

# Quantum Hall drag of exciton condensate in graphene

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**Exciton condensate is a Bose-Einstein condensate (BEC) of electron and hole pairs bound by the Coulomb interaction<sup>1,2</sup>. In an electronic double layer (EDL) under strong magnetic fields, filled Landau states in one layer bind with empty states of the other layer to form exciton condensate<sup>3-9</sup>. Here we report exciton condensation in bilayer graphene EDL separated by hexagonal boron nitride (hBN). Driving current in one graphene layer generates a near-quantized Hall voltage in the other layer, signifying coherent exciton transport<sup>4,6</sup>. Owing to the strong Coulomb coupling across the atomically thin dielectric, quantum Hall drag in graphene appears at a temperature ten times higher than previously observed in GaAs EDL. The wide-range tunability of densities and displacement fields enables exploration of a rich phase diagram of BEC across Landau levels with different filling factors and internal quantum degrees of freedom. The observed robust exciton condensation opens up opportunities to investigate various many-body exciton phases.**

An exciton BEC is formed when a large fraction of excitons occupy the ground state, establishing macroscopic coherence with weak dipolar repulsion<sup>1,3</sup>. However, optically generated excitons have short lifetimes. They can quickly recombine and release a photon, which leads to the annihilation of excitons. By trapping the released photon in an optical cavity, recent studies have shown the BEC of exciton-polaritons, consisting of a superposition of an exciton and a photon<sup>10-13</sup>. Another way to achieve a large density of long-lived excitons is to place electrons and holes in spatially-separated parallel conducting

25 layers, where excitons can form across the layers. In semiconducting EDLs, such indirect  
 26 excitons can be formed by optical excitation<sup>14</sup> or electrical doping<sup>15</sup>. One salient feature of  
 27 the exciton BEC is dissipationless exciton transport, consisting of counter-flowing  
 28 electrical currents carried by co-traveling electrons and holes<sup>4</sup>. The first experimental  
 29 observation of this superfluid exciton flow was demonstrated in GaAs EDLs under a strong  
 30 magnetic field, in which a strong correlation is formed between electron-like and hole-like  
 31 quasi-particles in quantizing orbits<sup>3-9</sup>.

32         The magnetic-field-induced layer coherence of the EDL can be established in the  
 33 following way. When a two-dimensional (2D) electron gas of density  $n$  is subject to a  
 34 perpendicular magnetic field  $B$ , the kinetic energy of electrons is quantized to discrete  
 35 Landau levels (LLs). Each LL contains  $n_0 = \frac{eB}{h}$  degenerate Landau orbits per unit area,  
 36 where  $e$  is electron charge and  $h$  is Planck's constant. If all the orbits in a LL are occupied  
 37 (i.e., the filling factor  $\nu = n/n_0$  is an integer), the 2D electron system forms a quantum  
 38 Hall state. In the EDL, the filling factor of the individual layer can be specified by  $\nu_{top} =$   
 39  $n_{top}/n_0$  and  $\nu_{bot} = n_{bot}/n_0$ , where  $n_{top}$  and  $n_{bot}$  are the density of top and bottom layer,  
 40 respectively. If LLs in both layers are partially filled, i.e.,  $\nu_{top}$  and  $\nu_{bot}$  are non-integer  
 41 numbers, neither layer can form a quantum Hall state on its own. However, Coulomb  
 42 repulsion forces the electrons in the two layers to occupy different orbitals in space, leading  
 43 to spatial anti-correlation between layers. Notably, when the total filling fraction,  $\nu_{tot} =$   
 44  $\nu_{top} + \nu_{bot}$ , becomes an integer, the two layers together can form a coherent state in  
 45 which each filled state (quasi-electron) in one layer correspond to an empty state (quasi-  
 46 hole) in the other layer. These bound empty-filled states can be described as excitons in the  
 47 quantum Hall scenario and yield a strong response in the Coulomb drag experiment:  
 48 driving current in one layer generates a quantized Hall drag voltage in the other layer. To  
 49 be specific, the ratio between Hall drag voltage ( $V_{xy}^{drag}$ ) and drive current ( $I^{drive}$ ), defined

50 as Hall drag resistance, is then quantized as  $R_{xy}^{drag} = V_{xy}^{drag} / I^{drive} = \frac{h}{v_{tot}e^2}$ . Meanwhile,  
 51 Hall resistance of the drive layer ( $R_{xy}^{drive}$ ), obtained from the drive Hall voltage ( $V_{xy}^{drive}$ ), is  
 52 also quantized to the same value despite having a partially filled LL, while the longitudinal  
 53 voltages in both layers vanishes.

