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Citation

Petrov, A. N., L. V. Skripnikov, A. V. Titov, N. R. Hutzler, P. W. Hess, B. R. O'Leary, B. Spaun, D. DeMille, G. Gabrielse, and J. M. Doyle. 2014. Zeeman Interaction in ThO H3[delta]1 for the Electron Electric-Dipole-Moment Search. Physical Review A 89 (6). doi:10.1103/physreva.89.062505.

Published version

<https://doi.org/10.1103/PhysRevA.89.062505>

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Zeeman interaction in ThO $H^3\Delta_1$ for the electron electric-dipole-moment search

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(Received 15 April 2014; published 11 June 2014)

The current limit on the electron’s electric dipole moment, $|d_e| < 8.7 \times 10^{-29} e \text{ cm}$ (90% confidence), was set using the molecule thorium monoxide (ThO) in the $J = 1$ rotational level of its $H^3\Delta_1$ electronic state [J. Baron *et al.*, *Science* **343**, 269 (2014)]. This state in ThO is very robust against systematic errors related to magnetic fields or geometric phases, due in part to its Ω -doublet structure. These systematics can be further suppressed by operating the experiment under conditions where the g -factor difference between the Ω doublets is minimized. We consider the g factors of the ThO $H^3\Delta_1$ state both experimentally and theoretically, including dependence on Ω doublets, the rotational level, and the external electric field. The calculated and measured values are in good agreement. We find that the g -factor difference between Ω doublets is smaller in $J = 2$ than in $J = 1$ and reaches zero at an experimentally accessible electric field. This means that the $H, J = 2$ state should be even more robust against a number of systematic errors compared to $H, J = 1$.

DOI: 10.1103/PhysRevA.89.062505

PACS number(s): 31.15.vn, 31.30.jp, 32.10.Dk, 33.15.Kr

I. EDM MEASUREMENTS WITH Ω DOUBLETS

The experimental measurement of a nonzero electron electric dipole moment (e EDM, d_e) would be a clear signature of physics beyond the standard model [1–3]. The most sensitive probes of the e EDM are precision spin-precession measurements in atoms [4] and molecules [5,6], which search for energy level shifts resulting from the interaction between the e EDM of a valence electron (or unpaired electrons) and the large effective internal electric field $\mathcal{E}_{\text{eff}}$ near a heavy nucleus [1,7]. The current limit, $|d_e| < 8.7 \times 10^{-29} e \text{ cm}$ (90% confidence), was set with a buffer-gas-cooled molecular beam [5,8,9] of thorium monoxide (ThO) molecules in the metastable electronic $H^3\Delta_1$ state.

Polar molecules have a number of advantages over atoms for e EDM searches [10,11], including a larger $\mathcal{E}_{\text{eff}}$ and resistance to a number of important systematics. Some molecules, for example, ThO [5,12], lead oxide (PbO) [13,14], HfF⁺ [15,16], and WC [17,18], have additional advantages due to the existence of closely spaced levels of opposite parity, called an Ω doublet. Molecules with Ω doublets can typically be polarized in modest laboratory electric fields ($\lesssim 1\text{--}100 \text{ V/cm}$), and in addition the spin-precession measurement can be carried out in a state where the molecular dipole is either aligned or antialigned with the external laboratory field. Since $\vec{\mathcal{E}}_{\text{eff}} = \mathcal{E}_{\text{eff}} \hat{n}$ points along the internuclear axis, $\hat{n}$, these states have equal yet opposite projections of $\vec{\mathcal{E}}_{\text{eff}}$ in the laboratory frame and therefore opposite energy shifts due to d_e . This means that the experimental signature of d_e can be detected either by performing the measurement in the other Ω -doublet state or by reversing the external electric field $\vec{\mathcal{E}}$. On the other hand, the internal field of an atom or molecule without Ω doublets can be reversed only by reversing $\vec{\mathcal{E}}$, which makes the measurement susceptible to systematic errors associated

with changing leakage currents, field gradients, and motional fields [1,4]. Molecules with Ω doublets are very robust against these effects, since the Ω -doublet structure acts as an “internal comagnetometer” [19]; the spin-precession frequencies in the two Ω -doublet states can be subtracted from each other, which heavily suppresses many effects related to magnetic fields [19] or geometric phases [20] but doubles the e EDM signature. The advantages of Ω doublets for suppression of systematic effects were first proposed [19] and realized [14,21] in the PbO e EDM search.

However, the upper and lower Ω -doublet states have slightly different magnetic g factors, and this difference depends on the laboratory electric field [21]. Systematic effects related to magnetic field imperfections and geometric phases can still manifest themselves as a false EDM, though they are suppressed by a factor of $\sim \Delta g/g$, where Δg is the g -factor difference between the two doublet states [5,14,22,23]. These systematics can be further suppressed by operating the experiment at an electric field where the g -factor difference is minimized [18,24] or where the g factors themselves are nearly canceled [25]; however, it is clear that understanding the g -factor dependence on electric fields is important for understanding possible systematic effects in polar-molecule-based e EDM searches. Additionally, measurement of Δg is a good test of an EDM measurement procedure [5,16].

