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Observation of Elastic Doublon Decay in the Fermi-Hubbard Model

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We investigate the decay of highly excited states of ultracold fermions in a three-dimensional optical lattice. Starting from a repulsive Fermi-Hubbard system near half filling, we generate additional doubly occupied sites (doublons) by lattice modulation. The subsequent relaxation back to thermal equilibrium is monitored over time. The measured absolute doublon lifetime covers two orders of magnitude. In units of the tunneling time $\hbar/J$ it is found to depend exponentially on the ratio of on-site interaction energy $U$ to kinetic energy $J$. We argue that the dominant mechanism for the relaxation is a simultaneous many-body process involving several single fermions as scattering partners. A many-body calculation is carried out using diagrammatic methods, yielding fair agreement with the data.

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Understanding the far-from-equilibrium dynamics of strongly correlated systems is a highly challenging task. Even the identification of the basic processes involved and the associated time scales is nontrivial when the system cannot be described by weakly interacting excitations or quasiparticles. In these systems, dynamics may couple states with widely different energies making the description in terms of a restricted set of low energy states impossible. While progress has been achieved for one-dimensional systems [1, 2], and references therein), these results can typically not be extended to higher dimensions.

The main difficulty in analyzing non-equilibrium dynamics in the setting of condensed matter experiments is the strong coupling to the environment, which introduces extrinsic relaxation mechanisms and makes it challenging to prepare far-from-equilibrium initial states in a controlled way. By contrast, the nearly perfect isolation of many-body systems realized with ultracold atoms makes them a perfect candidate for studying the intrinsic dynamics of strongly correlated systems. In the setting of ultracold atoms it is possible to prepare a well-controlled initial state, evolve it under the action of a precisely defined microscopic Hamiltonian, and monitor the effects of the characteristic relaxation process [3].

In this Letter, we take advantage of the recent realization of the repulsive Fermi-Hubbard model with ultracold atom systems [4–6] to investigate the relaxation of artificially created highly excited states. This problem appears in diverse contexts like multiphonon decay of excitons in semiconductors [7], pump-probe experiments [8] and dynamics of resonances in nuclear matter [9]. Due to the negligible coupling to an external environment, we are able to carry out a direct comparison of experiment and theory. The interpretation of these results shows the importance of high-order scattering processes in bridging the energy gap between low- and high-energy excitations and how they can lead to exponentially slow thermalization.

In the experiment, we study the time evolution of doubly occupied lattice sites (doublons) in the repulsive Fermi-Hubbard model. This model describes fermionic particles hopping on a lattice with tunneling $J$ and on-site repulsion $U$ and is realized by a two-component Fermi gas in an optical lattice. In the context of a dilute Bose-Hubbard system isolated repulsively bound pairs have been experimentally identified and studied [10].

We report on the observation of elastic decay of artificially created doublons [5–11] into single particles. The resulting lifetime is found to increase exponentially with the ratio $U/6J$ (i.e. the lifetime becomes longer as the interactions become stronger). We argue that a doublon, having an excess energy $U$, decays in a scatter-
ing process involving several single fermions, cf. Fig. 1. Since each of these scattering partners can only absorb an average energy of 6J, the number of virtual states involved in the simultaneous many-body process is U/6J. Hence the decay is exponentially suppressed for increasing U/6J. We find fair agreement with diagrammatic calculations where the strongly correlated nature of the underlying state is crucial in obtaining the correct value of the scaling exponent.

The experimental sequence used to produce quantum degenerate Fermi gases has been described in detail in Ref. 5. In brief, we prepare (50 ± 5) \times 10^3 ^{40}\text{K} atoms at temperatures below 15% of the Fermi temperature T_F in a balanced mixture of two magnetic sublevels of the F = 9/2 manifold. The confinement is given by a dipole trap with trapping frequencies \( \omega_{x,y,z} = 2\pi \times (35, 23, 120) \text{ Hz} \). Using Feshbach resonances in either \( mp = -9/2, -7/2 \) or \( mp = -9/2, -5/2 \) mixture 13 14, the interaction strength is tuned in the range 98 \( a_0 \sim 131 \ a_0 \) or 374 \( a_0 \sim 672 \ a_0 \) respectively, where \( a_0 \) is the Bohr radius. After adjusting the scattering length to the desired value, we add a three-dimensional cubic optical lattice. The lattice depth is increased in 200 ms to final values between 6.5 \( E_R \) and 12.5 \( E_R \) in units of the recoil energy \( E_R = \hbar^2/2m\lambda^2 \). Here \( \lambda = 1064 \text{ nm} \) is the wavelength of the laser beams. The lattice beams have Gaussian profiles with \( 1/e^2 \) radii of \( w_{x,y,z} = (160, 180, 160) \ \mu \text{m} \). For a given scattering length and lattice depth, \( J \) and \( U \) are inferred from Wannier functions 16. Their statistical and systematic errors are dominated by the lattice calibration and the accuracies in width and position of the two Feshbach resonances 13 14. Depending on \( U \) and \( J \) the accessible final regimes of the system range from metallic to Mott insulating phases with a double occupancy below 15%.