54 Quantized Hall drag for  $v_{tot} = 1$  has been observed in the lowest LLs in GaAs  
 55 EDLs<sup>6</sup>. Coherent tunneling between the layers<sup>5</sup> and perfect current drag measurements<sup>9</sup>  
 56 further confirmed the presence of the interlayer coherence and the superfluid exciton flow.  
 57 The BEC realized in semiconducting EDLs, however, turns out to be rather fragile, with a  
 58 BEC transition temperature  $T_c$  in the sub-Kelvin range. This fragility is mainly caused by a  
 59 relatively large EDL separation  $d$  required. It is noted that  $T_c$  is proportional to the  
 60 characteristic energy scale  $e^2/\epsilon\ell$ , where  $\epsilon$  is the dielectric constant and  $\ell = (\hbar/eB)^{1/2}$  is  
 61 the magnetic length specifying the distance between quasi-particles in a LL<sup>16,17</sup>. Also, the  
 62 exciton BEC only appears in the strong coupling regime<sup>4</sup>, where the  $d/\ell$  ratio is below the  
 63 critical value of  $d/\ell < 2$ . Thus reducing  $d$  substantially below the limit of the  
 64 semiconducting EDL will likely enhance  $T_c$  and increase the exciton binding energy.

65 Recent progress on 2D van der Waals heterostructures has created a new  
 66 opportunity to build EDLs using atomically thin materials<sup>18-21</sup>. Owing to electron-hole  
 67 symmetry and extremely light carrier mass, EDLs consisting of mono- and bilayer  
 68 graphene have been of particular interest to realize an exciton BEC<sup>22-25</sup>. Furthermore,  
 69 tunneling currents in graphene-hBN-graphene heterostructures are not appreciable when  $d$   
 70  $> 1.5$  nm at small biases, due to the large bandgap of hBN and the lattice direction  
 71 mismatch between graphene layers<sup>18,26</sup>. Initial experiments performed in graphene-hBN-  
 72 graphene heterostructures demonstrated a strong Coulomb drag effect in the semiclassical  
 73 regime realized at high temperatures, exhibiting the strong interaction between the two  
 74 layers in the zero and finite magnetic fields<sup>18-20</sup>. However, experimental evidence of

75 interlayer coherence has yet to be found. In this work, with improved device quality and  
 76 fabrication technique (see supplementary information (SI)), we demonstrate magnetic-field-  
 77 induced exciton condensation in graphene EDL.

78 Our devices are made of two Bernal stacked bilayer graphene (BLG) sheets  
 79 separated by 3 nm hBN and encapsulated by two thicker hBN layers (20~30 nm) (Fig. 1a,  
 80 b). The two graphene layers are independently contacted by multiple electrodes (see SI for  
 81 details). Both graphene layers have mobility  $0.5\sim 1\times 10^6\text{ cm}^2/\text{Vs}$  and exhibit symmetry  
 82 breaking quantum Hall states at fields as low as 5 T (SI, Fig. S3-4). No appreciable  
 83 tunneling current is measured above the noise level, providing a lower bound on the  
 84 tunneling resistance of 1 G $\Omega$ . The voltages applied to the top gate ( $V_{TG}$ ), the bottom gate  
 85 ( $V_{BG}$ ) and the interlayer bias between graphene layers ( $V_{int}$ ) tune the carrier densities of the  
 86 top and bottom graphene layers ( $n_{top}, n_{bot}$ ):  $n_{top} = C_{TG}V_{TG} - C_{int}V_{int}$ ;  $n_{bot} = C_{BG}V_{BG} +$   
 87  $C_{int}V_{int}$ . Here  $C_{TG}$ ,  $C_{BG}$ , and  $C_{int}$ , are capacitances between the top gate and top layer, the  
 88 bottom gate and bottom layer, and between the top and bottom graphene layers,  
 89 respectively. By controlling  $V_{TG}$ ,  $V_{BG}$ , and  $V_{int}$ , we can also adjust the average displacement  
 90 fields;  $D_{top} = (C_{TG}V_{TG} + C_{int}V_{int})/2$  and  $D_{bot} = (-C_{BG}V_{BG} + C_{int}V_{int})/2$ , for the top  
 91 and bottom layer, respectively. For the drag measurements, we apply current  $I^{drive}$  only in  
 92 the top layer and measure the Hall resistance  $R_{xy}^{drive}$  of the current-carrying (drive) layer,  
 93 and magneto- and Hall drag resistance,  $R_{xx}^{drag}$  and  $R_{xy}^{drag}$ , of the drag layer under a  
 94 perpendicular magnetic field  $B$ . Owing to the Onsager relation, switching the drive and  
 95 drag layer produces experimentally equivalent drag results (SI, Fig. S5).