In this paper we consider the g factors of the ThO $H^3\Delta_1$ state, both theoretically and experimentally, including dependence on Ω doublets, the rotational level, and the external electric field.

II. THEORY

Following the computational scheme of Ref. [24], the g factors of the rotational levels in the $H^3\Delta_1$ electronic state of the $^{232}\text{Th}^{16}\text{O}$ molecule are obtained by numerical diagonalization of the molecular Hamiltonian ($\hat{\mathbf{H}}_{\text{mol}}$) in external electric $\vec{\mathcal{E}} = \mathcal{E} \hat{z}$ and magnetic $\vec{\mathcal{B}} = \mathcal{B} \hat{z}$ fields over

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the basis set of the electronic-rotational wave functions $\Psi_{\Omega} \theta_{M,\Omega}^J(\alpha, \beta)$. Here Ψ_{Ω} is the electronic wave function; $\theta_{M,\Omega}^J(\alpha, \beta) = \sqrt{(2J+1)/4\pi} D_{M,\Omega}^J(\alpha, \beta, \gamma = 0)$ is the rotational wave function; α , β , and γ are Euler angles; and M (Ω) is the projection of the molecule angular momentum on the laboratory $\hat{z}$ (internuclear $\hat{n}$) axis. We define the g factors such that the Zeeman shift is equal to

$$E_{\text{Zeeman}} = -g\mu_B \mathcal{B}M. \quad (1)$$

In other words, we use the convention that a positive g factor means that the projection of the angular momentum and the projection of the magnetic moment are aligned. Note that this definition of the g factor for the $J = 1$ $H^3\Delta_1$ state differs by a factor of -2 from that given in Ref. [26].

In our model the molecular Hamiltonian is written as

$$\hat{\mathbf{H}}_{\text{mol}} = \hat{\mathbf{H}}_{\text{el}} + B_{\text{rot}} \vec{J}^2 - 2B_{\text{rot}}(\vec{J} \cdot \vec{J}^e) + \mu_B(\vec{L}^e - g_S \vec{S}^e) \cdot \vec{B} - \vec{D} \cdot \vec{E}, \quad (2)$$

where $\vec{J}$, $\vec{L}^e$, $\vec{S}^e$, and $\vec{J}^e = \vec{L}^e + \vec{S}^e$ are the electronic-rotational, electronic orbital, electronic spin, and total electronic momentum operators, respectively. $\hat{\mathbf{H}}_{\text{el}}$ is the electronic Hamiltonian, $B_{\text{rot}} = 9.76$ GHz [27] is the rotational constant, μ_B is the Bohr magneton, and $g_S = -2.0023$ is a free-electron g factor.

Our basis set includes four electronic states. The electronic structure calculations described below show that these states contain the following leading configurations in the $\Lambda\Sigma$ -coupling scheme:

$$\begin{aligned} H^3\Delta_1 &: |\sigma\downarrow\delta_2\downarrow|, \quad (T_e = 5317 \text{ cm}^{-1}), \\ Q^3\Delta_2 &: \frac{1}{\sqrt{2}}(|\sigma\uparrow\delta_2\downarrow| + |\sigma\downarrow\delta_2\uparrow|), \quad (T_e = 6128 \text{ cm}^{-1}), \\ A^3\Pi_{0+} &: \frac{1}{\sqrt{2}}(|\sigma\downarrow\pi_1\downarrow| + |\sigma\uparrow\pi_{-1}\uparrow|), \quad (T_e = 10601 \text{ cm}^{-1}), \\ {}^3\Pi_{0-} &: \frac{1}{\sqrt{2}}(|\sigma\downarrow\pi_1\downarrow| - |\sigma\uparrow\pi_{-1}\uparrow|), \quad (T_e = 10233 \text{ cm}^{-1}). \end{aligned} \quad (3)$$

Here $T_e = \langle \Psi_{\Omega} | \hat{\mathbf{H}}_{\text{el}} | \Psi_{\Omega} \rangle$ are energies of the electronic terms, σ , π , and δ are molecular orbitals; σ predominantly consists of the Th $7s$ atomic orbital and δ and π consist predominantly of the Th $6d$ orbital. The up (down) arrow means electronic spin aligned (antialigned) with the internuclear axis. T_e is known experimentally for the $H^3\Delta_1$, $Q^3\Delta_2$, and $A^3\Pi_{0+}$ states [28], but is presently unknown for the ${}^3\Pi_{0-}$ state. In our calculation we put $T_e({}^3\Pi_{0-}) = 10233 \text{ cm}^{-1}$ to reproduce the Ω doubling [27], $a = h \times 186(18) \text{ kHz}$, for $H^3\Delta_1$; this value is within the error bar of our present calculation (described below) of the $A^3\Pi_{0+} \rightarrow {}^3\Pi_{0-}$ transition energy, $T_e(A^3\Pi_{0+}) - T_e({}^3\Pi_{0-}) = 569 \text{ cm}^{-1}$. Provided that the *electronic* matrix elements are known, the matrix elements of $\hat{\mathbf{H}}_{\text{mol}}$ between states in the basis set (3) can be calculated with the help of angular momentum algebra [29]. The required *electronic* matrix elements are

