correctly pick the number of clusters (half of the methods underestimated this number, the other half overestimated). Given that the gap statistic is the most widely used method for determining the optimal number of clusters in applied statistics, it is interesting that it overestimated the optimal number of clusters for the four-cluster simulated dataset.

All metrics require the user to specify a finite range over which the number of clusters is optimized. For the eight existing metrics presented in our article, the lower limit of this range permitted was two, and the upper limit was determined by choosing the maximum number of clusters that produced clusters with at least five genes. The lower limit allowed by our informativeness metric was one, and we applied the same criterion to determine the upper limit.

We also extended our simulation study to evaluate the performance of the informativeness metric against the other nine metrics in the context of (i) a larger number of genes than samples (2000 genes, 100 samples); (ii) 100 simulated datasets where the number of clusters is known to be four, six and eight clusters; (iii) clusters produced by both hierarchical clustering and $k$-means clustering; (iv) no clustering structure; (v) a simulated dataset with unequal sample sizes for each phenotypic group (300 genes, 110 samples with 20, 20, 30, 40 replicates per group); (vi) a simulated dataset with a larger number of genes and small number of samples (1800 genes, 40 samples); (vii) unequal variance between clusters where each cluster in the dataset is simulated under a different variance parameter; and (viii) unequal variance within clusters where different genes within each cluster were simulated under different variance parameters (see Supplementary Material). In almost all of these simulations, the informativeness metric accurately estimated the correct number of clusters simulated, with the only other metric, the gap statistic demonstrating similar consistent performance, while the remaining metrics performed on average, quite poorly. In instances where the informativeness metric failed to estimate the correct number of clusters exactly, it usually gave the estimate closest to the true parameter, compared to the other metrics.

3.3 Comparison of performance on experimental datasets

We then extended our evaluation to an experimental dataset which studied cell type-specific gene expression differences in distinct human stem cell populations (Müller et al., 2008) (NCBI GEO accession number GSE11508). This dataset surveyed 20 different cell lines, but to simplify our analyses we limited ourselves to evaluating the ability of clustering metrics to predict the optimal number of gene expression clusters between four cell types: embryonic stem cells, neural progenitor cells, neural stem cells and a teratoma-differentiated cell line. We further restricted the samples to those that had been used on the same Illumina BeadChip platform (WG-6), giving a total of $n = 68$ samples, where the number of samples for each group was $n_1 = 12$, $n_2 = 31$, $n_3 = 8$, $n_4 = 17$, respectively. We applied a quality filter which retained a probe only if it passed a 0.99 detection score in 75% of samples for at least one of the four cell types. These filtering processes resulted in a total of 11 044 probes.

While it is possible to apply a cluster analysis to all genes in this dataset, we instead preferred to interpret gene clusters within the context of literature-supported biological pathways. Therefore, we used gene sets defined by biological pathways from the Kyoto Encyclopedia of Genes and Genomes (KEGG) (Kanehisa and Goto, 2000) and for the purposes of this article, chose to demonstrate the performance of the informativeness metric on three pathways which were selected to reflect relevant aspects of the biology associated with the four cell types we have selected from the Müller dataset. We then applied a cluster analysis method separately to each of the top three most significant and largest KEGG pathways: the mitogen-activated protein kinase (MAPK) signaling pathway ($g = 154$ genes), the focal adhesion pathway ($g = 136$ genes) and the regulation of actin cytoskeleton pathway ($g = 138$ genes). In this way, for each KEGG pathway, we obtain a final set of clusters using the informativeness metric that describe the distinct repertoire of expression patterns between cell types supported by the genes that participate in that pathway. Note that we also tested these metrics on clusters derived from a more conventional analysis that began by filtering out genes from the entire dataset and clustering about 2000 genes (Supplementary Material).

Unlike the simulated dataset, here we have no prior knowledge of what the ‘real’ number of clusters is. If, however, we compare...
the gene expression profiles across phenotypic groups as a function of the number of clusters, we can gauge how informative the results are and whether the optimal number of clusters has been identified. The majority of methods estimated the optimal number of clusters to be two (Table 2) for all three pathways, except the Dunn index, which estimated the optimal number to be two (MAPK), four (focal adhesion) and 10 (actin cytoskeleton).