96 Fig. 1c shows measurements of  $R_{xy}^{drive}$ ,  $-R_{xx}^{drag}$ ,  $R_{xy}^{drag}$  under  $B = 25$  T,  
 97 corresponding to the strong coupling limit ( $\ell = 5.1$  nm and  $d/\ell = 0.58$ ). In this plot, we  
 98 adjust  $V_{TG}$  and  $V_{BG}$  such that the filling fractions of each layer are balanced ( $\nu \equiv \nu_{drive} =$   
 99  $\nu_{drag}$ ). We observe that each layer exhibits its own quantum Hall (QH) effect. For  $\nu \geq 1$ ,

100  $R_{xy}^{drive}$  exhibit QH plateaus at the values  $(R_{xy}^{drive})^{-1} = \frac{e^2}{h}, \frac{4}{3} \frac{e^2}{h}, \frac{2e^2}{h}$ . In these well-developed  
 101 integer ( $\nu=1, 2$ ) and fractional ( $\nu=4/3$ ) QH regimes of the individual layers, we find no  
 102 appreciable drag signal ( $R_{xx}^{drag} \approx R_{xy}^{drag} \approx 0$ ). The vanishing drag signals at low  
 103 temperatures are expected in the semiclassical picture due to the diminishing scattering  
 104 phase space<sup>27</sup>. However, the observed drag signals are significantly enhanced when the first  
 105 LL of both layers are partially filled ( $\nu < 1$ ). In particular, for  $\nu=1/2$ , where both layers are  
 106 half-filled and thus  $\nu_{tot} = \nu_{drive} + \nu_{drag} = 1$ , the Hall drag signal reaches close to the  
 107 quantization value of  $h/e^2 = 25.8 \text{ k}\Omega$ , while the magneto-drag ( $R_{xx}^{drag}$ ) dips to nearly  
 108 zero. Under the same condition, the Hall resistance in the drive (top) layer, which originally  
 109 rises beyond  $h/e^2$  as  $\nu_{drive}$  drops below one (i.e., partially filled LL), re-enters  $h/e^2$  again  
 110 at  $\nu_{tot}=1$ . This re-entrant behavior of  $R_{xy}^{drive}$  to the same quantized value of  $R_{xy}^{drag}$   
 111 indicates that the entire EDL behaves like a single  $\nu=1$  quantum Hall system despite that  
 112 LLs in each layer are only partially filled.

113 The quantized Hall drag and re-entrant QHE in the drive layer have been observed  
 114 previously in the GaAs EDLs for  $\nu_{tot}=1$  and are considered as a strong evidence of  
 115 interlayer coherence and exciton superfluidity<sup>6</sup>. We note, however, the unambiguous  
 116 demonstration of superfluidity and coherence requires further measurements. A simple  
 117 physical picture for the observed quantized Hall drag can be built upon a two-fluid picture.  
 118 In this model, currents in each layer are carried by excitons in the bulk ( $I_{ex}^{(i)}$ ) and quasi-  
 119 particles flowing on the edge ( $I_{qp}^{(i)}$ ), where the superscript is the layer index. Excitons  
 120 generate counter flow currents  $I_{ex}^{drag} = -I_{ex}^{drive}$ ; and the zero accelerating electric force  
 121 requirement on superfluid excitons demands  $V_{xy}^{drive} = V_{xy}^{drag} = V_{xy}$ . In addition, boundary  
 122 conditions of the drag and drive layers requires  $I_{ex}^{drag} + I_{qp}^{drag} = 0$ ,  $I = I_{ex}^{drive} + I_{qp}^{drive}$ .  
 123 Furthermore, by considering the two layers as a single coherent quantum Hall system at