$$G_{\parallel} = \frac{1}{\Omega} \langle H^3\Delta_1 | \hat{L}_{\hat{n}}^e - g_S \hat{S}_{\hat{n}}^e | H^3\Delta_1 \rangle = 0.0083, \quad (4)$$

$$G_{\perp}^{(1)} = \langle Q^3\Delta_2 | \hat{L}_{+}^e - g_S \hat{S}_{+}^e | H^3\Delta_1 \rangle = 2.706, \quad (5)$$

$$G_{\perp}^{(2)} = \langle H^3\Delta_1 | \hat{L}_{+}^e - g_S \hat{S}_{+}^e | {}^3\Pi_{0\pm} \rangle = 1.414, \quad (6)$$

$$\Delta^{(1)} = 2B_{\text{rot}} \langle Q^3\Delta_2 | J_{+}^e | H^3\Delta_1 \rangle = 0.882 \text{ cm}^{-1}, \quad (7)$$

$$\Delta^{(2)} = 2B_{\text{rot}} \langle H^3\Delta_1 | J_{+}^e | {}^3\Pi_{0\pm} \rangle = 0.923 \text{ cm}^{-1}, \quad (8)$$

$$D_{\parallel} = \langle H^3\Delta_1 | \hat{D}_{\hat{n}} | H^3\Delta_1 \rangle = 1.67 \text{ a.u.}, \quad (9)$$

$$D_{\perp}^{(1)} = \langle Q^3\Delta_2 | \hat{D}_{+} | H^3\Delta_1 \rangle = -0.068 \text{ a.u.}, \quad (10)$$

$$D_{\perp}^{(2)} = \langle H^3\Delta_1 | \hat{D}_{+} | {}^3\Pi_{0\pm} \rangle = 0.693 \text{ a.u.} \quad (11)$$

The molecule-fixed magnetic dipole moment parameter $G_{\parallel}$ is chosen in such a way that the mean g factor of the upper and lower states, $\bar{g}(J) = [g_e(J) + g_f(J)]/2$, for $J = 1$ exactly corresponds to the experimental datum [30]. The molecule-fixed dipole moment, $D_{\parallel}$, is taken from experiment [31]. The positive value for $D_{\parallel}$ means that the unit vector $\hat{n}$ along the molecular axis is directed from O to Th. Note that $\hat{n}$ is defined backwards with respect to the convention used in Ref. [26]. $G_{\perp}^{(2)}$ and $\Delta^{(2)}$ are estimated on the basis of the configurations listed in Eq. (3) using only angular momentum algebra. The DIRAC12 [32] and MRCC [33] codes are employed to calculate the matrix elements (5, 7, 10, 11) and the energy of transition between the $A^3\Pi_{0+}$ and ${}^3\Pi_{0-}$ states. The innercore $1s-4f$ electrons of Th are excluded from molecular correlation calculations using the valence (semilocal) version of the generalized relativistic effective core potential method [34]. Thus, the outermost 38 electrons of ThO are treated explicitly. For Th we have used the atomic basis set from Ref. [26] (30,20,17,11,4,1)/[30,8,6,4,4,1] in calculations of matrix elements, Eqs. (5), (7), and (10), and the energy of transition between the $A^3\Pi_{0+}$ and ${}^3\Pi_{0-}$ states. To calculate the matrix element in Eq. (11) the basis set is reduced to (23,20,17,11,3)/[7,6,5,2,1] and 20 electrons are frozen due to convergence problems. For oxygen the aug-ccpVQZ basis set [35] with two removed g -type basis functions is employed; i.e., we have used the (13,7,4,3)/[6,5,4,3] basis set. The relativistic two-component linear response coupled-clusters method with single- and double-cluster amplitudes is used to account for electron correlation and transition properties. To compute the matrix elements of operators $\hat{L}_{+}^e$ and $\hat{S}_{+}^e$ in the Gaussian basis set, we have used the code developed in Refs. [26,36,37].