The preparation of the system is followed by a sinusoidal modulation of the lattice depth with an amplitude of 10% and frequency close to \( U/\hbar \). This causes an increase of the double occupancy to values up to 35% 17 18.

After the modulation the system is in a non-equilibrium state, which we let evolve freely at the initial lattice depth and interaction strength for up to 4 s. This is followed by a sudden increase of the lattice depth to 30 \( E_R \), which prevents further tunneling. We then measure the amount of atoms residing on singly (doubly) occupied sites \( N_s \) (\( N_d \)) by encoding the double occupancy into a previously unpopulated spin state using RF spectroscopy 5. Combining Stern-Gerlach separation and absorption imaging we obtain the single occupancy \( n_s = N_s/N_{\text{tot}} \) double occupancy \( n_d = N_d/N_{\text{tot}} \) and total atom number \( N_{\text{tot}} = N_s + N_d \).

We record the time evolution of the total atom number and the single and double occupancy, see Fig. 2. The double occupancy is found to decay exponentially, while additional losses are also observed on longer timescales, which lead to a reduction of the total atom number. To extract the doublon lifetime we model these decays by a set of coupled rate equations:

\[
\begin{align*}
\Delta \dot{N}_d &= - \left( \frac{1}{\tau_{\text{d}}} + \frac{1}{\tau_{\text{m}}} + \frac{1}{\tau_{\text{loss}}} \right) \Delta N_d \\
\dot{N}_{d,0} &= - \left( \frac{1}{\tau_{\text{m}}} + \frac{1}{\tau_{\text{loss}}} \right) N_{d,0} \\
\dot{N}_s &= \frac{1}{\tau_{\text{d}}} \Delta N_d - \frac{1}{\tau_{\text{loss}}} N_s
\end{align*}
\]

Here \( \Delta N_d \) is the additional amount of double occupancy created by the lattice modulation as compared to the equilibrium population \( N_{d,0} \). The three time constants correspond to three independent local decay processes differing in the type of site they affect: the lifetime of doublons \( \tau_{\text{d}} \) describes a population flow from doubly occupied to singly occupied lattice sites visible as a fast decay (rise) of double (single) occupancy within 0.01 – 1 s. The other two times denote loss time constants, which lead to a reduction of the total atom number: \( \tau_{\text{loss}} \) corresponds to losses affecting both site types in the same manner, which is only observed in the total atom number. Additional inelastic losses on doubly occupied sites are summarized by \( \tau_{\text{m}} \), visible as a simultaneous decay of both the total atom number and double occupancy. Changes of the decay times during the decay and higher order terms in the rate equations are excluded.

![Fig. 2: Comparison of the time evolution of the double occupancy and total atom number for different ratios U/6J.](image)

We simultaneously fit the time-dependent populations obtained from Eq. [1] to this dataset and to a corresponding reference dataset without lattice modulation. Since the modulation does not change the losses, this procedure removes the influence of \( \tau_{\text{m}} \) and \( \tau_{\text{loss}} \), allowing for a reliable determination of the doublon lifetime \( \tau_{\text{d}} \). The model and the observation are found to agree very well within experimental uncertainties, as shown in Fig. 2.

We measure this doublon lifetime for various tunneling and interaction strengths, covering a parameter range...
where \( J \) and \( U \) each differ by at least a factor of four (inset Fig. [3]). The lifetime in units of the tunneling time is plotted logarithmically versus the ratio \( U/6J \) in Fig. [3]. The data is well described by an exponential function:

\[
\frac{\tau_D}{\hbar/J} = C \exp \left( \frac{U}{6J} \alpha \right).
\]

The scaling exponent \( \alpha \) is found to be \( \alpha = 0.82 \pm 0.08 \) with \( C = 1.6 \pm 0.9 \). We find fair agreement with our calculations of the doublon lifetime. The systematic deviation of the data for the two spin mixtures [10] seems to indicate that the data show physics beyond Eq. (2).

In the following we argue that this exponential scaling of the doublon lifetime originates from a high order scattering process involving several single atoms as scattering partners. In the preparation of the non-equilibrium state by lattice modulation, we create holes as well as doublons in the bulk and thus drive the system into a compressible state. An isolated doublon has an energy \( U \), which it must transfer to other excitations in order to decay. In the compressible state the most relevant excitations are metallic with a typical energy scale of \( 6J \). Thus a doublon must scatter with several fermions. The number of scattering partners is on the order of \( n = U/6J \). The matrix element \( M \) for the decay rate \( \Gamma \) may be estimated via perturbation theory \( M \sim \frac{J}{U} \times \frac{J}{U} \times \cdots \times \frac{J}{U} \) and \( \Gamma/J \propto M^2 \). Using Stirling’s formula, we then find the same scaling behavior as in Eq. (2). Here \( \alpha \) is a parameter on the order of unity and depends at most logarithmically on \( U/6J \).