124 filling fraction  $\nu_{tot}$ , we have  $I_{qp} = I_{qp}^{drag} + I_{qp}^{drive} = \frac{\nu_{tot}e^2}{h}V_{xy}$ . Summing up, we obtain the  
 125 experimental observation  $R_{xy}^{drive} = R_{xy}^{drag} = h/\nu_{tot}e^2$  with vanishing  $R_{xx}^{drag}$  and  $R_{xx}^{drive}$ .

126 We found that the observed quantized Hall drag in graphene is much more robust  
 127 than that of the GaAs EDLs. The signatures of the exciton condensate, i.e., nearly quantized  
 128  $R_{xy}^{drag}$  and re-entry behavior of  $R_{xy}^{drive}$ , persist up to a few Kelvin for  $\nu_{tot} = 1$  at  $B = 25$  T  
 129 (Fig. 1c inset). For quantitative analysis, we compute the counter-flow resistances  $R_{xy}^{CF}$  and  
 130  $R_{xx}^{CF}$  and plot them as a function of  $1/T$  at  $\nu_{tot} = 1$  (SI, Fig. S7). While the theoretical  
 131 expectation for 2D BEC transition is the Kosterlitz-Thouless transition<sup>16,28</sup>, we find that the  
 132 vanishing  $R_{xy}^{CF}$  and  $R_{xx}^{CF}$  exhibit thermally activating behavior similar to what has been  
 133 observed in GaAs system<sup>6</sup>. However, the activation gap we obtained ( $\Delta \approx 8$  K) is ten  
 134 times larger than previous reported (SI, Fig. S7b).

135 The exciton BEC in graphene is also found to be robust against the density  
 136 imbalance between layers.<sup>29</sup> The signatures of the exciton condensation, i.e.,  $R_{xy}^{drag} \approx$   
 137  $R_{xy}^{drive} \approx h/e^2$  and  $R_{xx}^{drag} \approx R_{xx}^{drive} \approx 0$  withstand a range of gate voltages satisfying  
 138  $\nu_{drag} + \nu_{drive} = 1$ , corresponding to the diagonal line specified in Fig. 1d-f. For a more  
 139 quantitative analysis, we plot  $R_{xy}^{drag}$  cut along this diagonal line as an overlay graph in Fig.  
 140 1d (white trace). The level of  $R_{xy}^{drag}$  quantization indicates that the BEC persists for the  
 141 density imbalance  $\frac{\Delta n}{n_{tot}} = \frac{n_{drag} - n_{drive}}{n_{drag} + n_{drive}}$  up to  $\sim \pm 30\%$ . Beyond this limit the more stable  
 142 integer QH states ( $\nu_{drag}$  or  $\nu_{drive} = 0$  or  $1$ ) in each layer take over the exciton BEC phase.

143 While the exciton BEC has been discovered only for the half-filled lowest LL in the  
 144 GaAs EDLs, the gate tunability in graphene EDL devices allows us to explore the phase  
 145 diagram of possible condensate states other than  $\nu_{tot} = 1$ . Fig. 2 shows experimental survey  
 146 for  $R_{xy}^{drag}$  as a function of  $\nu_{drive}$  and  $\nu_{drag}$ , covering the electron-electron ( $\nu_{drive}, \nu_{drag} >$   
 147  $0$ ) and hole-hole ( $\nu_{drive}, \nu_{drag} < 0$ ) regimes. Remarkably, we find at least two additional  
 148 interlayer correlated states in these regimes:  $(\nu_{drive}, \nu_{drag})$  centered near  $\sim (0.35, 2.65)$  and