In the framework of second-order perturbation theory for the g factors of the f and e states of $H^3\Delta_1$, g_f and g_e , respectively, as functions of J in the absence of electric field we have [18,24]

$$\begin{aligned} g_e(J) = & -\frac{G_{\parallel}}{J(J+1)} + \frac{G_{\perp}^{(2)}\Delta^{(2)}}{T_e(H^3\Delta_1) - T_e(A^3\Pi_{0+})} \\ & + \frac{G_{\perp}^{(1)}\Delta^{(1)}}{T_e(H^3\Delta_1) - T_e(Q^3\Delta_2)} \frac{(J+2)(J-1)}{2J(J+1)}, \end{aligned} \quad (12)$$

$$\begin{aligned} g_f(J) = & -\frac{G_{\parallel}}{J(J+1)} + \frac{G_{\perp}^{(2)}\Delta^{(2)}}{T_e(H^3\Delta_1) - T_e({}^3\Pi_{0-})} \\ & + \frac{G_{\perp}^{(1)}\Delta^{(1)}}{T_e(H^3\Delta_1) - T_e(Q^3\Delta_2)} \frac{(J+2)(J-1)}{2J(J+1)}. \end{aligned} \quad (13)$$

Because of the small value of $G_{\parallel}$ in the $H^3\Delta_1$ state, contributions from off-diagonal interactions with the other electronic states included in the basis set (3) significantly influence the g

factors of $H^3\Delta_1$. Formally, the interactions with other $\Omega = 0^\pm$ and $\Omega = 2$ states, not included in this basis, also influence the g factors of $H^3\Delta_1$. Note, however, that if one preserves in the configurations of Eq. (3) only the leading atomic orbitals of Th, they would be the only terms generating nonzero matrix elements, Eqs. (5)–(8), since the operators treated are radially independent. Therefore, the corresponding matrix elements with $\Omega = 0^\pm$ and $\Omega = 2$ states not included in the basis set (3) are several times smaller than those in Eqs. (4)–(8), and the matrix elements for higher excited states are suppressed even more. Since the corresponding contribution to the g factors of $H^3\Delta_1$ appear at higher orders in the perturbation, they are negligible for our treatment. For highly excited states we have additional suppression due to large energy denominators. Thus, we expect that inclusion of terms arising only from this truncated basis set should adequately describe the g factors of the $H^3\Delta_1$ state.

The external electric field mixes levels of opposite parity (with the same J as well as with $\Delta J = \pm 1$) and changes the values of the g factors. In the present work we have calculated and measured this effect for the $J = 1, 2$ states in $H^3\Delta_1$ for electric fields up to several hundred V/cm. The major effects come from mixing the rotational levels of the same electronic states, determined by the body-fixed dipole moment (9). Since the rotational (~ 40 GHz) energy spacing for the $H^3\Delta_1$ state and its distance from other electronic states (~ 25 THz) are much larger than the Ω -doublet spacing (~ 1 MHz), there is a range of electric fields where the e and f levels are almost completely mixed [$|d(J)\mathcal{E}| \gg aJ(J+1)$] while the interactions with other rotational and electronic states can be treated as a linear perturbation with respect to $\mathcal{E}$. For this linear Stark regime the difference between the g factors will be (to a good approximation) a linear function of the external electric field, with the g -factor dependence given by [21]

$$g(J, \mathcal{N}, \mathcal{E}) = \bar{g}(J) + \eta(J)|\mathcal{E}|\mathcal{N}, \quad (14)$$

where $\mathcal{N} = \text{sgn}(M\Omega\vec{\mathcal{E}} \cdot \hat{z})$. The quantity $\mathcal{N}$ refers to the molecular dipole either being aligned ($\mathcal{N} = +1$, lower energy) or antialigned ($\mathcal{N} = -1$, higher energy) with $\vec{\mathcal{E}}$, $\bar{g}(J)$ is the mean g factor of the upper and lower states, and η is a constant which depends on the molecular electronic and rotational states. Note that $g_e(J) = g(J, \mathcal{N} = -1, |\mathcal{E}| \rightarrow 0)$ and $g_f(J) = g(J, \mathcal{N} = +1, |\mathcal{E}| \rightarrow 0)$. Below, for brevity, we use this relation for the nonzero laboratory electric field as well.

III. MEASUREMENT OF g AND η

We write the energy shifts for the $M = \pm 1$ Zeeman levels in the H state in the linear Stark regime as

$$\begin{aligned} E &= -Mg(J, \mathcal{E}, \mathcal{N})\mu_B\mathcal{B} - \frac{D_{\parallel}M\Omega}{J(J+1)}\mathcal{E} - M\tilde{\mathcal{N}}\tilde{\mathcal{E}}\mathcal{E}_{\text{eff}}d_e \\ &= -M\bar{g}(J)\mu_B\mathcal{B} - \eta(J)\tilde{\mathcal{N}}M\mu_B|\mathcal{E}|\mathcal{B} - \tilde{\mathcal{N}}d(J)|\mathcal{E}| \\ &\quad - M\tilde{\mathcal{N}}\tilde{\mathcal{E}}\mathcal{E}_{\text{eff}}d_e. \end{aligned} \quad (15)$$

From left to right, these terms represent the Zeeman shift, the electric field dependence of the magnetic g factors, the dc Stark shift, and the e EDM interacting with the effective internal electric field. Here d_e is the e EDM, $\mathcal{E}_{\text{eff}} = 84$ GV/cm

[26] is the internal effective electric field, and μ_B is the Bohr magneton. A tilde over a quantity indicates the sign (± 1) of a quantity which is reversed in the experiment, $\tilde{\mathcal{B}} = \text{sgn}(\vec{\mathcal{B}} \cdot \hat{z})$, $\tilde{\mathcal{E}} = \text{sgn}(\vec{\mathcal{E}} \cdot \hat{z})$, and $\tilde{\mathcal{N}} = \mathcal{N}$ for consistency.