For the quantitative analysis a few assumptions are made: we consider the decay of a single doublon in the background of a homogeneous compressible system. This is justified since most of the doublons are created in the central region of the trap, where the filling is highest, and decay at most within a few sites of where they are produced (the estimated travel distance for a random walk during the decay process is not more than \( \sqrt{\tau_D J/\hbar} \lesssim 10 \) sites, which is less than the cloud radius). We neglect spin excitations and collisions between doublons, as typical energy transfers in these processes are on the order of \( J^2/U \), which leads to a subdominant exponential scaling in \( U^2/J^2 \). Further, the population of higher bands can be excluded, since \( U \) is always smaller than half the band gap. We also note that confinement assisted decay of doublons after quantum tunneling to the edge of the cloud is unlikely, as the accessible confinement energy is smaller than \( U \) and the tunneling rate is very small.

The complete Hamiltonian of the system may be written as \( H = H_{pf} + H_d + H_{fd} \), where \( H_{pf} \) describes the background fermions, \( H_d \) is the on-site energy of doublons and \( H_{fd} \) is the interaction of the doublon with the background fermions.

The strong Hubbard repulsion between the fermions leads to the concept of projection, where two fermions are forbidden from occupying the same site. In this case, the fermions can only hop in the presence of a hole on a neighboring site and are governed by the Hamiltonian

\[
H_{pf} = -J \sum_{\langle ij \rangle, \sigma} (1 - n_{i, \sigma}) c_{i, \sigma}^{\dagger} c_{j, \sigma} (1 - n_{j, \sigma}),
\]

where \( c_{i, \sigma}^{\dagger} \) (\( c_{i, \sigma} \)) is the fermion creation (annihilation) operator and \( n_{i, \sigma} \) is the number operator for fermions with spin \( \sigma \) (\( \bar{\sigma} \) denotes spin opposite to \( \sigma \)). Expanding out this Hamiltonian we obtain \( H_{pf} = H_{f} + H_{p} \), with

\[
H_{f} = -J \sum_{\langle ij \rangle, \sigma} c_{i, \sigma}^{\dagger} c_{j, \sigma} - \mu \sum_{i, \sigma} c_{i, \sigma}^{\dagger} c_{i, \sigma},
\]

\[
H_{p} = J \sum_{\langle ij \rangle, \sigma} \left( n_{i, \sigma} c_{i, \sigma}^{\dagger} c_{j, \sigma} + c_{i, \sigma}^{\dagger} c_{j, \sigma} n_{j, \sigma} \right),
\]

where \( H_{f} \) describes the free Fermi sea and \( H_{p} \) describes the interaction induced by the projection and can be thought of as a process in which a fermion scatters off the Fermi sea and creates a particle-hole pair. We assume that the system is close to half filling (chemical potential \( \mu = 0 \)), but we checked that the result is not very sensitive to the precise value of the filling as shown by the shaded region in Fig. [3]. We neglect the term \( n_{i, \sigma} c_{i, \sigma}^{\dagger} c_{j, \sigma} n_{j, \sigma} \) in \( H_{p} \) as we have checked that it leads to negligibly small corrections to the doublon decay rate [20].

We now consider the propagation and decay of a doublon in the background state of the projected Fermi sea.
The on-site energy of the doublon is $H_d = U \sum d_i^d d_i^c$, where $d_i^d$ is a doublon creation operator. The doublon-fermion interaction $H_{df}$ is given by

$$H_{df} = J \sum_{\langle ij \rangle} (d_i^d d_j^c + d_j^d d_i^c) c_{i \sigma}^c c_{j \sigma}$$

and shown that the lifetime of doublons scales exponentially with the ratio of interaction energy to kinetic energy. We argue that the dominant decay mechanism of doublons is a high order scattering process involving several single particles, and we obtain fair agreement with the experiments based on a perturbation theory calculation. The results have implications also for the simulation of strongly correlated lattice models with ultracold atoms as they pose adiabaticity constraints on the sweep rates for the system parameters. On a qualitative level, the results should also be applicable to bosonic atoms and might help to explain the long equilibration times recently observed [21].

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14. We determine the widths of both resonances by measuring the zero-crossing via dephasing of Bloch oscilla-
This yields $\Delta B_{-7/2,-9/2} = 7.5 \pm 0.1$ G and $\Delta B_{-5/2,-9/2} = 7.6 \pm 0.1$ G, the latter differing from [13].


[19] Separate fits to the two spin mixtures yield values of $\alpha_{-9/2,-5/2} = 0.75 \pm 0.10$ and $\alpha_{-9/2,-7/2} = 1.00 \pm 0.14$.