149 (-1.5, -1.5), corresponding to the drag between  $\frac{1}{2}$  -  $2\frac{1}{2}$  filled electron LLs ( $\nu_{tot} = 3$ ) and  
 150  $1\frac{1}{2}$  -  $1\frac{1}{2}$  filled hole LLs ( $\nu_{tot} = -3$ ), respectively. Similar to the BEC in  $\nu_{tot} = 1$ , these  
 151 states exhibit the near-quantized Hall drag  $R_{xy}^{drag} \approx h/\nu_{tot}e^2$  and  $R_{xx}^{drag} \approx 0$ , for a range of  
 152  $(\nu_{drive}, \nu_{drag})$  satisfying  $\nu_{drive} + \nu_{drag} = \nu_{tot}$  (see Fig 2. b-j). These Hall drag features  
 153 appear as diagonals in the  $(\nu_{drive}, \nu_{drag})$  plots and are confined to the sectors  
 154 corresponding to partially filled first (drive) and third (drag) electron LLs (with all  
 155 symmetries are lifted) and partially filled second (drive and drag) hole LLs. While we  
 156 cannot rule out other possible scenario compatible with experimental observation, we  
 157 interpret these interlayer correlated states as exciton BEC for  $\nu_{tot} = \pm 3$ . Measurements at  
 158 lower magnetic fields also reveal a signature of developing exciton BEC for  $(\nu_{drive},$   
 159  $\nu_{drag})=(2.5, 0.5)$ , the symmetric pair for  $(0.5, 2.5)$  discussed above (SI, Fig. S5&8). The  
 160 relatively weak presence of this symmetric pair is presumably due to the quality difference  
 161 between the top and bottom graphene layers. We also remark that while  $R_{xy}^{drag} \approx$   
 162  $h/\nu_{tot}e^2$  and  $R_{xx}^{drive} \approx R_{xx}^{drag} \approx 0$  are observed in the  $\nu_{tot} = \pm 3$  state, we find  $|R_{xy}^{drive}| >$   
 163  $h/\nu_{tot}e^2$  (Fig. 2e and k). Together with less developed quantization of  $R_{xy}^{drag}$  in these  
 164 states, compared to  $\nu_{tot} = 1$ , we speculate that a dissipative exciton transport of a fragile  
 165 BEC is responsible for this incomplete re-entrant QHE.

166 Interestingly, our experimental observations strongly indicate that the apparent  
 167 electron-hole symmetry of LLs is broken for the exciton BEC. For example, the  $(0.5, 0.5)$   
 168 BEC exists while  $(-0.5, -0.5)$  is absent. The electron-hole asymmetry has been observed in  
 169 the filling fraction sequences of the fractional quantum Hall effect in bilayer graphene and  
 170 related with the orbital degeneracy of bilayer graphene LLs<sup>30</sup>.

171 We note that the existence of the exciton BEC at fixed  $(\nu_{drive}, \nu_{drag})$  sensitively  
 172 depends on the  $V_{int}$  (Fig.3 and Fig. S8-10). When the density of each layer is kept close to  
 173 half-filling by coordinately tuning  $V_{BG}$  and  $V_{TG}$ ,  $V_{int}$  changes the displacement field exerted

174 on both layers,  $D_{top} = C_{int}V_{int} + n_{top}/2$  and  $D_{bot} = C_{int}V_{int} - n_{bot}/2$ . Fig. 3c shows  
 175  $R_{xy}^{drag}$  as a function of  $D_{top}$  (top axis of Fig. 3b) and  $D_{bot}$  (bottom axis of Fig. 3d) while  
 176 keeping  $\nu_{tot} = 1$  at B=13T, T=1.5K. We observe that  $R_{xy}^{drag}$  undergoes multiple distinct  
 177 transitions between high and low values as  $V_{int}$  changes. By comparing the displacement  
 178 fields of these transitions with those of the integer quantum Hall transitions of each layer  
 179 (Fig. 3b, d, Fig. S10a), we found a close connection between the Hall drag and the LL  
 180 character of each layer.