As discussed in detail elsewhere [5, 12, 38], the terms in Eq. (15) are determined by performing a spin-precession measurement on a pulsed molecular beam of ThO molecules. By measuring the phase accumulated by a superposition of the $M = \pm 1$ Zeeman sublevels (in any level with $J \geq 1$), we can determine the spin-precession frequency $\omega = \Delta E/\hbar$, where ΔE is the energy splitting between the $M = \pm 1$ states, and then calculate ΔE . By measuring this frequency with all possible values of $\tilde{\mathcal{N}}$, $\tilde{\mathcal{E}}$, and $\tilde{\mathcal{B}}$, we can determine each of the terms in Eq. (15) individually. Specifically, we measure the component of ω which is either even or odd under reversal (or “switch”) of $\tilde{\mathcal{N}}$, $\tilde{\mathcal{E}}$, and $\tilde{\mathcal{B}}$. We denote these components with a superscript indicating under which experimental switches the component is odd; for example, $\omega^{\mathcal{NB}}$ is the component of the spin-precession frequency which is odd under reversal of $\tilde{\mathcal{N}}$ and $\tilde{\mathcal{B}}$, but not $\tilde{\mathcal{E}}$. For the terms in Eq. (15), we have

$$\hbar\omega^{\mathcal{B}} = -\bar{g}(J)\mu_B|\mathcal{B}|, \quad (16)$$

$$\hbar\omega^{\mathcal{NB}} = -\eta(J)\mu_B|\mathcal{E}|\mathcal{B}|, \quad (17)$$

$$\hbar\omega^{\mathcal{NE}} = -d_e\mathcal{E}_{\text{eff}}. \quad (18)$$

The Stark interaction is a common-mode shift which does not cause spin precession. All measurements are performed in the $M = \pm 1$ states of $J = 1, 2, 3$ in H , since our measurement scheme relies on driving a Λ -type transition to an $M = 0$ level in the excited electronic C state. Population is transferred to the $H, J = 1, 2, 3$ states by optically pumping through the $A^3\Pi_{0+}$ electronic state. To populate $H, J = 1$ we pump through the $A, J = 0$ state, which can only decay to the $J = 1$ state in H since there is no $H, J = 0$ state. To populate the higher rotational levels we pump into higher rotational states in A , which reduces our population transfer efficiency and signal sizes; this limits the number of rotational levels which we are able to probe.

A. Measurement of η

We can extract $\omega^{\mathcal{NB}}$ (Fig. 1) from our data (using the same methods by which we extract $\omega^{\mathcal{NE}}$ to determine d_e [5]) and use the known $\mathcal{E}$ and $\mathcal{B}$ fields to determine the value of η , via

$$\eta = -\frac{\hbar\omega^{\mathcal{NB}}}{\mu_B|\mathcal{E}|\mathcal{B}|}. \quad (19)$$

With the exception of the $\mathcal{B} = 59$ mG and $J = 2$ measurements in Table I, we determined η from the same data set which was used to extract d_e . By measuring η for several values of $|\mathcal{E}|$ and $|\mathcal{B}|$, we ensure that the value of η is indeed a constant, independent of the applied fields.

The uncertainty on η comes from a combination of statistical uncertainty on $\omega^{\mathcal{NB}}$ and from a systematic uncertainty. The primary systematic error is similar to one affecting our e EDM measurement, which is discussed in more detail in Ref. [5]. Specifically, here the $\mathcal{N}$ -correlated laser detuning $\delta^{\mathcal{N}}$ (caused by differences between the Stark splitting and acousto-optical modulator frequencies used to shift the lasers into resonance)

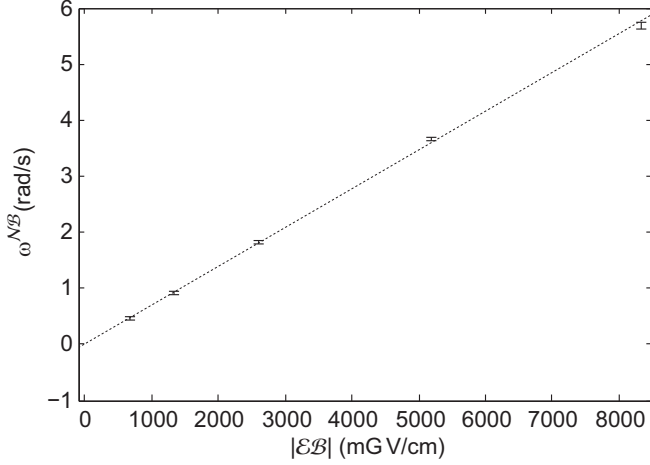


FIG. 1. Plot of ω^{NB} vs $|EB|$ for $J = 1$ with a linear fit. According to Eq. (19) this slope is $\omega^{NB}/|EB| = -\eta(1)\mu_B/\hbar$, from which we extract $\eta(1) = -0.79(1)$. Error bars are combined statistical and systematic uncertainties, as in Table I. The reduced χ^2 value of the fit is 1.5, which agrees with the expected value of 1 ± 0.7 for 4 degrees of freedom.