In contrast, the informativeness metric identified three, four and five optimal clusters for the MAPK pathway, focal adhesion pathway and regulation of actin cytoskeleton pathway, respectively. The risk with underestimating the optimal number of clusters is that important features of the data might be hidden. Figure 3A shows the two clusters, produced by the hierarchical clustering of the MAPK pathway, that were identified by all four compactness-based metrics tested. The predominant patterns observed were genes that are up-regulated and down-regulated in the neural progenitor samples relative to the other cell types. When we examine the three clusters predicted by the informativeness metric, we see that in addition to the patterns observed in the original two cluster, a third cluster (cluster 1, Fig. 3B) appears that uniquely highlights similarities in the expression patterns between the embryonic stem cells and neural stem cells versus increased expression in the neural progenitor cells and the teratoma-differentiated cells. While the original two clusters highlight the uniqueness of the neural stem cell niche, the additional cluster revealed by the informativeness metric identifies an important biological pattern—a shared phenotype of embryonic stem cells and neural progenitors—that would otherwise have been masked.

For the focal adhesion pathway, we find similar results (Supplementary Material). When the genes are split into two clusters, the dominant themes represented are genes up-regulated or down-regulated in the neural progenitor cells relative to the other cell types. However, the four gene clusters identified using the informativeness metric also identifies patterns of teratoma-differentiated specific expression changes (Supplementary Material, Supplementary Fig. S4B, cluster 3) and embryonic stem cell-specific expression changes (Supplementary Material, Supplementary Fig. S4B, cluster 4). Note that the Dunn index was also able to identify the same four clusters as the informativeness metric.

For the regulation of actin cytoskeleton pathway (Supplementary Material, Supplementary Fig. S5), the two primary clusters found using the informativeness metric and Dunn index, we see two separate embryonic stem cells and progenitor cells from the neural stem cells and teratoma-differentiated cells, with genes either up-regulated (Supplementary Fig. S5B, cluster 2) or down-regulated (Supplementary Material, Supplementary Fig. S5B, cluster 5) in the ESC/progenitor cell group. We also see a cluster with a less easily interpreted expression pattern (Supplementary Material, Supplementary Fig. S5B, cluster 4). Although this cluster does not have a clear interpretation in terms of its differential expression pattern, it may nonetheless capture some of the underlying biology of the actin cytoskeletal system, which is important to the structural integrity of the cell types profiled by Müller et al. (2008), all of which have similar cell shapes. Regardless, the identification of two additional and clearly relevant clusters through the use of the informativeness metric underscores its overall utility. While we found additional biologically relevant structure by adding new clusters, there is clearly an upper limit. For the actin pathway, the Dunn index suggested 10 clusters (compared to 5 as suggested by the informativeness metric). However, having 10 clusters does not provide a set of clusters that are overall informative (Supplementary Material, Supplementary Fig. S6), where, for example, clusters 6, 9, 10 are essentially the same profile, containing genes that are invariant across the phenotypic group. Unlike the situation in using simulated data, it is difficult to objectively determine whether the number of gene clusters identified by any method captures the underlying biology being explored in the experiment. The informativeness metric generally identified a larger number of clusters than other approaches and in each occasion these provided additional, relevant discriminating patterns between the cell types. In the one instance in which additional clusters were identified by another method, the Dunn index, these provided no additional insight into patterns discriminating between cell types. The evidence here suggests that our informativeness metric strikes the right balance, and succeeds in teasing out more informative clusters from the expression data.

### 4 DISCUSSION

The motivation underlying all clustering methods is to determine whether the data can be partitioned into useful groups that provide insight into the relationship between group members, or the discriminating elements between groups. While identifying clusters that reflect finer substructures may be desirable, there are also instances where a dataset may have no such underlying structure.
The routines implementing this metric and associated tools for visualization are freely available as an R package attract and has been submitted to Bioconductor. We have also uploaded a script which details the calculations performed as well the data analyzed in this article, available from http://compbio.dfci.harvard.edu/pubs/informativeness.zip. The Bioconductor R package cValid (Datta and Datta, 2000) contains functions that calculate the six other metrics: the connectivity score, the Dunn Index, the silhouette width, APN, AD, ADM and FOM. To our knowledge, the Bioconductor package SAGs contains the only implementation of the Gap statistic in R.

**ACKNOWLEDGEMENTS**

We acknowledge the assistance of Drs Jiyuan An, Alistair Chalk and Nick Matigian, The National Centre for Adult Stem Cell Research, Griffith University, who provided valuable help in assembling the experimental dataset for this article. We also thank the constructive suggestions from our anonymous peer reviewers, in particular on extensions to our simulation work.

**Funding**: Australian Research Council International linkage project (LX0882502 to C.A.W.). C.A.W. is supported by a CDA fellowship (481945) from the National Health and Medical Research Council, Australia. J.Q. and J.C.M. were supported by a grant from the US National Institute for Human Genome Research (P50 HG004235); J.Q. was also supported by a grant from the US National Library of Medicine (R01 LM010129).

**Conflict of Interest**: none declared.

**REFERENCES**