181 For a single bilayer graphene, the lowest Landau level (LLL) have eight-fold  
 182 degeneracy in the single particle picture (between  $\nu = -4$  and  $\nu = 4$ ). This SU(8)  
 183 symmetry space consists of spin degeneracy  $|\uparrow\rangle$  and  $|\downarrow\rangle$ , valley degeneracy  $K$  and  $K'$  and  
 184 orbital degeneracy of  $N = 0, 1$ <sup>31-34</sup>. In high quality samples, these symmetries are broken by  
 185 quantum Hall ferromagnetism (QHFM), and different symmetry-breaking states can be  
 186 found at different displacement fields for each filling factor<sup>31-34</sup>. The symmetry-breaking  
 187 state  $\nu = 1$  has three transition points at  $D = 0$  and  $D = \pm D_1$ , and  $\nu = 0$  has four transition  
 188 points at  $D = \pm D_2, \pm D_3$ , which can be identified in Fig. 3b, d. Across these transitions, the  
 189 fully filled LLs have different spin, valley or orbital indexes. For partially filled LLs, layer  
 190 polarization and orbital character were identified by a recent study using capacitance  
 191 measurements<sup>34</sup>. The partially filled LL  $0 < \nu < 1$  is found to hold different layer- and  
 192 orbital-polarized states at different displacement fields (Fig. 3a) (+/- denote the layer  
 193 polarization, which is equivalent to valley polarization  $K/K'$  in the lowest LL, and 0/1  
 194 denote the orbital index). The transitions between these states line up with the transitions of  
 195  $\nu = 1$  and  $\nu = 0$  states regarding to displacement field. In our experiment, the  $\nu_{tot} = 1$   
 196 state is formed between two partially filled bilayer graphene with  $0 < \nu_{top}, \nu_{bot} < 1$ . We  
 197 found that Hall drag is suppressed when the partially filled LLs of one bilayer graphene or  
 198 both bilayer graphene are in the N=1 orbital state (shaded regions in Fig. 3c and Fig. S10).



199 This also explains the absence of other integer total filling factor states and the broken  
 200 electron-hole symmetry, as the  $-1 < \nu < 0$  ( $0 < \nu < 1$ ) LL is polarized in the N=1 (N=0)  
 201 orbital state under the same displacement field; the latter is capable of forming an exciton  
 202 BEC while the former is not. We speculate that the inability of the N=1 orbit to establish an  
 203 interlayer correlated state is due to its broader spatial wavefunction (Fig. 3a right) and thus  
 204 weaker interaction. Similarly, the weaker Hall drag signal in the region where  $D_{top} >$   
 205  $0$  and  $D_{bot} < 0$  can be related to the weaker interaction when the wavefunctions of the two  
 206 layers are further apart due to the opposite layer polarization.

## 207 **Methods**

208 **Sample fabrication** The five single-crystal layers of graphene and hBN (Fig. S1a) are  
 209 prepared by mechanical exfoliation and van der Waals (vdW) transfer technique<sup>35</sup>. During  
 210 the process, we choose two strip-shape bilayer graphene and align them into a cross, so we  
 211 can use the overlapped part as the main channel area while fabricating individual contacts  
 212 onto the non-overlapped parts (Fig. S1b). The edge contacts and the top gate are fabricated  
 213 after etching the entire stack into the final device geometry. Usually, the parts of graphene  
 214 near metal contacts are slightly doped and form unwanted PN junctions due to the metal-  
 215 graphene work function mismatch. These contact-induced local PN junctions cause contact  
 216 barriers under high magnetic fields. In order to address this problem, we fabricate local top  
 217 gates (contact gates) to dope the area of graphene around the contacts. These contact gates  
 218 are adjusted to highly dope graphene leads next to the metal electrodes with the same  
 219 carrier type of the channel (Fig. S1c).

220 **Drag measurements** In most of our measurements, we use the top layer as the drive layer  
 221 and the bottom layer as the drag layer (switching the drive and drag layers does not affect  
 222 our drag experiment results as shown in Fig. S5). We apply  $I^{drive} = 2\text{nA}$  AC current  
 223 (17.7Hz) to the drive layer and measure the voltage drop along the longitudinal direction in

224 the drag layer to obtain  $V_{xx}^{drag}$ . We also measure the voltage drops along the perpendicular  
 225 direction in the drag and drive layers to obtain  $V_{xy}^{drag}$  and  $V_{xy}^{drive}$ , respectively. The magneto  
 226 and Hall drag resistances are obtained by  $R_{xx}^{drag} = V_{xx}^{drag} / I^{drive}$  and  $R_{xy}^{drag} = V_{xy}^{drag} / I^{drive}$   
 227 from this measurement. One of the contacts in the drag layer is connected to ground  
 228 through a  $1M\Omega$  resistor to allow the gates to tune the density of the drag layer.