and the overall detuning $\delta^{(0)}$ couple to an ac Stark shift to cause the spin-precession frequency $\hbar\omega^{NB} \propto \delta^{(0)}\delta^N|B|$. Since we determine η from ω^{NB} , this will systematically change our determination of η . In the course of the systematic error analysis of our EDM search [5], we experimentally measured that $\eta^{\text{meas}}/(\delta^{(0)}\delta^N) = 2.61(2) \text{ nm V}^{-1} \text{ MHz}^{-2}$ with $|E| = 141 \text{ V/cm}$, where η^{meas} is the value of η calculated from Eq. (19) by ignoring the ac Stark shift. Given our measured average $\delta_{\text{RMS}}^{(0)} \approx 70 \text{ kHz}$ and $\delta_{\text{RMS}}^N \approx 20 \text{ kHz}$, this gives rise to a systematic uncertainty in η of $\approx 0.01 \text{ nm/V}$, which is comparable to the statistical uncertainty. The values of E and B are known to $\sim 10^{-3}$ fractionally [5], so we do not include those uncertainties in our error budget.

B. Measurement of the g factors

The measurement of $\bar{g}(1)$ was performed in a previous publication [30], and we use the value reported there of $\bar{g}(1) = -0.00440(5)$. The previous measurement did not determine the sign, but the spin-precession measurement employed here

TABLE I. Measured values of $\eta(J)$ (in units of nm/V) in different electric and magnetic fields. We expect $\eta(J)$ to be independent of E and B . Error bars are a quadrature sum of the 1σ Gaussian statistical uncertainty and the systematic uncertainty discussed in the text. $\eta(3)$ was not measured due to small signal sizes.

E (V/cm)	B (mG)	$\eta(1)$	$\eta(2)$
36	19	-0.81(2)	—
36	38	-0.79(2)	—
141	19	-0.80(1)	—
141	38	-0.80(1)	—
141	59	-0.78(2)	—
106	38	—	+0.03(2)
Weighted mean		-0.79(1)	+0.03(2)

is sensitive to signs and we find $\bar{g}(1) < 0$ (that is, the magnetic moment and the angular momentum are antialigned in the molecule).

To measure the g factor in the higher rotational (J) levels, we find the smallest magnetic field which results in a $\pi/4$ phase rotation of each Zeeman sublevel. Because our spin-precession measurement is time resolved, we choose the magnetic field B_J which results in a $\pi/4$ rotation for the molecules in the center of the beam pulse. We measure that $B_J = 19.7, 29.6$, and 35.5 mG for $J = 1, 2$, and 3 is required to impart a $\pi/4$ phase.

In terms of the flight time τ , the fields B_J are given by $\bar{g}(J)\mu_B B_J \tau = \pi/4$. If we make the assumption that τ ($\approx 1.1 \text{ ms}$) does not change during the time it takes to change the lasers to address and/or populate the other rotational levels, we can see that $\bar{g}(J)/\bar{g}(J') = B_{J'}/B_J$ for any J, J' . Since $\bar{g}(1)$ is known, we can solve for $\bar{g}(J) = \bar{g}(1) \times (B_J/B_1)$ with the values reported above. To compute an uncertainty, we make use of the fact that τ is typically observed to drift on the $\pm 1\%$ level for short time scales and that the magnetic fields were only set with a resolution of 0.7 mG . Together, this gives an overall uncertainty on the g -factor measurements (for $J > 1$) of $\approx \pm 3\%$.

IV. RESULTS AND DISCUSSION

Table II lists the measured and calculated [using Eqs. (12) and (13)] g factors for the $H^3\Delta_1$ for different quantum numbers J . For a pure Hund's case a molecule (for the details see, for example, Ref. [29]), we expect $\bar{g}(J) = -G_{\parallel}[J(J+1)]^{-1}$ [39]. However, from comparison of the experimental results (final column) to this expectation (first column) shown in Table II, we see that this scaling is badly violated. Accounting for the contribution of interaction with $Q^3\Delta_2$ (second column of Table II) leads to much better agreement between the measured and calculated values. Furthermore, accounting for perturbation from the $^3\Pi_{0\pm}$ states makes the agreement better still (third through fifth columns). $Q^3\Delta_2$ is the nearest state to $H^3\Delta_1$ and its contribution is about an order of magnitude larger than those from the $^3\Pi_{0\pm}$ states. Note, however, that the interaction with $^3\Delta_2$ (as opposed to the interaction with $^3\Pi_{0\pm}$) does not contribute in the leading order (at zero electric field) to the difference in g factors of the f and e states.