229 A typical way to drive current in lock-in measurements is applying AC bias voltage  $V^{drive}$   
 230 on one side of the graphene channel while grounding the other side. However, in Coulomb  
 231 drag measurements, biasing the drive layer employing this scheme can create spurious drag  
 232 signals in the drag layer due to drive bias induced AC gating. Because of the finite contact  
 233 and channel resistances of the drive layer, the direct biasing scheme raises the potential in  
 234 the middle of the drive layer to  $\sim V^{drive} / 2$  with respect to ground. Since the drag layer is  
 235 grounded, an AC interlayer bias of  $\sim V^{drive} / 2$  is produced accordingly. In the previous drag  
 236 experiments performed in GaAs double quantum wells, it has been shown that this AC  
 237 interlayer bias induces spurious drag signals<sup>36</sup>. In order to prevent the AC interlayer bias,  
 238 we employ a bridge setup<sup>37</sup> as shown in Fig. S2. In this scheme, the initial 4 Volts AC  
 239 voltage is reduced down to 4mV through a voltage divider. Then this 4mV AC voltage is  
 240 fed into the bridge through a 1:1 ground-isolating transformer. By tuning the variable  
 241 resistor in the bridge, we can adjust the AC electrical potential in the middle of the drive  
 242 layer to approximate zero. The 4mV is then converted into  $\sim 2nA$  by passing through two  
 243  $1M\Omega$  resistors in series. This setup also allows us to control the DC interlayer bias  $V_{int}$ .  
 244 To monitor the drive current, we measure the voltage across one of the two  $1M\Omega$   
 245 resistors.

246 **Data Availability** The data that support the plots within this paper and other findings of  
 247 this study are available from the corresponding author upon reasonable request.

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249 **References**

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343

### 344 **Figure legends**

345 **Figure 1 | Quantized Hall drag for  $\nu_{tot} = 1$  state in bilayer graphene double layers. a,**  
 346 schematic diagram of device and measurement setup. **b,** optical microscope image of the  
 347 device. Metal leads on the left and right of the image (three on each side) contact the top  
 348 layer graphene, while others contact the bottom layer graphene. The blue shaded area of  
 349 graphene is under the top gate; white and green shaded regions are under the contact gate.  
 350 The contact gates support highly transparent electrical contacts under high magnetic fields,  
 351 providing reliable data away from  $\nu = 0$  insulating state. **c,**  $R_{xy}^{drag}$ ,  $R_{xx}^{drag}$ ,  $R_{xy}^{drive}$  as a  
 352 function of filling factors of both layers at B=25T and T=300mK. The exciton BEC can be  
 353 recognized by near quantized Hall drag ( $R_{xy}^{drag} = \frac{h}{e^2}$ ,  $R_{xx}^{drag} = 0$ ) with the simultaneous re-  
 354 entrant quantum Hall in the drive layer. **c inset,** temperature dependence ( $T=0.9, 2.29, 3.13,$   
 355  $4.35, 6, 8, 10$ K) of  $R_{xy}^{drag}$  at B=25T. **d, e, f,**  $R_{xy}^{drag}$ ,  $-R_{xx}^{drag}$ ,  $R_{xy}^{drive}$  as a function of filling  
 356 fractions  $\nu_{top}$  and  $\nu_{bot}$ , computed from  $V_{TG}$  and  $V_{BG}$ . The exciton BEC region appears as a  
 357 diagonal region satisfying  $\nu_{top} + \nu_{bot} = 1$ . The white trace in **d** shows the value of  
 358  $R_{xy}^{drag}$  (axis on the left) along  $\nu_{tot} = 1$  line (dashed line in **d**). For more quantitative  
 359 analysis, we also present several traces of the color plot in SI Fig. S11.