TABLE II. The g factors (in units of 10^{-3}) calculated and measured for the $H^3\Delta_1$ state in $^{232}\text{Th}^{16}\text{O}$.

J	Calculation, Eqs. (12) and (13)					Expt.
	$\bar{g}^a$	$\bar{g}^b$	g_f	g_e	$\bar{g}^c$	
1	-4.144	-4.144	-4.409	-4.391	-4.400	-4.40(5) [30]
2	-1.381	-2.362	-2.628	-2.609	-2.618	-2.7(1)
3	-0.691	-1.917	-2.182	-2.164	-2.173	-2.4(2)

^aResults when interactions with both $^3\Pi_{0\pm}$ and $^3\Delta_2$ were omitted. In this case the g factors for e and f states are equal and given by $-G_{\parallel}/J(J+1)$.

^bResults when interactions with only $^3\Pi_{0\pm}$ were omitted. In this case the g factors for e and f states are equal.

^cResults when the parameter $G_{\parallel}$ was chosen in such a way that $\bar{g}(1)$ exactly corresponds to the experimental value.

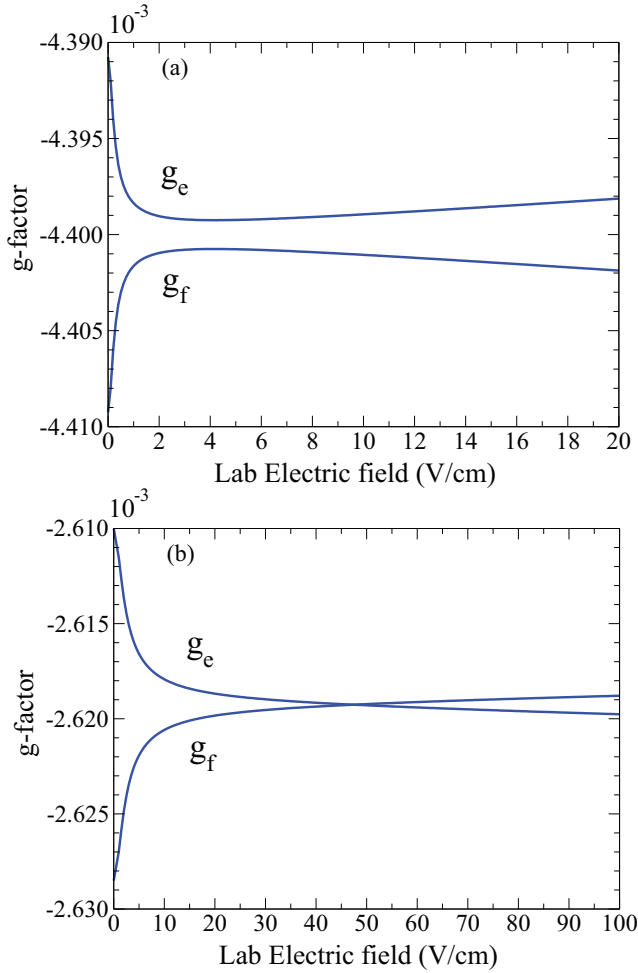


FIG. 2. (Color online) Calculated g_e and g_f for $H^3\Delta_1$ $^{232}\text{Th}^{16}\text{O}$ as functions of the electric field. Both Zeeman and Stark interactions with the $^3\Delta_2$ and $^3\Pi_{0\pm}$ states are taken into account. (a) $J = 1$ and $M = 1$. (b) $J = 2$ and $M = 1$.

In Fig. 2 the calculated g factors for the $J = 1$ and $J = 2$ levels of the ThO $H^3\Delta_1$ state are shown as functions of the laboratory electric field. Since the electric field mixes e and f levels one might expect that the initial small difference between g_e and g_f would converge to zero with increasing the electric field. Figure 2, however, shows that g_e and g_f for $J = 1$ do not tend to coincide. This fact is explained by perturbations from the $J = 2$ level, as discussed in Refs. [18,21,24]. In turn, the nearest perturbing state for $J = 2$ is $J = 1$. The energy denominator for the $J = 2$ level in the perturbation theory will have the opposite sign compared to the $J = 1$ level, and the corresponding curves for g_e and g_f cross each other.

In Fig. 3 the calculated and experimental values for $\eta(1)$ and $\eta(2)$ are shown. For small electric fields, $\eta(J)$ is a function of the electric field which converges to a constant value as the electric field increases. Both theoretical and experimental data show that for $\mathcal{E} > 36$ V/cm $\eta(1)$ can be considered as independent of $\mathcal{E}$ within experimental accuracy.

In their search for the e EDM in the PbO molecule, Bickman *et al.* [21] observed dependence of the molecular g factor on the laboratory electric field $\mathcal{E}$ and found that $\eta(1) = \bar{g}(1)D_{\parallel}/(20B_{\text{rot}})$. In the ThO $H^3\Delta_1$, $v = 0$, $J = 1$ state, we

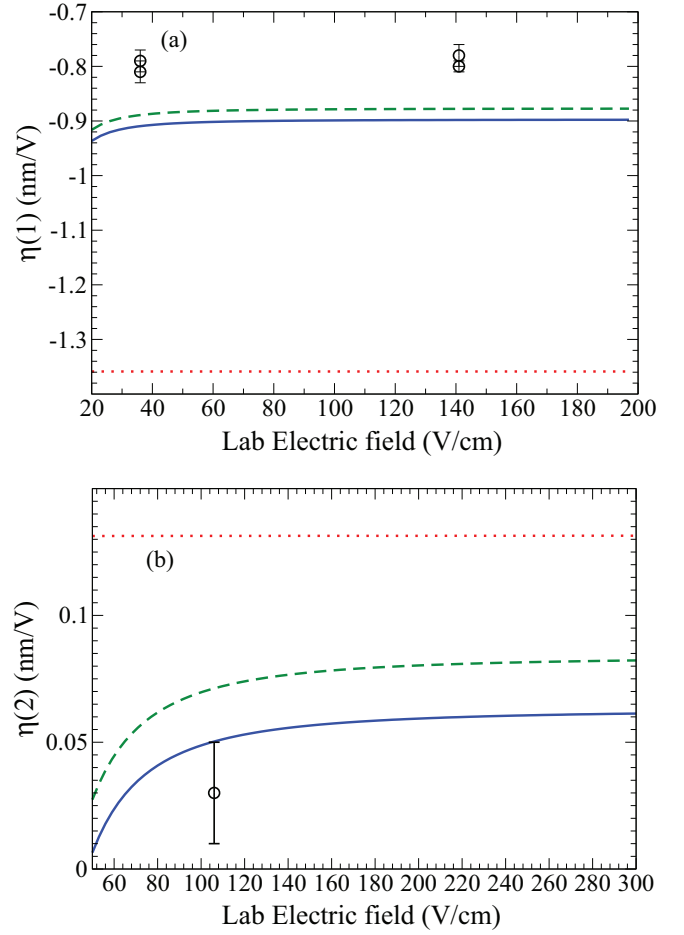


FIG. 3. (Color online) Calculated $\eta(J)$ as functions of the electric field. Solid (blue) curves: Both Zeeman and Stark interactions with the $^3\Delta_2$ and $^3\Pi_{0\pm}$ states are taken into account. Dashed (green) curves: Only the Zeeman interaction with the $^3\Delta_2$ and $^3\Pi_{0\pm}$ states is taken into account. Dotted (red) curves: Both Zeeman and Stark interactions with the $^3\Delta_2$ and $^3\Pi_{0\pm}$ states are omitted. Circles (black): Experimental values. (a) $J = 1$ and $M = 1$. (b) $J = 2$ and $M = 1$.

have $\bar{g}(1) = -0.00440(5)$ [30], $D_{\parallel} = h \times 2.13$ MHz/(V/cm) [12], and $B_{\text{rot}} = 9.76$ GHz [27], and we would therefore expect $\eta(1) \approx -1.4$ nm/V based on the treatment from Ref. [21]. Instead we measure $\eta(1) = -0.79(1)$ nm/V, as shown in Table I. The discrepancy is due to the fact that $\bar{g}(J)$ and $\eta(J)$ are much smaller in ThO than in PbO, and therefore the small perturbations from nearby electronic states considered in this paper are of comparable size to the residual values from the mechanisms considered in Ref. [21].

If the magnetic interaction with $^3\Pi_{0\pm}$ is neglected, then $g_e = g_f$ for zero electric field and mixing between e and f (with the same J) does not influence the g factors. In this case $\eta(J)$ is a linear function for both small and large electric fields [see dotted (red) curves in Fig. 3]. Similar to case for the zero-field g -factor values, the Zeeman interaction with other electronic states has a large contribution to $\eta(J)$, and including this effect makes the measured and predicted values of $\eta(J)$ much closer. Due to a large energy separation between different electronic states, the Stark interaction between electronic states, Eqs. (10) and (11), has smaller effects on the g factors of $H^3\Delta_1$. We have found, however, that it is not negligible;

taking this interaction into account significantly improves the agreement between experimental and theoretical values, particularly for $\eta(J = 2)$.

The small value of $\eta(2)$ means that the $H, J = 2$ state should be even more robust against a number of systematic errors, as compared to $H, J = 1$. Since the energy shift due to d_e does not depend on J when the molecule is fully polarized [40], performing an EDM measurement in multiple rotational levels could be a powerful method to search for and reject systematics in this type of Ω -doublet system.

ACKNOWLEDGMENTS

The PNPI-SPbU team acknowledges St. Petersburg State University for a research grant (Grant No. 0.38.652.2013) and the RFBR for Grant No. 13-02-01406. L.S. is also grateful to the President of RF for Grant No. 5877.2014.2. The molecular calculations were partly performed at the Supercomputer “Lomonosov.” The work of the Harvard and Yale teams was performed as part of the ACME Collaboration, to whom we are grateful for its contributions, and was supported by the NSF.

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