360 **Figure 2 | Exciton BEC in various LL fillings. a**,  $R_{xy}^{drag}$  as a function of the top and  
 361 bottom layer filling factors at  $B=25T$ ,  $T=300mK$  and  $V_{int}=-0.05V$ . Besides  $(\nu_{drag},$   
 362  $\nu_{drive}) = (0.5, 0.5)$ , a different exciton BEC state is found near  $(0.5, 2.5)$ . **b, c, d**,  
 363 zoomed-in plot of  $R_{xy}^{drag}$ ,  $R_{xx}^{drag}$ ,  $R_{xy}^{drive}$  around  $\nu_{tot} = 3$  at a higher field of  $B=31T$ . **e**,  
 364 line-cut of  $R_{xy}^{drag}$ ,  $R_{xx}^{drag}$ ,  $R_{xy}^{drive}$  along dashed line show in **b, c, d**. **f**,  $R_{xy}^{drag}$  as function of  
 365 filling factors at  $B=25T$ ,  $T=300mK$  and  $V_{int}=0.15V$ . Additional exciton BEC state in the  
 366 hole-hole regime is identified around  $(\nu_{drag}, \nu_{drive}) = (-1.5, -1.5)$ . **g, h, i, j**,  
 367  $R_{xy}^{drag}$ ,  $R_{xx}^{drag}$ ,  $R_{xy}^{drive}$ ,  $R_{xx}^{drive}$  at the same condition as **f**. **k**, line-cut  
 368 of  $R_{xy}^{drag}$ ,  $R_{xx}^{drag}$ ,  $R_{xy}^{drive}$ ,  $R_{xx}^{drive}$  along the dashed line in **g, h, i, j**. The horizontal dashed  
 369 lines in **e** and **k** indicate  $\pm \frac{h}{3e^2}$  where  $R_{xy}^{drag}$  and  $R_{xy}^{drive}$  are expected to be quantized to.

370 **Figure 3 | Phase transition of  $\nu_{tot} = 1$  exciton BEC induced by transverse electric**  
 371 **field. a**, schematic diagram of Landau levels sequence (left) and wave functions (right) of  
 372 bilayer graphene QHFM states for the lowest LL corresponding to  $-4 < \nu < 4$ . In the left  
 373 diagram, x direction represents displacement field  $D$  and colored lines denote QHFM  
 374 Landau levels with different orbital (0/1), layer (+/-) and spin ( $\uparrow/\downarrow$ ) quantum numbers, as  
 375 noted next to the lines. Different colors are used for different orbital and layer quantum  
 376 numbers. As the displacement field changes, the colored lines cross each other,  
 377 representing QHFM transitions induced by the displacement field. The horizontal black  
 378 dashed line marks charge neutrality ( $\nu = 0$ ) and the horizontal white dashed line marks  
 379 Fermi level of half-filled first LL ( $\nu = 1/2$ ). The diagram on the right depicts wave  
 380 functions of different bilayer graphene QHFM states, with the same color code as the lines  
 381 in the left diagram. **b (d)**, longitudinal resistance of top (bottom) bilayer graphene as a  
 382 function of displacement  $D_{top}$  ( $D_{bot}$ ) and density  $n_{top}$  ( $n_{bot}$ ) at  $B = 13T$  and  $T=1.5K$ . The  
 383 QHFM transitions are marked with arrows. The data in **b** is taken at a fixed  $V_{BG} = -5.5V$   
 384 and the data in **d** is taken at  $V_{TG} = -1.1V$ . **c**,  $R_{xy}^{drag}$  (blue curve) as a function of  $D_{top}$  (top

385 axis of **b**) or  $D_{bot}$  (bottom axis of **d**) for  $\nu_{tot} = 1$  state at  $B=13T$  and  $T=1.5K$ . Each data  
 386 point is taken at a different  $V_{int}$ , with  $V_{BG}$  and  $V_{TG}$  tuned around  $\nu_{tot} = 1$  to maximize  
 387  $R_{xy}^{drag}$  (filling factor  $\nu_{top}, \nu_{bot}$  calculated from the gate voltages are marked by the  
 388 horizontal dashed line in **b** and **d**). The colored bars on the top and bottom of the plot  
 389 represent orbital and layer character of the half-filled LL ( $\nu = 1/2$ ) of the top and bottom  
 390 bilayer graphene with the same color code as **a**. The orange and green shaded regions of the  
 391 main plot which signify  $N=1$  orbital states of the top and bottom layer coincide well with  
 392 where the Hall drag vanishes, indicating  $N=1$  orbit is incapable of forming exciton BEC  
 393 phase.